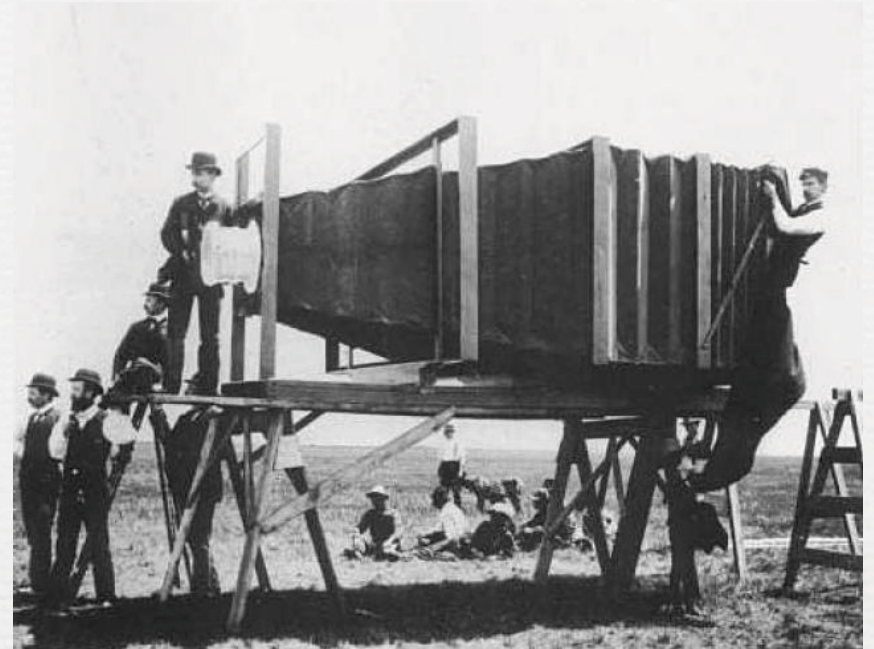


Computation is the New Optics: Coded Imaging in Computational Photography

Frédo Durand
MIT CSAIL

Traditional imaging

- ♦ Optics forms the image
- ♦ Sensor/film just record
- ♦ Displayed image is pretty much the optical image
- ♦ This is the same for digital camera
 - post-processing is limited

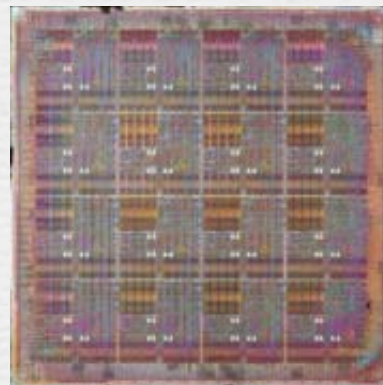


Computational Photography

- ◆ Computation between optical and displayed image
 - The optical image is not the final product
 - Can be modified heavily
- ◆ Goals:
 - Alleviate physical limitation
 - Capture more information (e.g. depth)
- ◆ Best to design computation and optics together



Generalized imaging



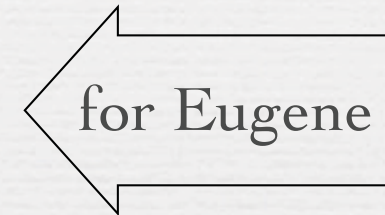
Lots of computation



Final image

Related fields

- ♦ Computer graphics
 - Try to reproduce reality
- ♦ Computer Vision
 - Extract information from visual array
- ♦ Image Processing
- ♦ Computational Imaging
- ♦ Astronomy/telescope
- ♦ Radar
- ♦ Microscopy
- ♦ Medical Imaging



Big ideas in Comp. Photo.

♦ Goals:

- Beat physics, better image quality/quantity
- More data (depth, etc.)
- Seeing the unseen
- Creative choices during post-process
- New visual media

♦ Multiple-exposure imaging & multiplexing

♦ Coded imaging

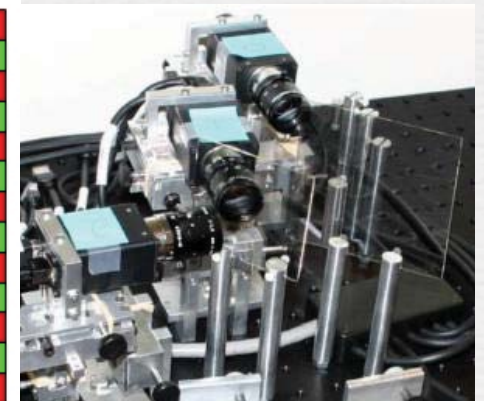
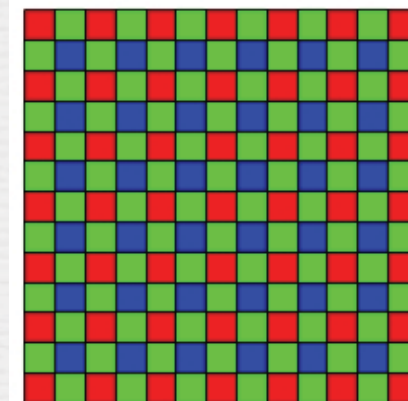
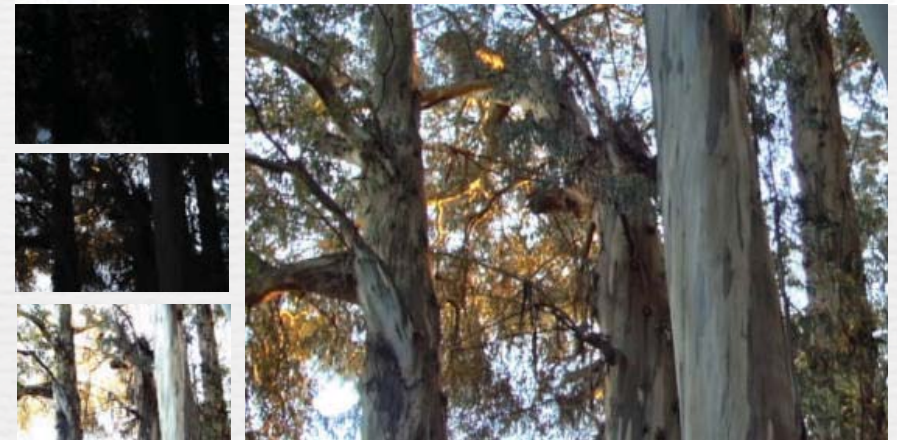
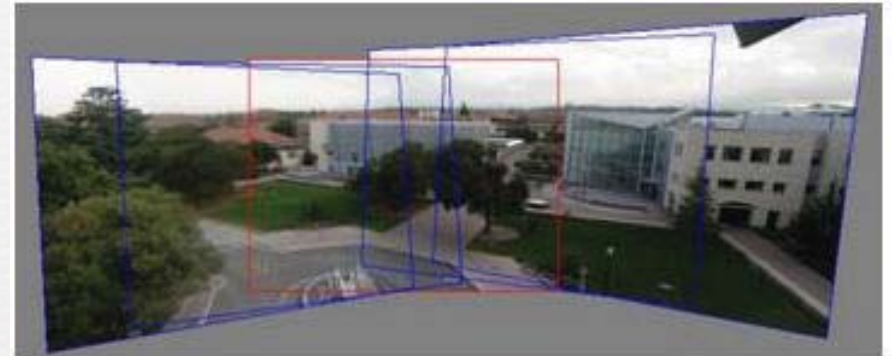
♦ Prior information

♦ The raw data is high dimensional

♦ Active imaging

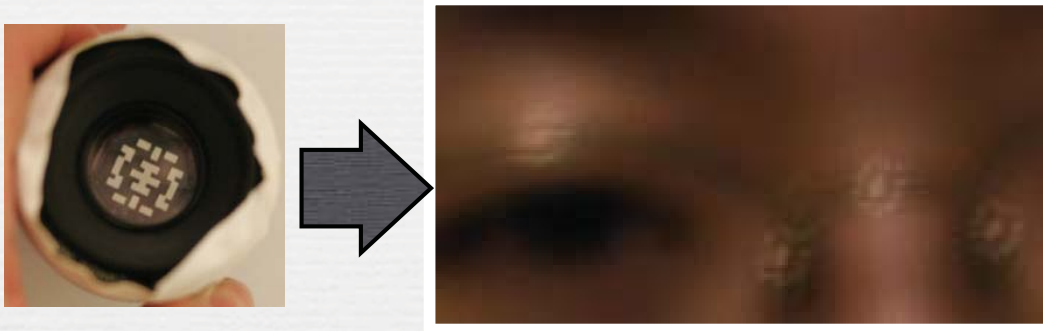
Multiple-exposure & multiplexing

- ◆ Expand capabilities by combining multiple images
- ◆ Multiplex through time, assorted pixels, beam splitters, camera array
- ◆ e.g.
 - Panorama stitching
 - High-dynamic-range imaging
 - Focus stacks
 - Photomontage
 - Super-resolution

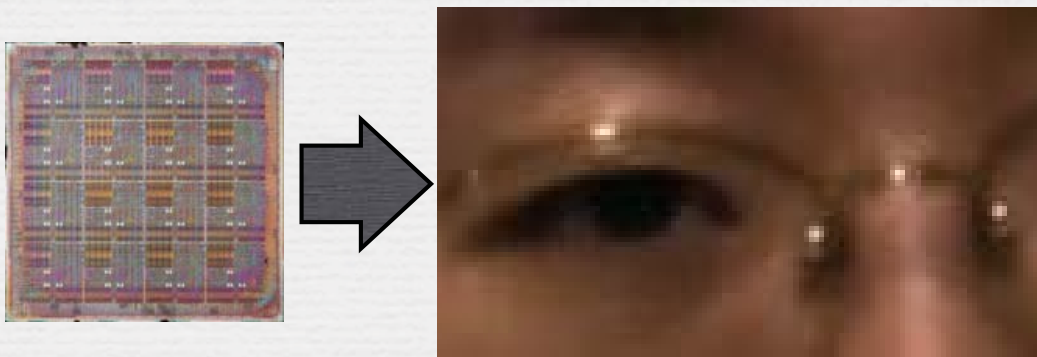


Coded Imaging

Optics encodes information



Computation decodes



♦ e.g.

- wavefront coding
- coded aperture
- flutter shutter
- motion-invariant
- compressive sensing
- heterodyning
- warp-unwarp

Natural signal prior

- ◆ Statistics that distinguish images of the world from random signals
- ◆ Use to “bias” algorithms to output more likely results or to disambiguate ill-posed problems
- ◆ Extension of regularization
- ◆ e.g.
 - Denoising
 - Deconvolution
 - Compressive sensing
 - Light field prior



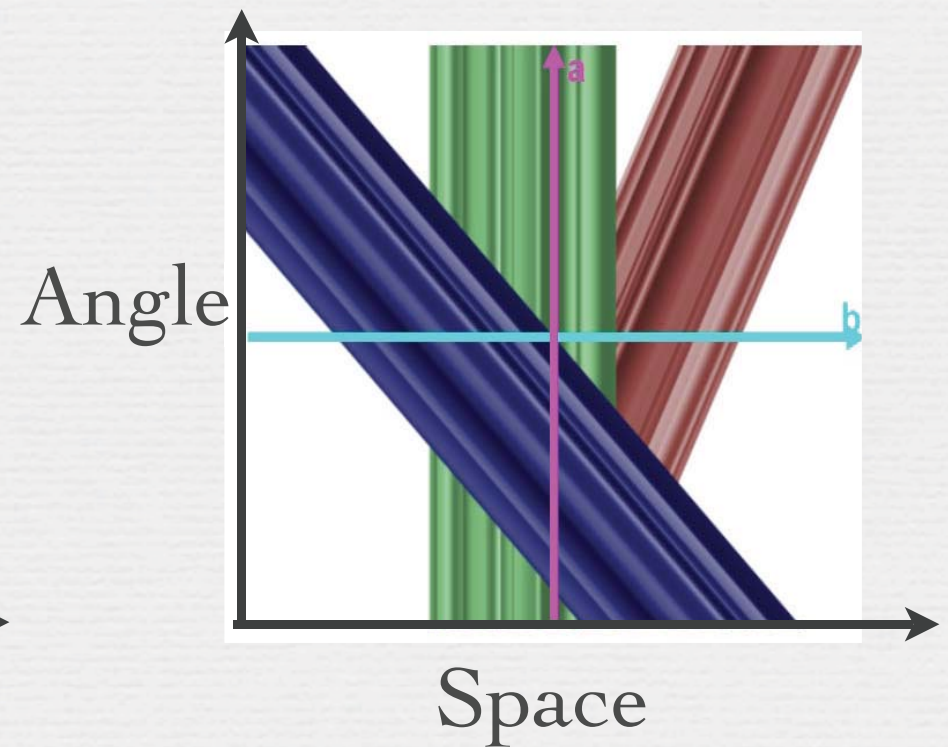
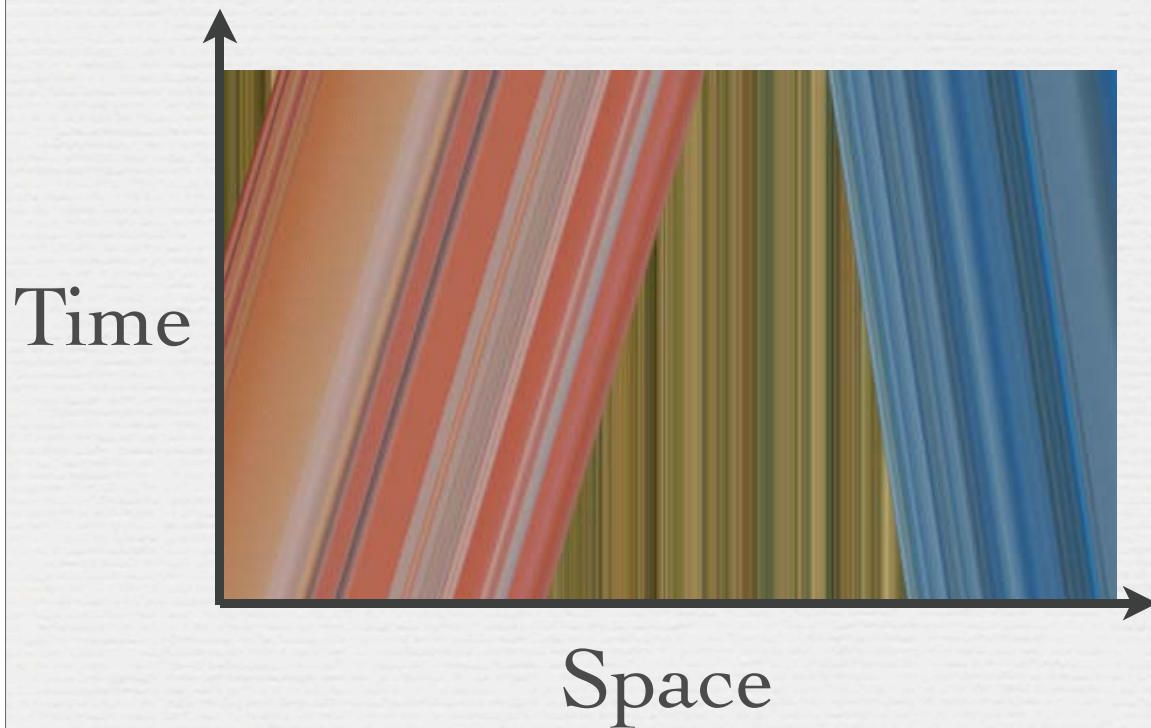
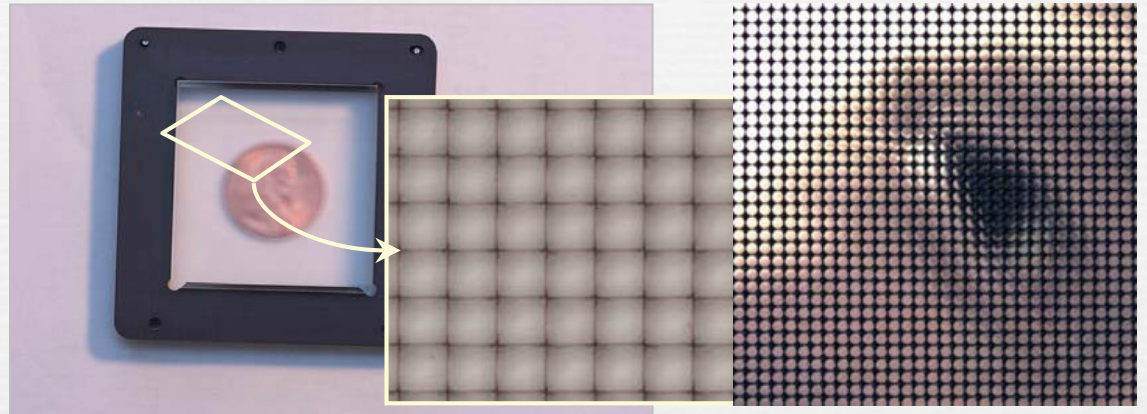
Random



“Natural” image

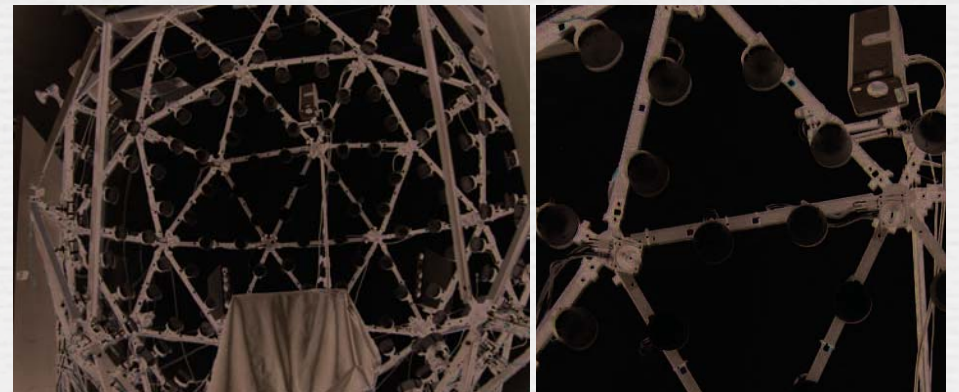
The raw data is high dimensional

- ♦ Light field: 4D (space-angle)
- ♦ Time space: 3D
- ♦ +Fourier



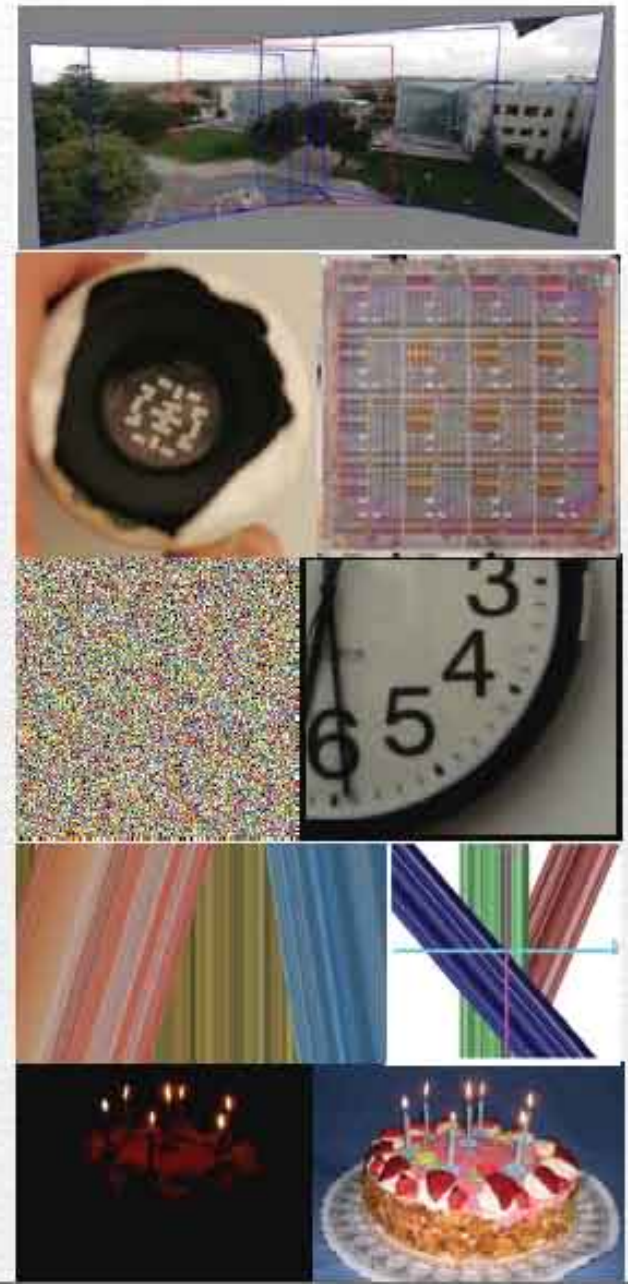
Active imaging

- ◆ Modulate light to facilitate information gathering
- ◆ e.g.
 - Flash/no flash
 - Light stages
 - Dual imaging
 - Structured-light scanning



Recap: Big ideas in Comp. Photo.

- ◆ Multiple-exposure & multiplexing
- ◆ Coded imaging
- ◆ Prior information
- ◆ The raw data is high dimensional
- ◆ Active imaging



Computational Photography: Coded Blur Removal

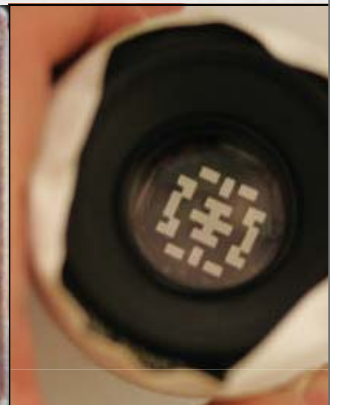
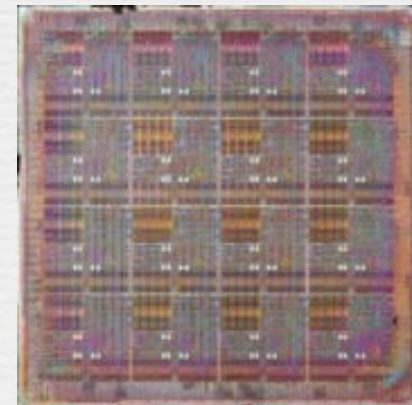
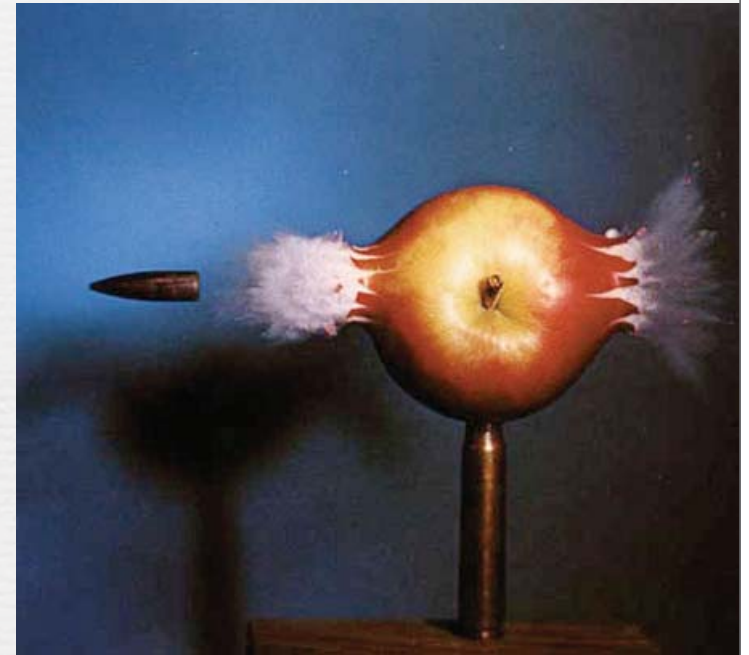
Frédo Durand
MIT CSAIL

with Anat Levin, Peter Sand, Rob Fergus,
Taeg Sang Cho, Bill Freeman



This talk: blur removal

- ◆ Blur often reduces image quality
 - Motion blur, diffraction, defocus
- ◆ Traditional solution:
 - Faster shutter speed, smaller aperture, bigger aperture
 - Often increases noise (gathers less light)
- ◆ Today: computational solution
 - Remove blur given **single** image
 - Imaging hardware + software



Motion blur

Most of the scene is static

red bull is moving
from left to right



Can we remove the blur?

- ◆ Given single image with blur
- ◆ Blur is mostly a linear process, just invert it
 - called deconvolution
- ◆ But we need to know the exact blur
- ◆ But the process needs to be invertible
 - Lose as little information as possible



Deconvolution



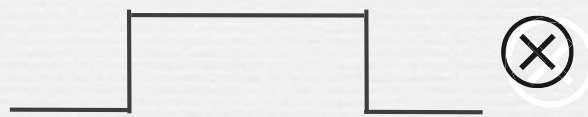
Kernel identification



Input blurry image

?

=



Correct kernel



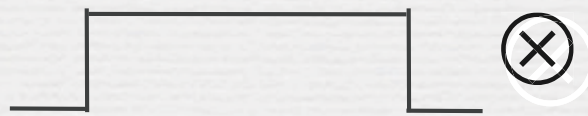
Output from correct kernel



Input blurry image

?

=



Wrong kernel



Output from wrong kernel

Kernel identification

- ♦ The kernel is spatially varying

Entire image
deblurred with kernel
corresponding to the
cans' velocity



Challenge with deblurring

- ◆ Blur destroys information
 - Often box filter

Deblurring given known blur:



blurred input



deblurred



static input

Challenge with DoF and motion

- ◆ Blur destroys information
 - Often box filter
- ◆ Kernel identification
 - Spatially varying



This talk: two opposite solutions

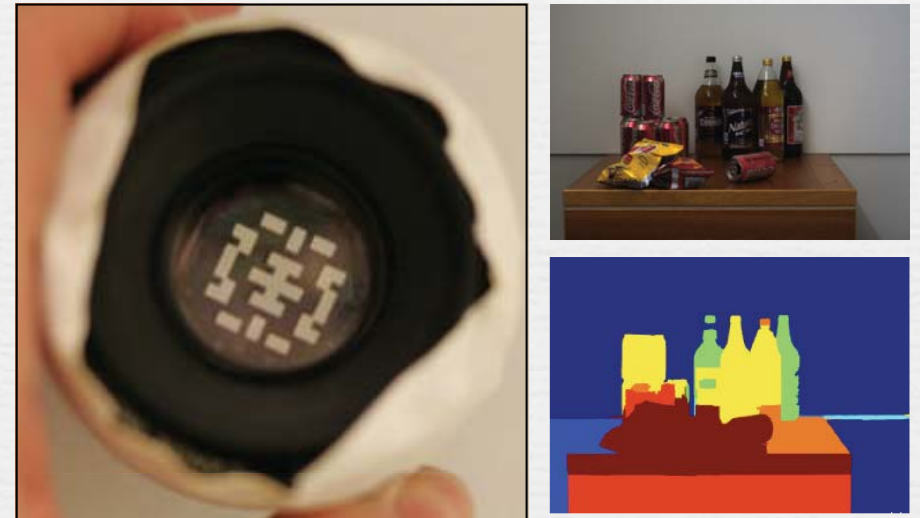
- ♦ Make blur very variant
 - Easier to identify
- ♦ Make blur invariant
 - No need to identify
- ♦ In both cases, we also make the blur easy to invert
 - Preserve information

Outline

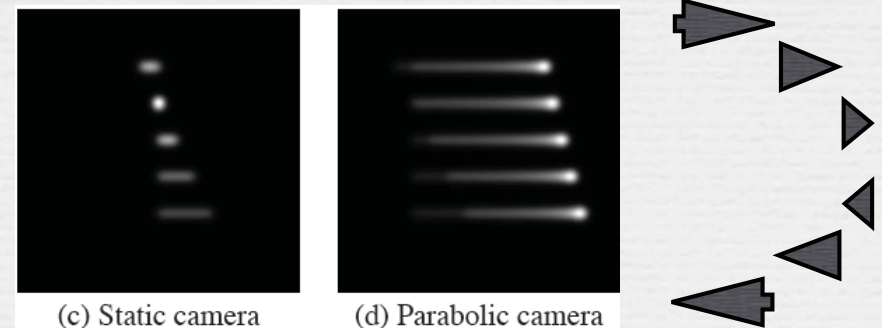
- ◆ Natural image prior: help the inversion



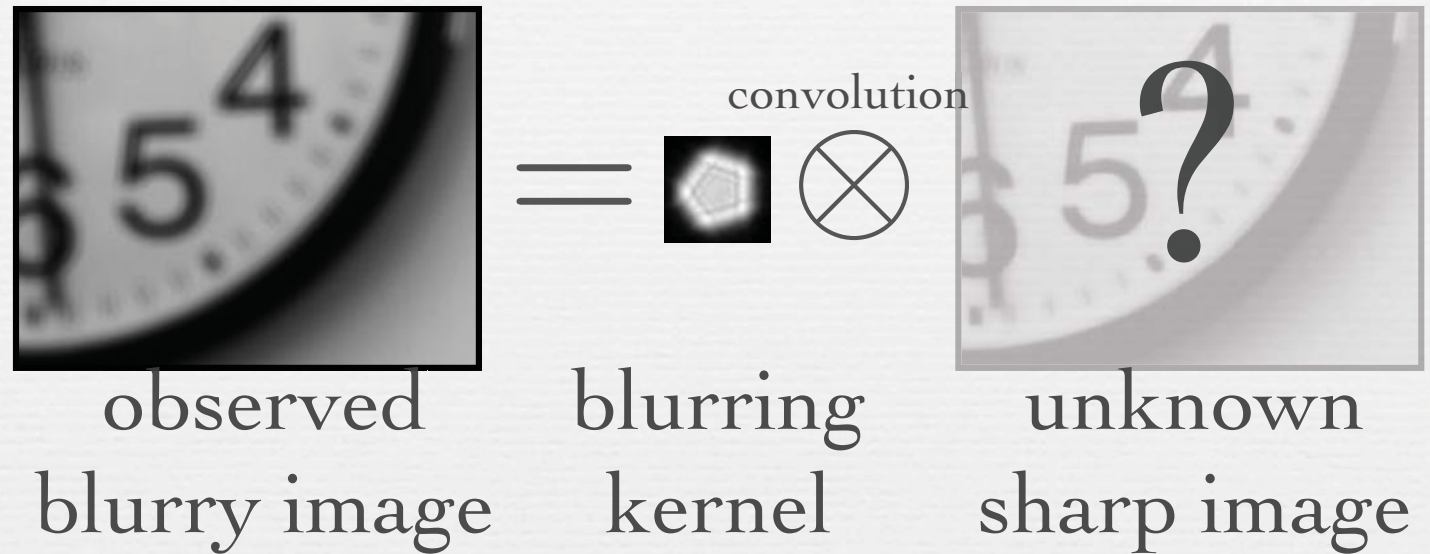
- ◆ Coded aperture: make blur vary more with depth



- ◆ Motion-invariant photography



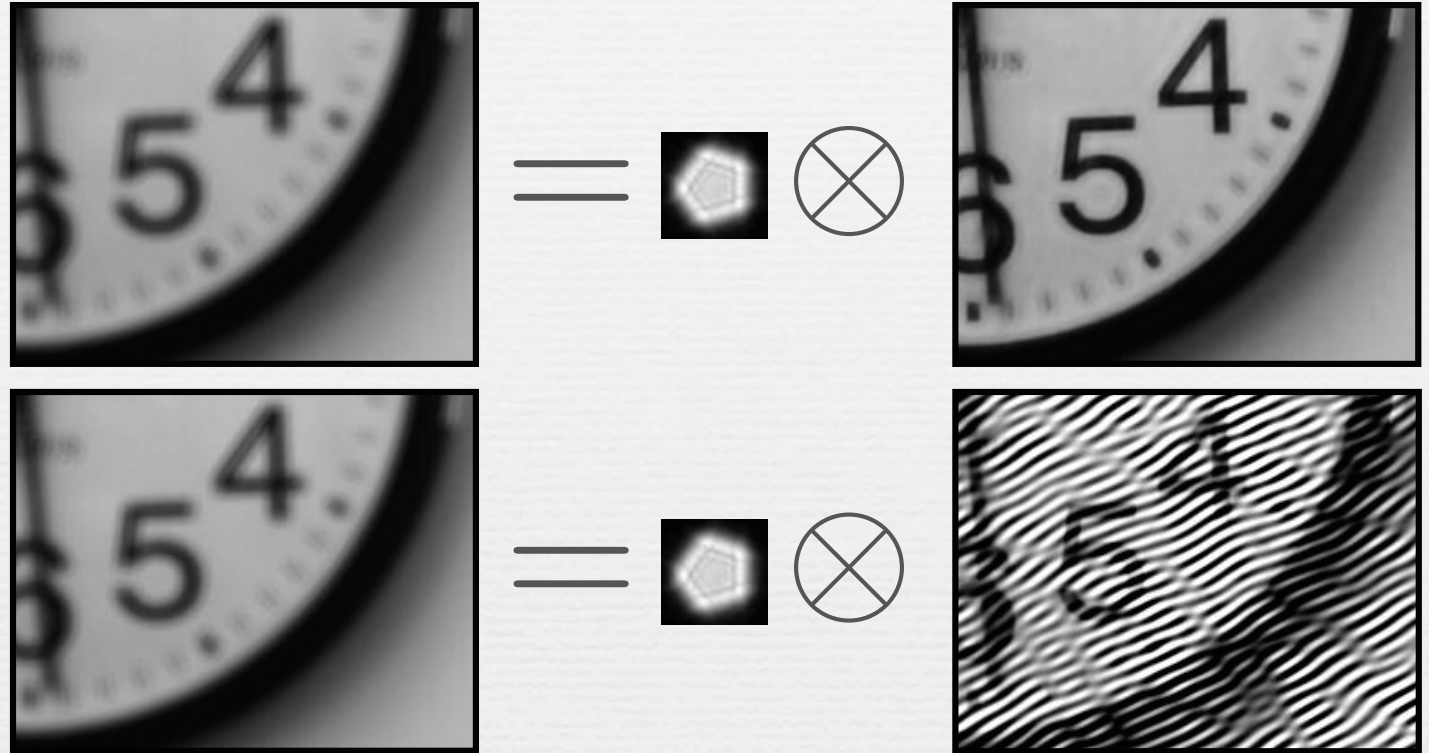
Deconvolution with known kernel



- ◆ Given blurred image and blurring kernel
infer sharp image

Deconvolution challenge

- ♦ Ill-posed



- ♦ Traditional algorithms lead to ringing

Richardson-Lucy
deconvolution



Idea 1: Natural image prior

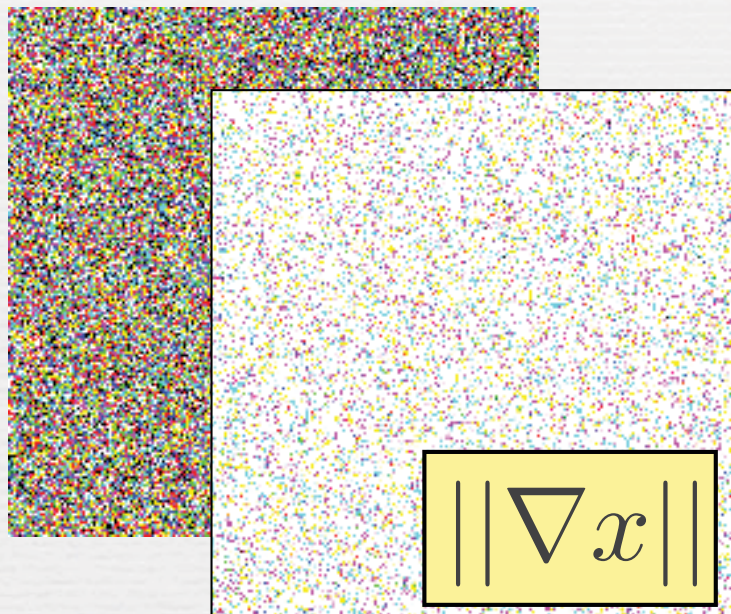
- ♦ Random 2D arrays of colors don't look like the world around us



- ♦ If we can characterize natural images, we can bias algorithms to output better results

Sparse derivatives prior

- ♦ Natural images have sparse derivative
(the gradient is small almost everywhere)



- ♦ Add an optimization term
(a.k.a. regularization)

Pay penalty where gradient is non-zero

$$\sum ||\nabla x||^{0.8}$$

Sparsity prior for deconvolution



Input

$$\sum ||\nabla x||^2$$

spread error

$$\sum ||\nabla x||^{0.8}$$

localize error



Richardson-Lucy



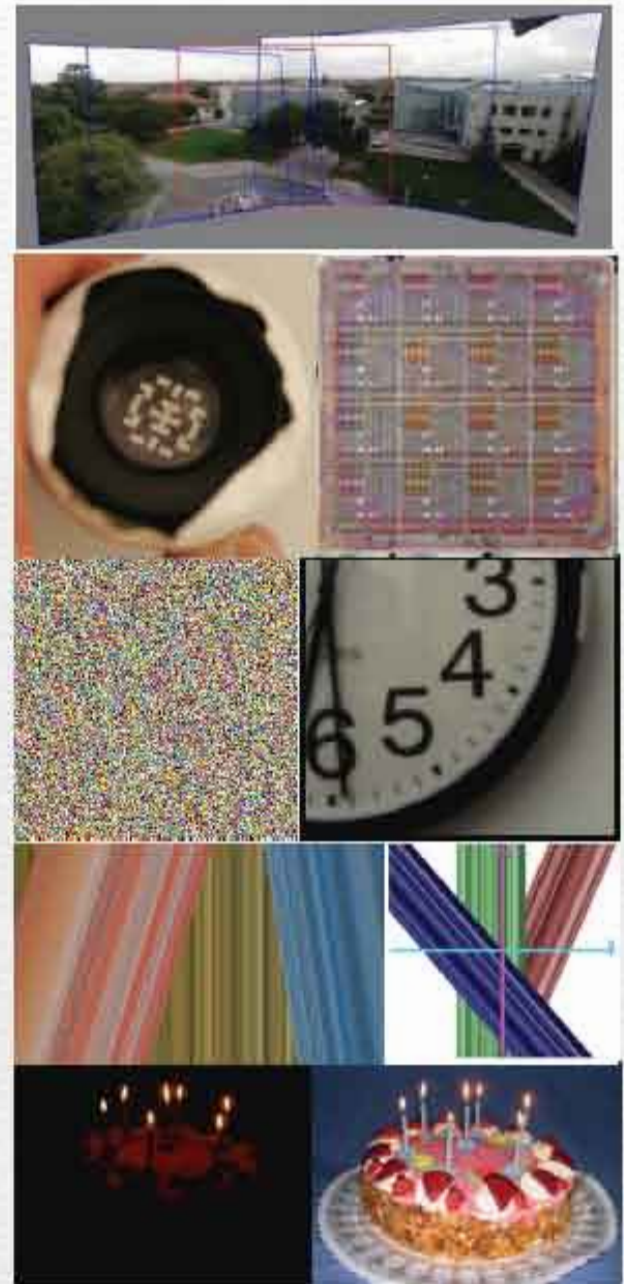
Gaussian prior



Our sparse prior

Big ideas in Comp Photo

- ◆ Multiple-exposure & multiplexing
- ◆ Coded imaging
- ◆ **Prior information**
- ◆ The raw data is high dimensional
- ◆ Active imaging

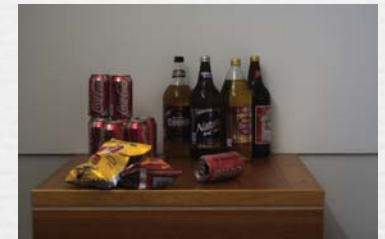


Outline

- ◆ Natural image prior:
help inversion



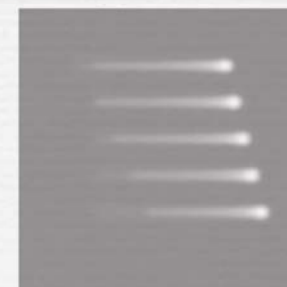
- ◆ Coded aperture:
make blur vary
more with depth



- ◆ Motion-invariant
photography



(c) Static camera



(d) Parabolic camera



Image and Depth from a Conventional Camera with a Coded Aperture

*With Anat Levin, Rob Fergus,
Bill Freeman [Siggraph 2007]*

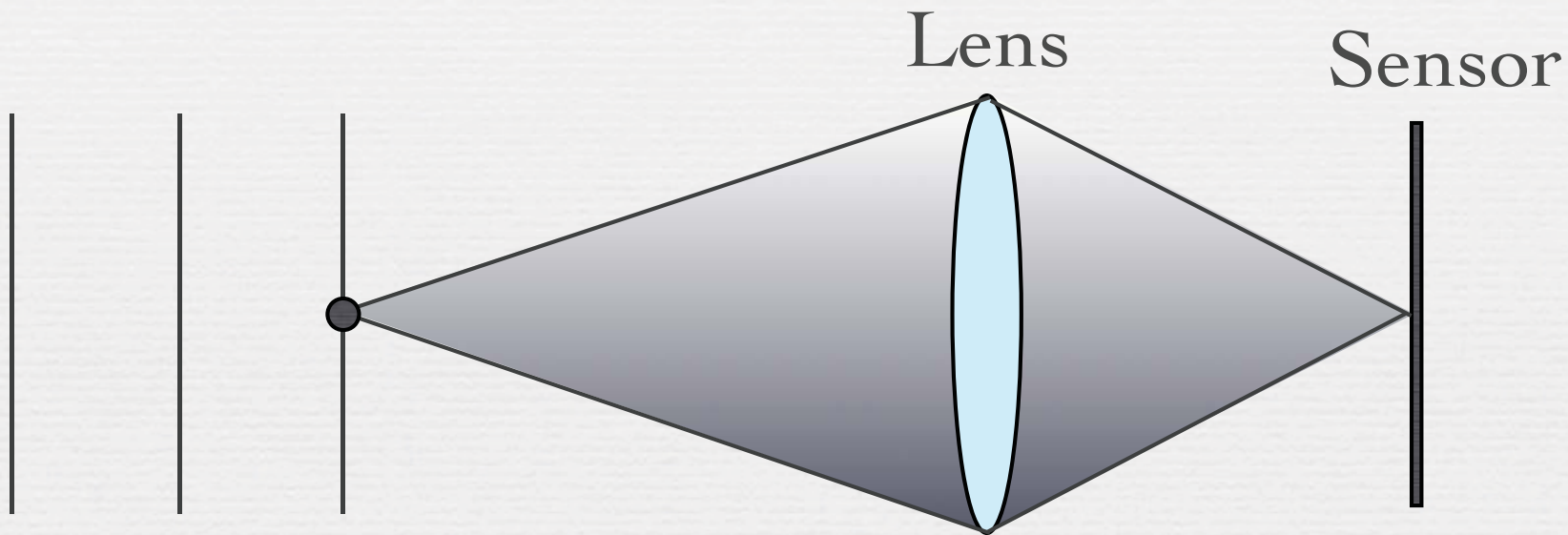


RGB & coarse depth from single image



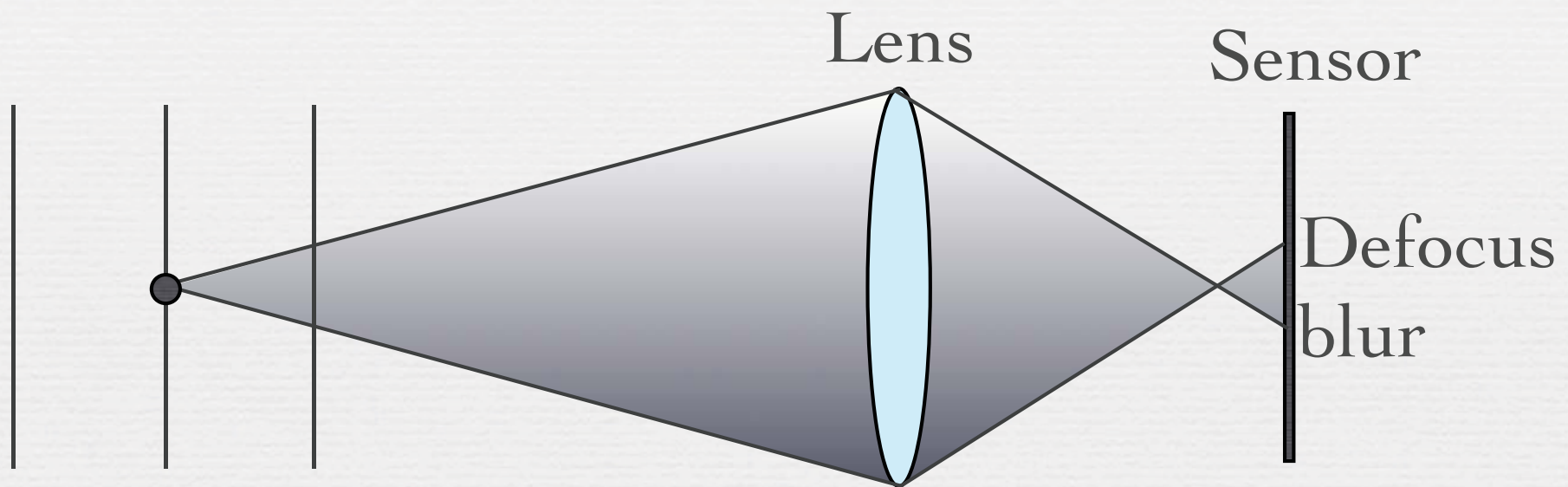
Defocus & depth

- ◆ Objects at focusing distance are sharp



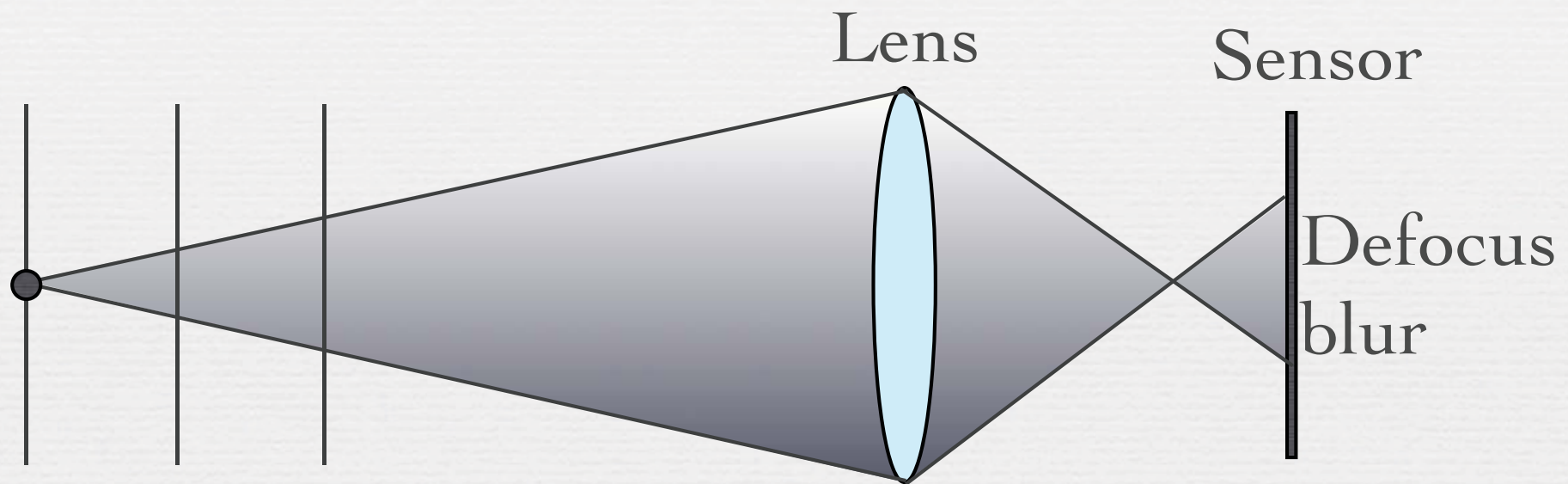
Defocus & depth

- ◆ Objects far from focusing distance are blurrier



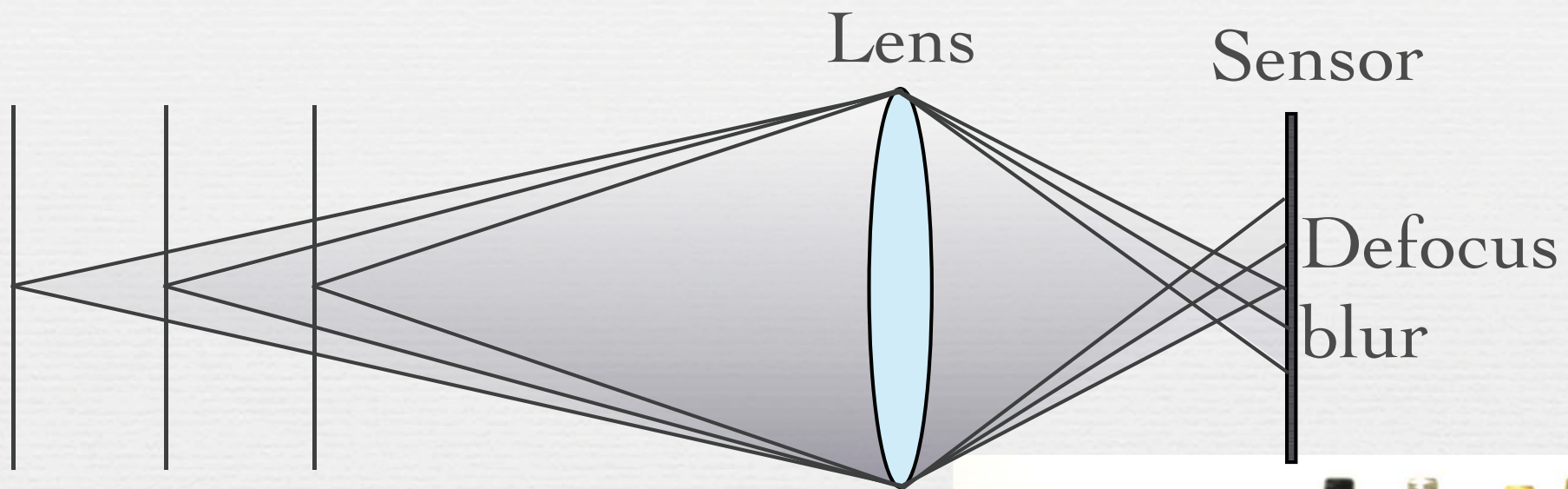
Defocus & depth

- ◆ Objects far from focusing distance are blurrier



Defocus & depth

- ◆ Objects far from focusing distance are blurrier

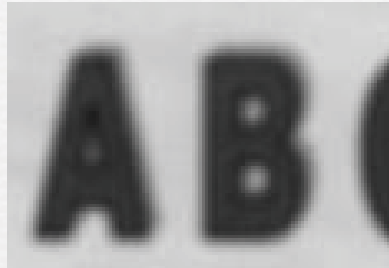


- ◆ By inferring blur, we can infer depth



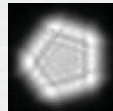
Strategy

- ◆ Input:



- ◆ For each candidate depth, try to deconvolve with corresponding kernel

...



too far



correct



...

too close

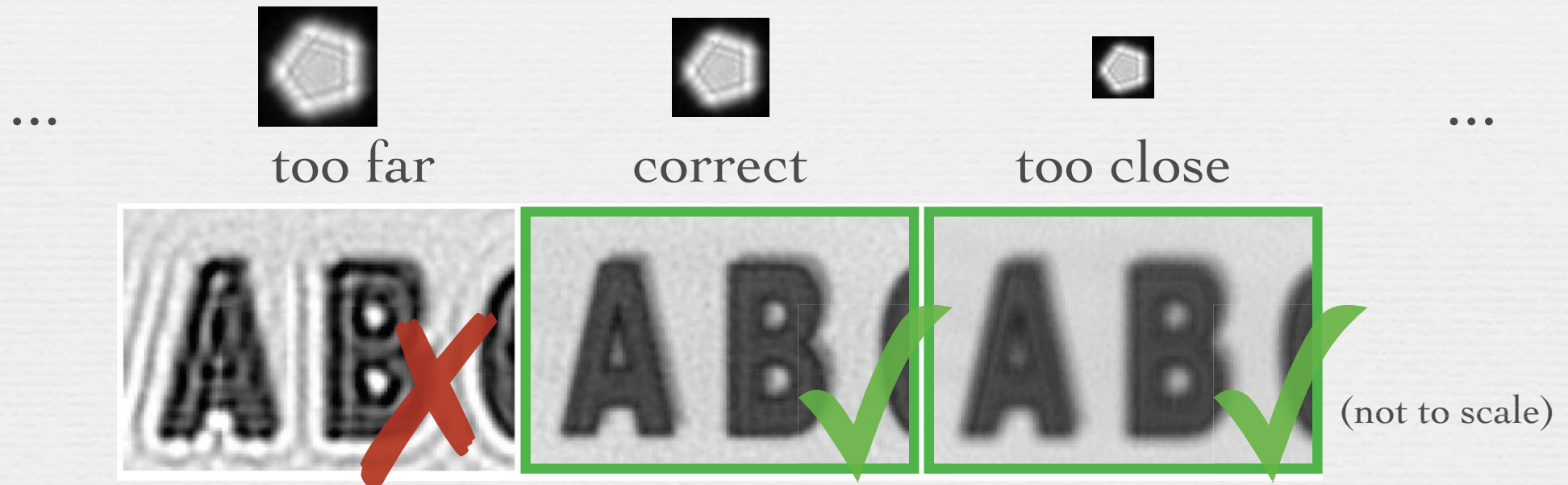


(not to scale)

- ◆ For each pixel, keep best kernel/depth

Challenge: hard to infer depth

- ♦ For each candidate depth, try to deconvolve with corresponding kernel



- ♦ “Too close” not so different from “correct”

Solution: Coded aperture

- ♦ Put a mask (code) on aperture plane (diaphragm)
 - ➔ more structured blur
 - ➔ easier to identify kernel/depth
 - ➔ easier to remove blur



Conventional



Coded

Build your own coded aperture



Open the lens



Open the lens



Open the lens



Open the lens



Open the lens



Open the lens



Open the lens



Now the critical part



Cardboard mask



Cardboard mask



Cardboard mask



Cardboard mask



Cardboard mask



Cardboard mask



Cardboard mask



Close it up



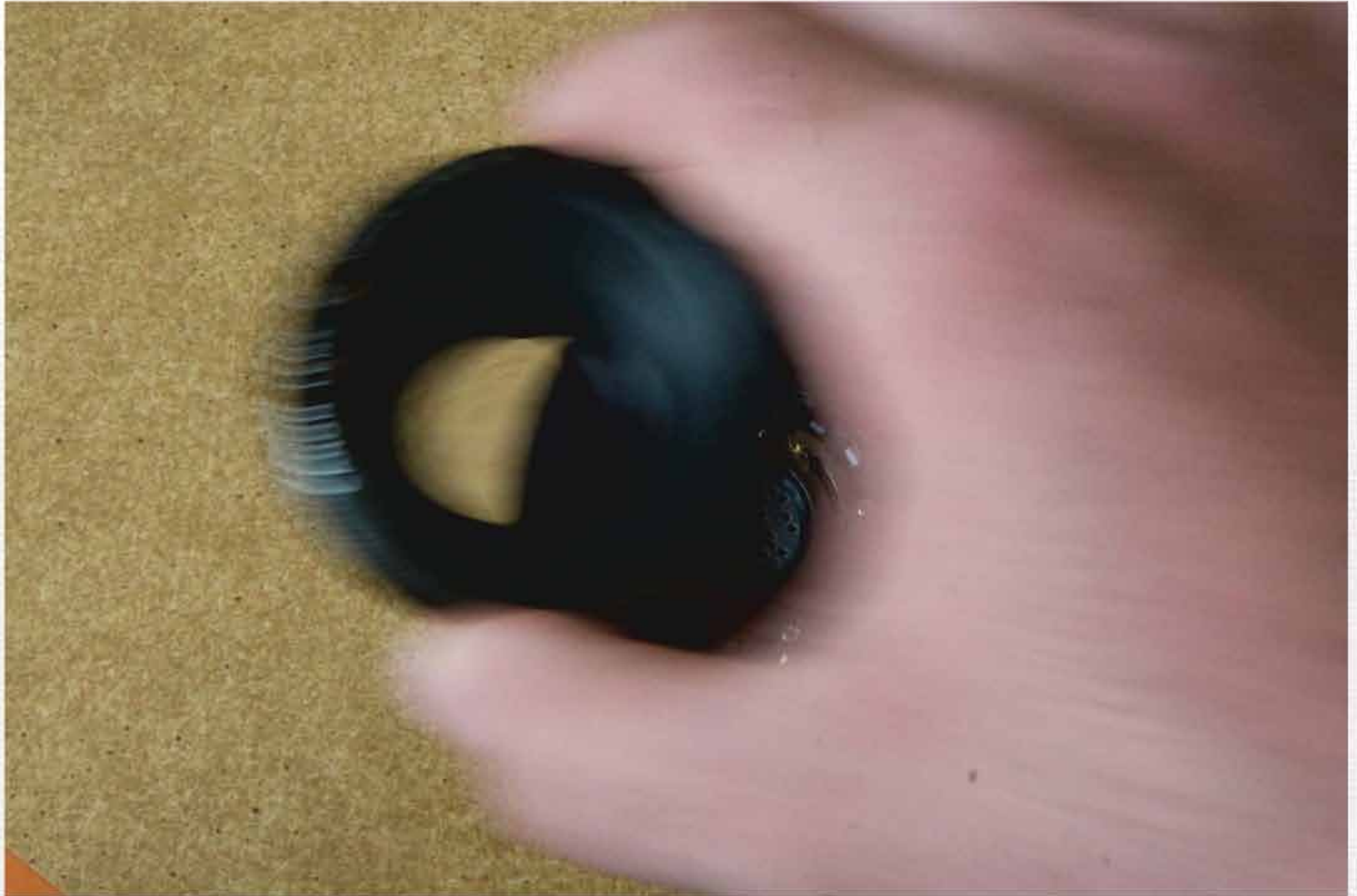
Close it up



Close it up



Close it up



Close it up



Close it up



Close it up



Voilà!



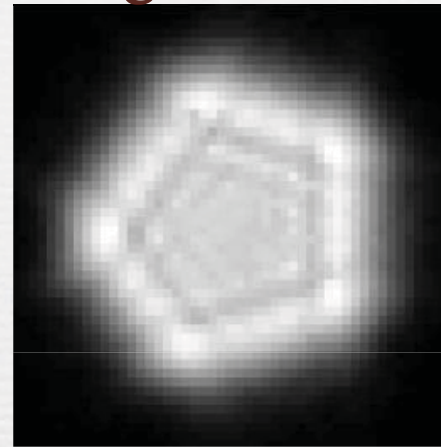
Traditional aperture defocus

- ♦ Shape of mask scaled according to depth

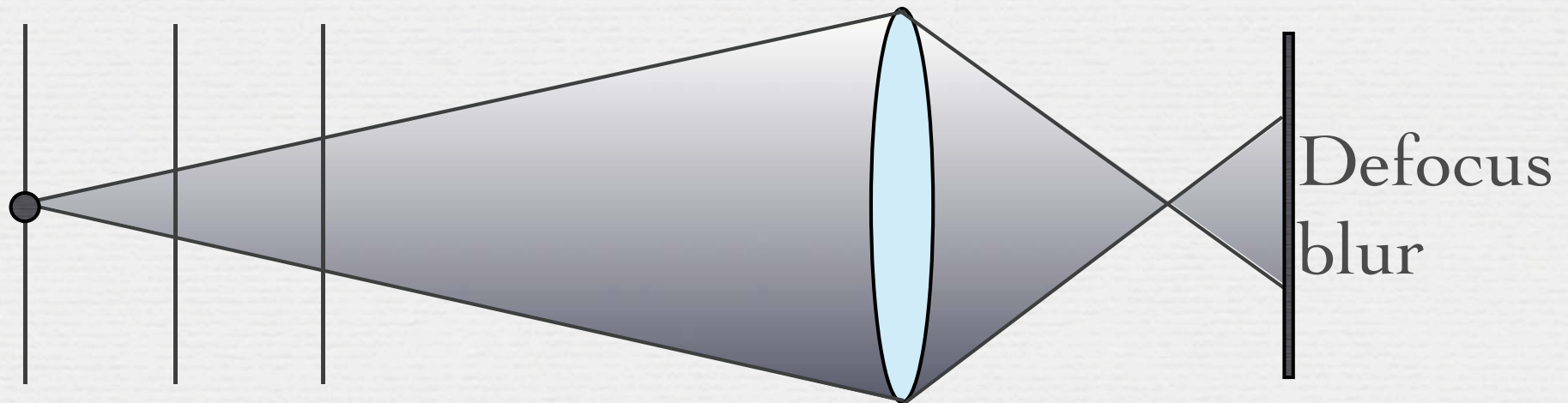


Conventional

Image of defocused point light



Conventional



Coded aperture defocus

- ◆ Shape of mask scaled according to depth

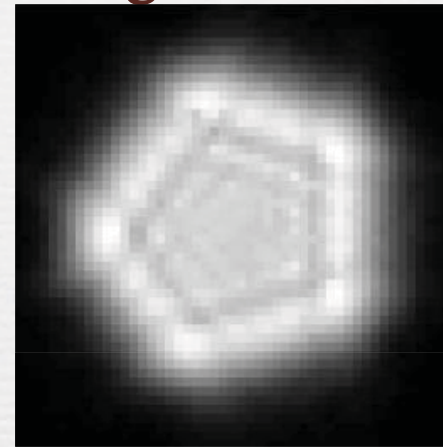
Image of defocused point light



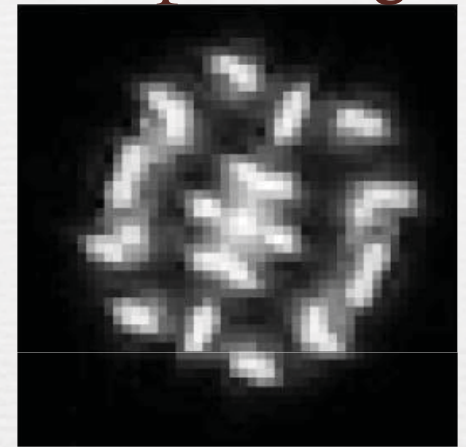
Conventional



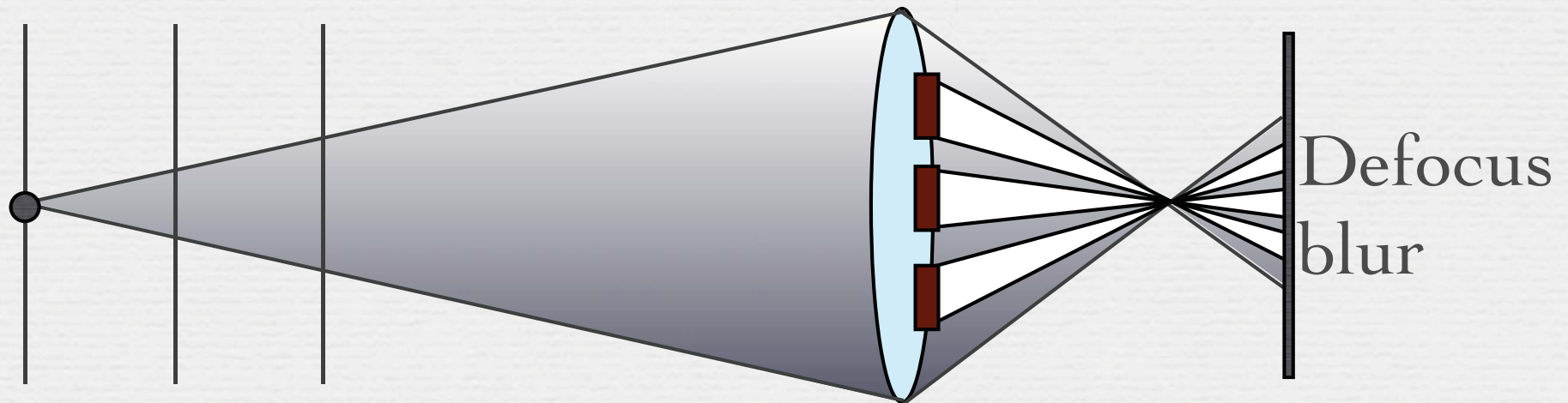
Coded



Conventional



Coded



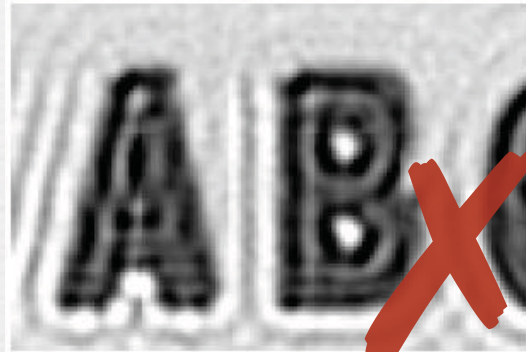
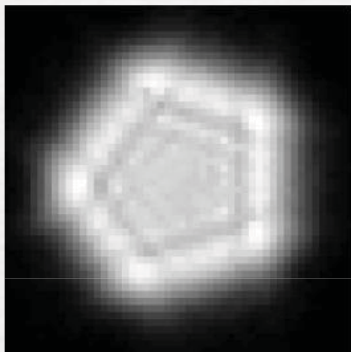
Why code helps

- ♦ Wrong blur is making more mess

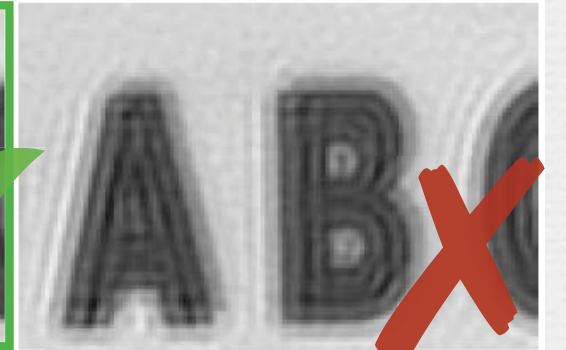
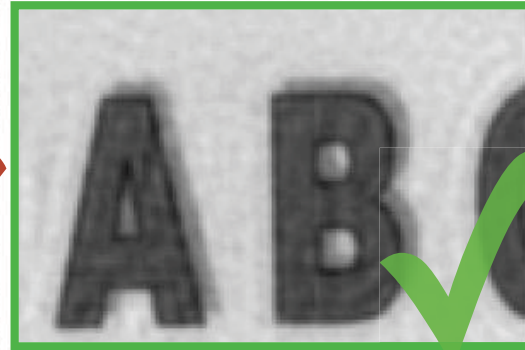
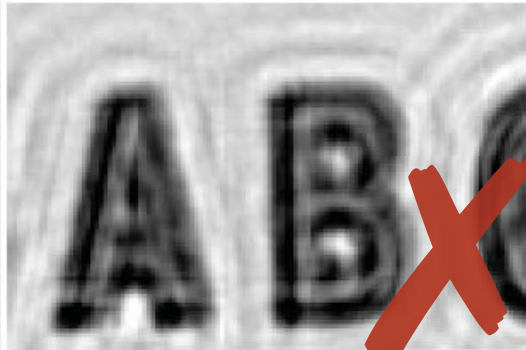
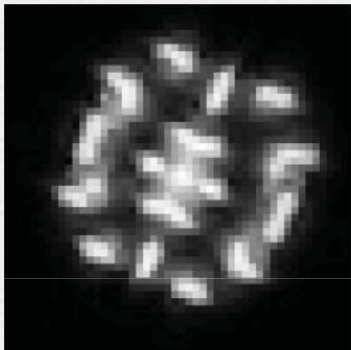
too far

correct

too close



Conventional aperture



Coded aperture

Input



Deconvolved (all-focus)



Close up



Original image



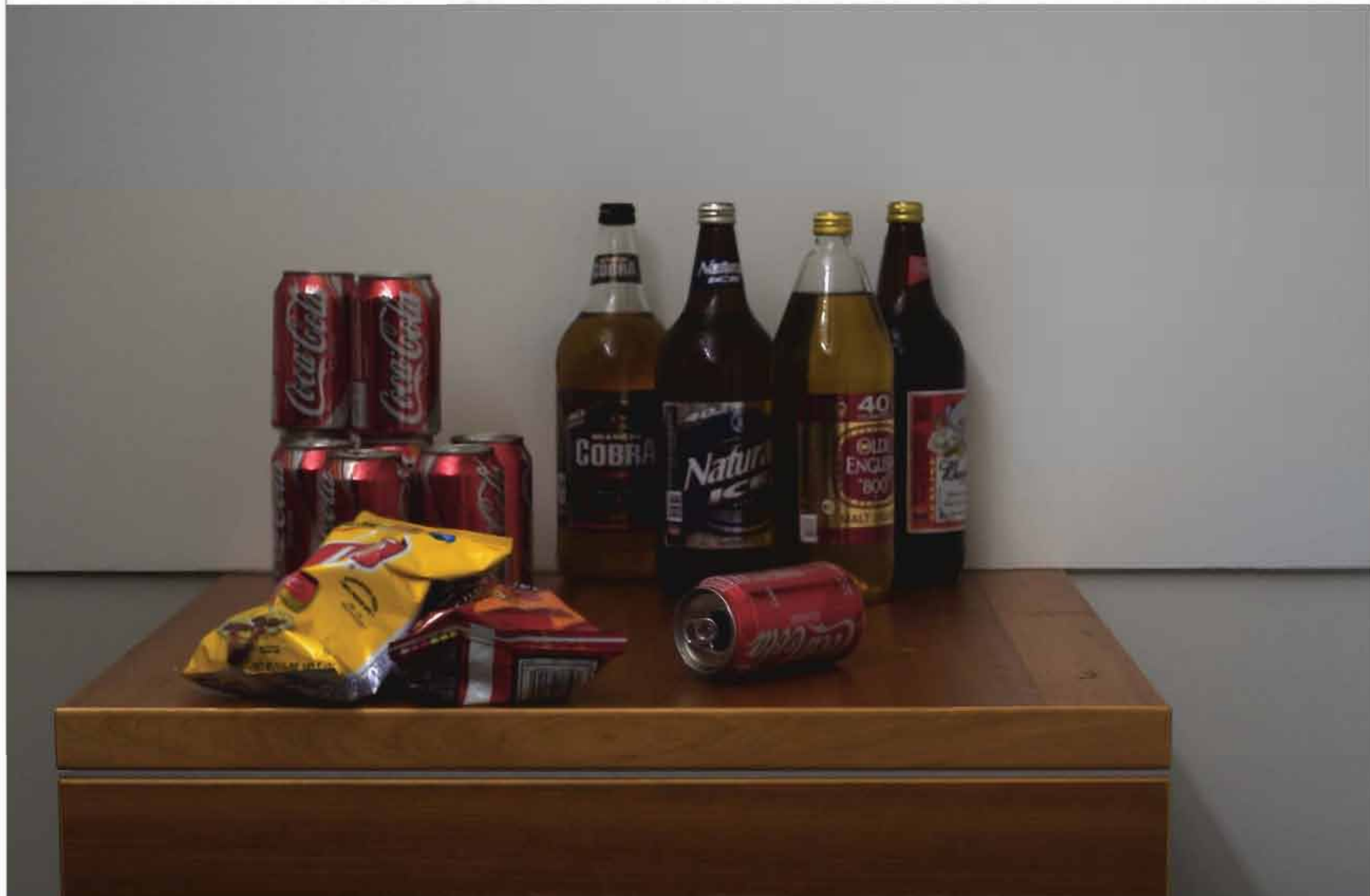
All-focus image



Depth



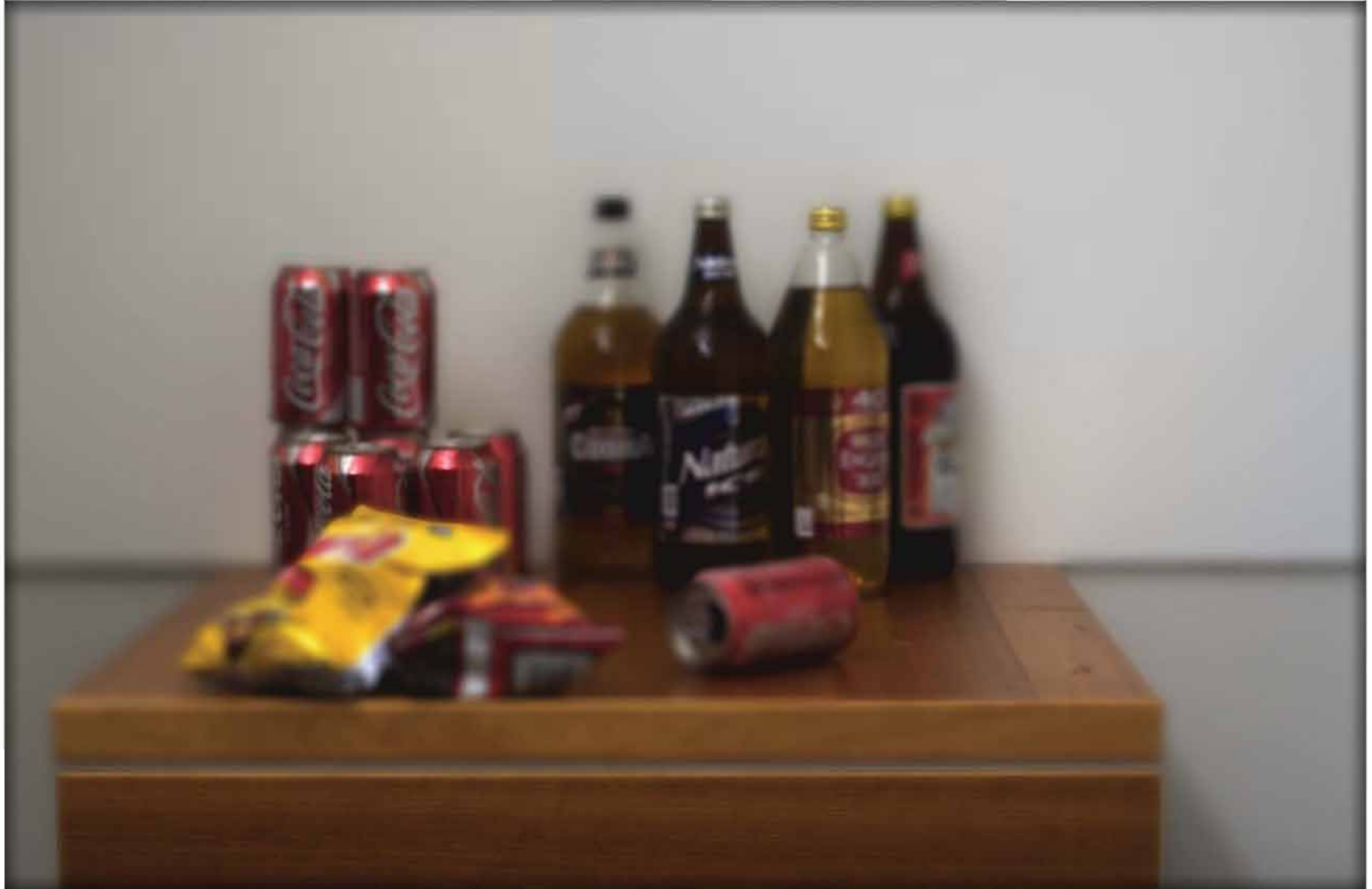
Deconvolved (all-focus)



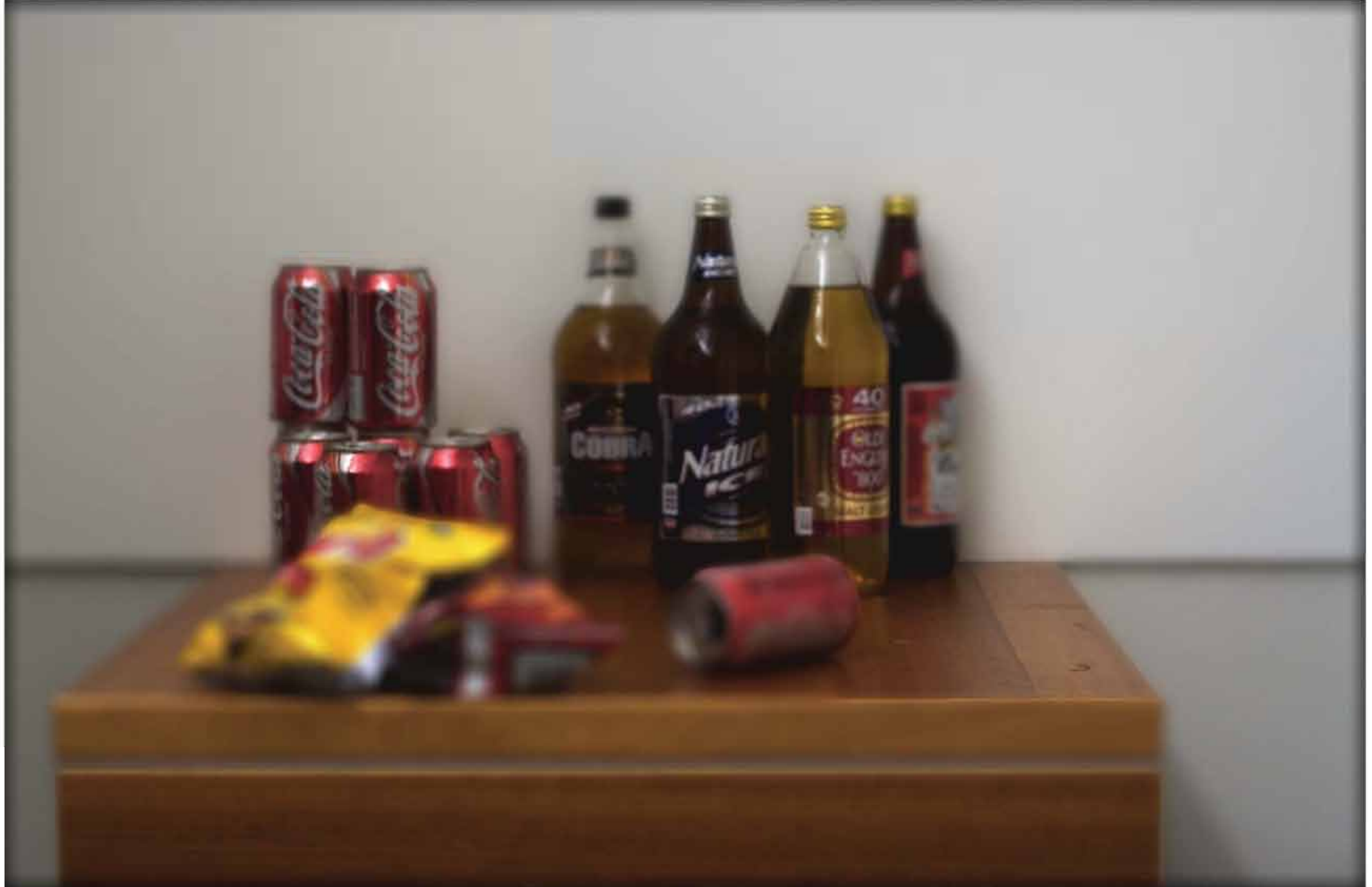
Refocusing (from single image!)



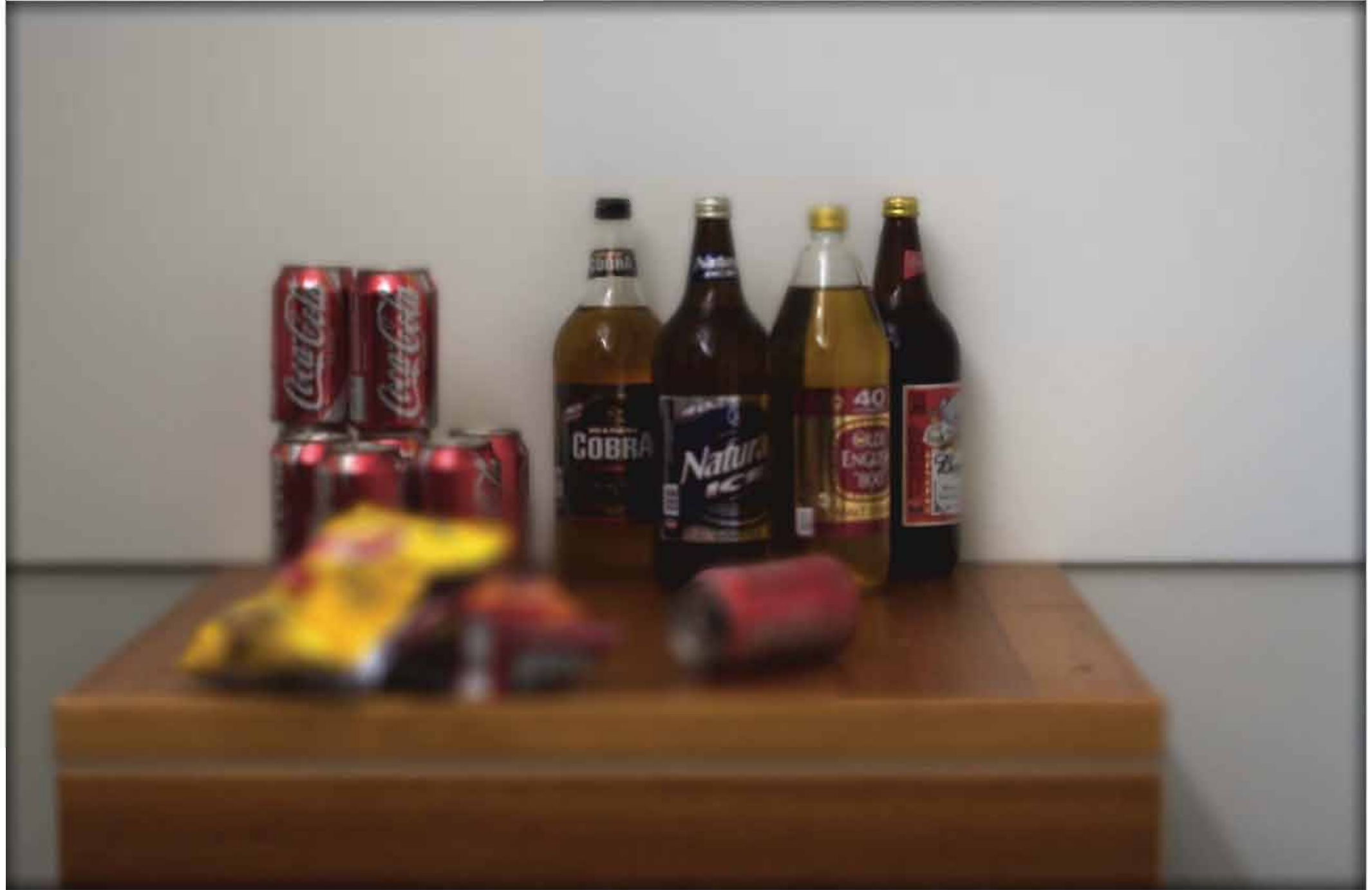
Refocusing (from single image!)



Refocusing (from single image!)



Refocusing (from single image!)



Results



Input



Deconvolved



Refocusing (from single image!)



Refocusing (from single image!)

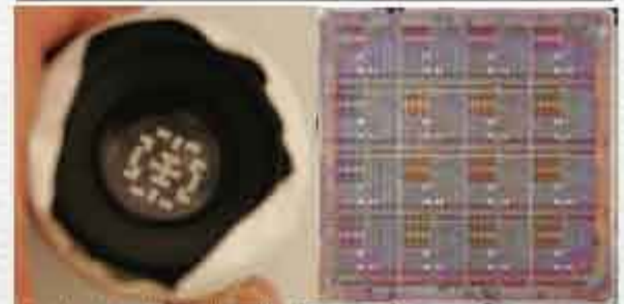


Refocusing (from single image!)



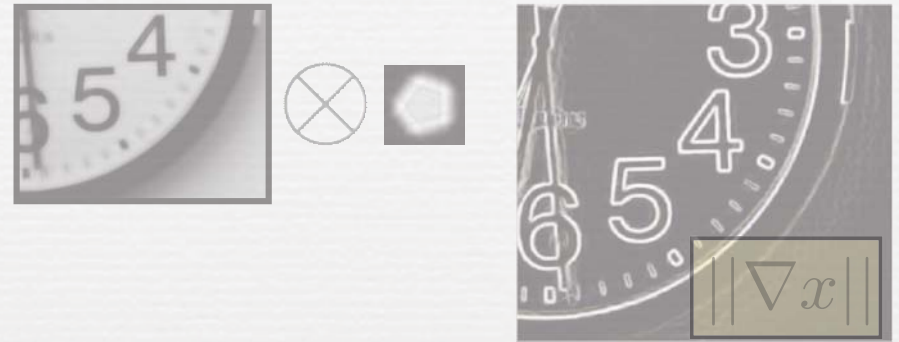
Big ideas in Comp Photo

- ◆ Multiple-exposure & multiplexing
- ◆ **Coded imaging**
- ◆ **Prior information**
- ◆ The raw data is high dimensional
- ◆ Active imaging

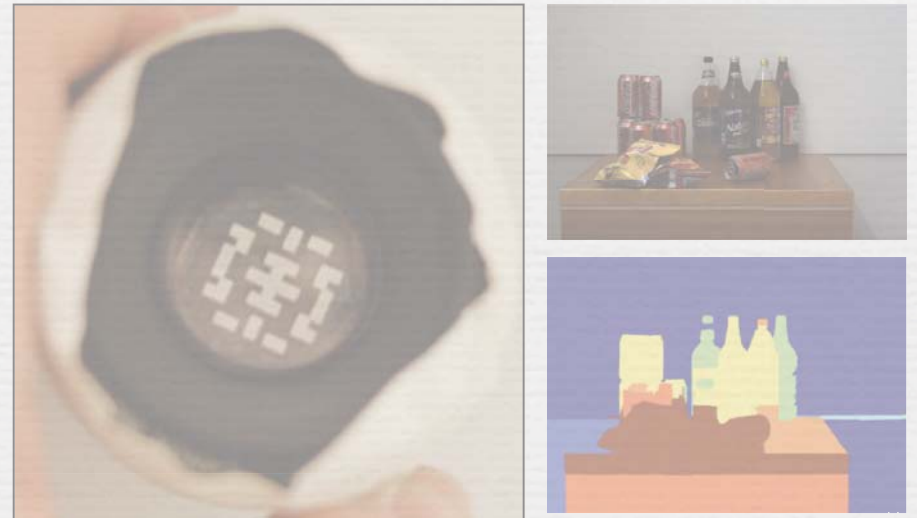


Outline

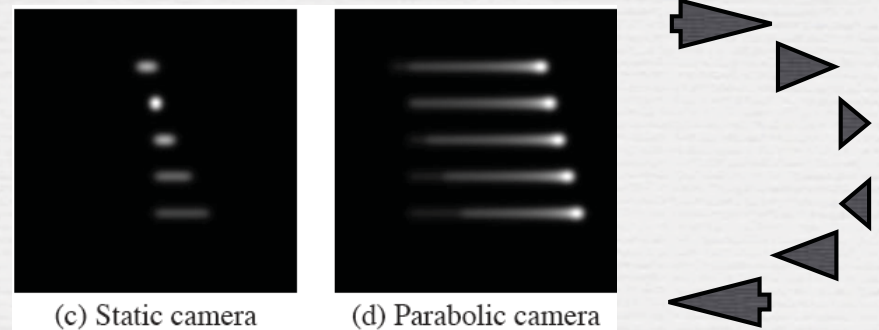
- ◆ Natural image prior



- ◆ Coded aperture:
make blur vary
more with depth



- ◆ Motion-invariant
photography



Counter intuitive solution:

To reduce motion blur, increase it!

- move camera as picture is taken
- **Makes blur invariant to motion- can be removed with spatially uniform deconvolution**
 - kernel is known (no need to estimate motion)
 - kernel identical over the image (no need to segment)
- **Makes blur easy to invert**

Inspiration: depth invariant defocus

- **Wavefront coding - manipulate optical element**

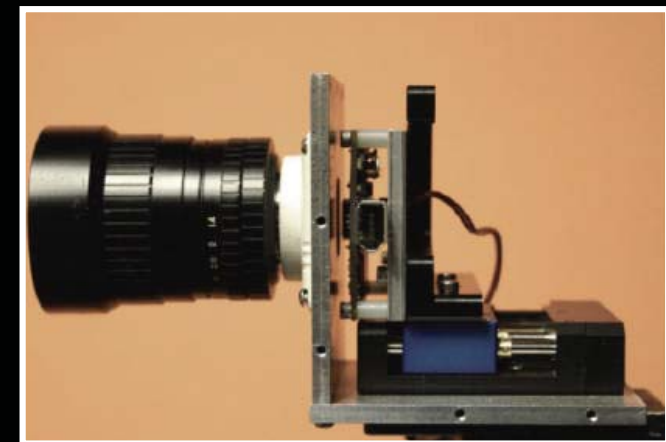
Cathey and Dowski 94



- **Vary object/detector distance during integration**

- Hausler 72

- Nagahara, Kuthirummal, Zhou, Nayar 08



Motion invariant blur– disclaimers:

- **Assumes 1D motion (e.g. horizontal)**
- **Degrades quality for static objects**

Controlling motion blur



Controlling motion blur

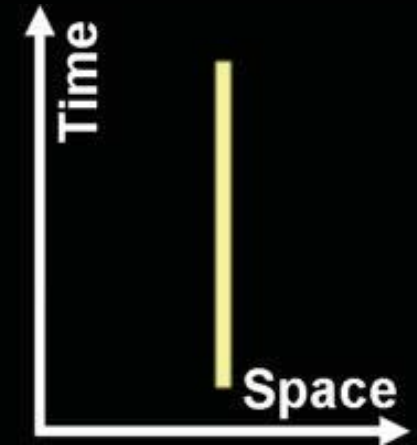
Static- recorded image



Can we control motion blur?

Controlling motion blur

Static- recorded image

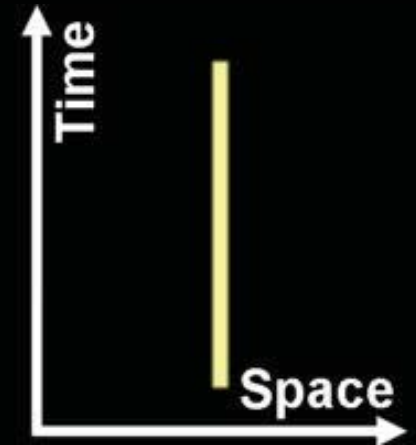


Tracking- sensor displacement

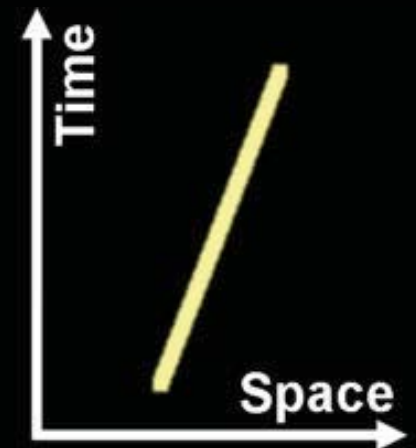


Controlling motion blur

Static- recorded image

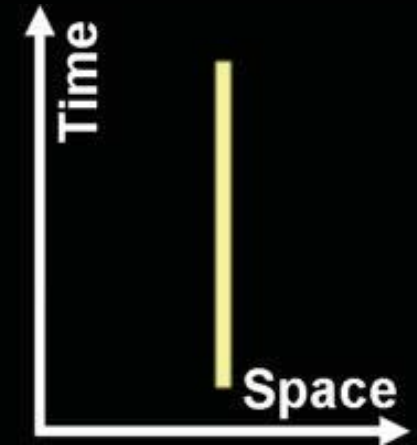


Tracking- recorded image

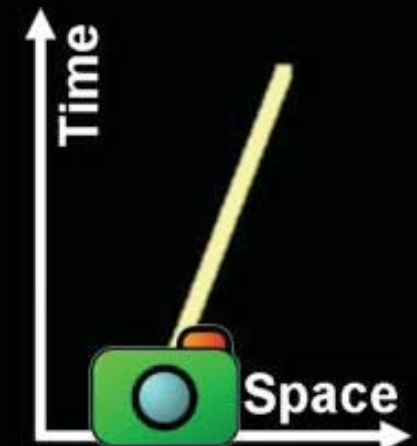


Controlling motion blur

Static- recorded image

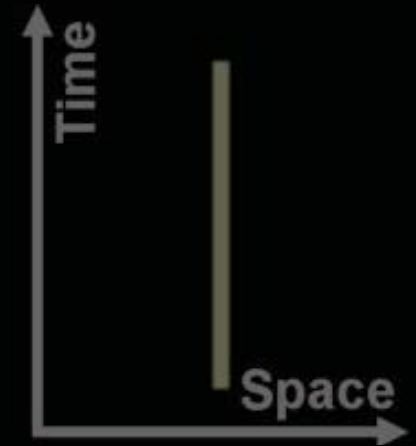


Tracking- view from sensor

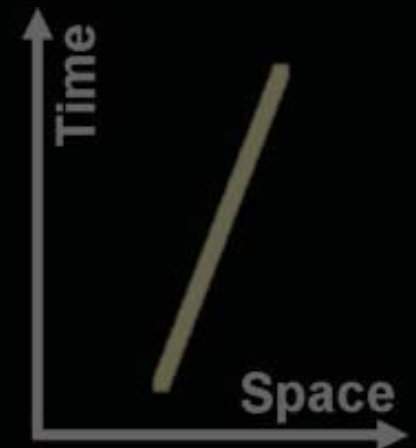


Controlling motion blur

Static- recorded image



Tracking- recorded image



Motion invariant blur



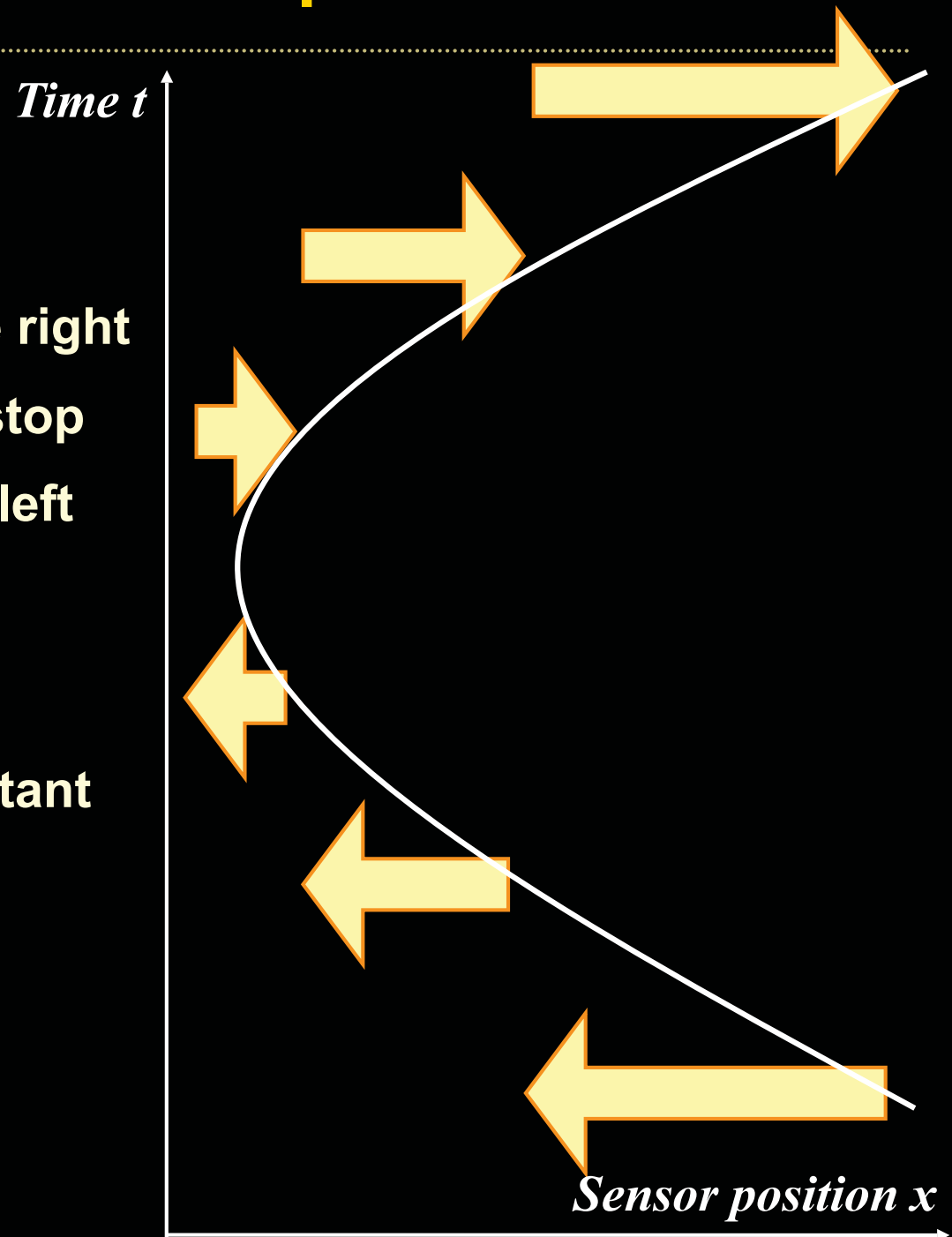
Parabolic sweep

Sensor position $x(t) = a t^2$

- Start by moving very fast to the right
- Continuously slow down until stop
- Continuously accelerate to the left

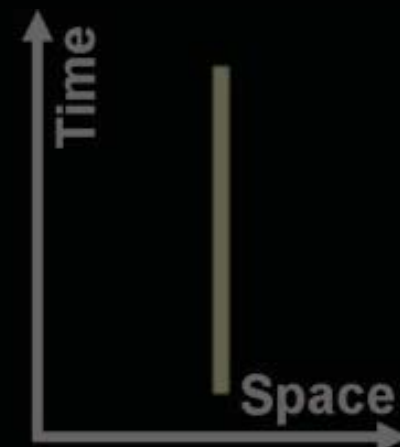
Intuition:

For any velocity, there is one instant where we track perfectly.

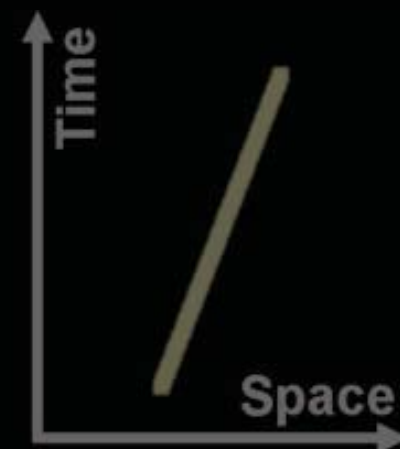


Motion invariant blur

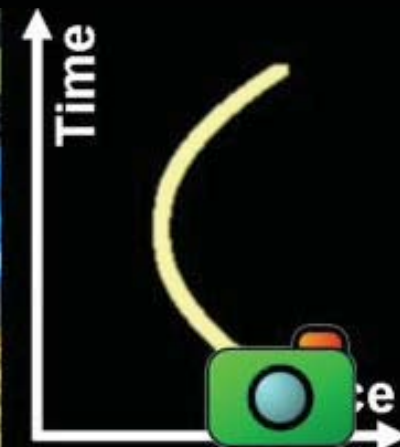
Static- recorded image



Tracking- recorded image

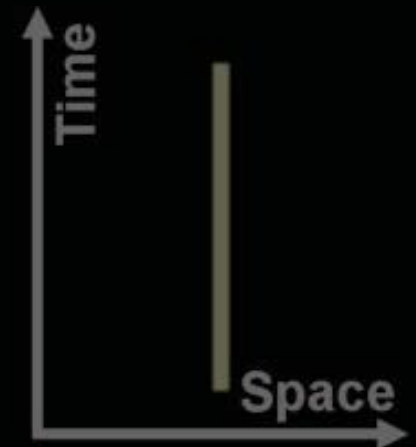


Parabolic- sensor displacement

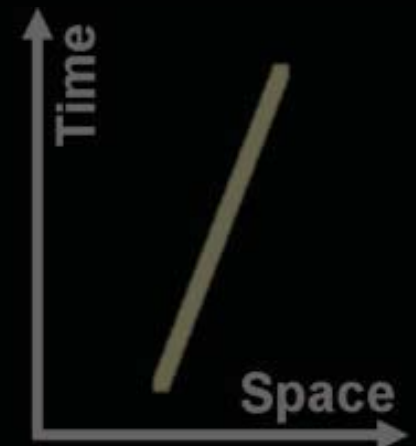


Motion invariant blur

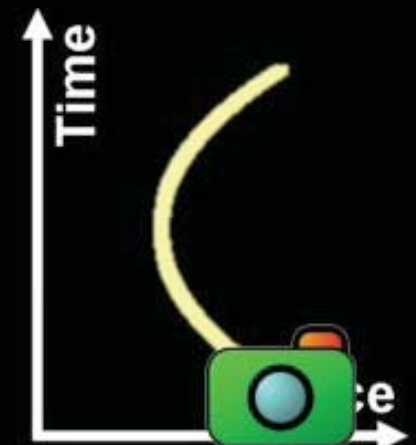
Static- recorded image



Tracking- recorded image

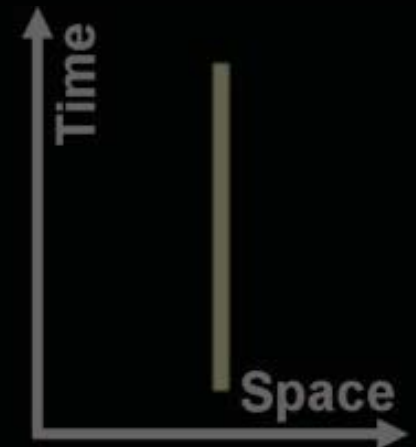


Parabolic- view from sensor

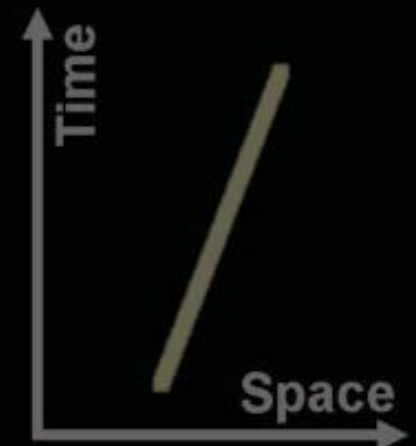


Motion invariant blur

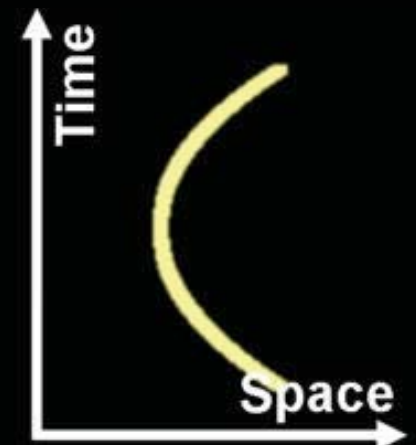
Static- recorded image

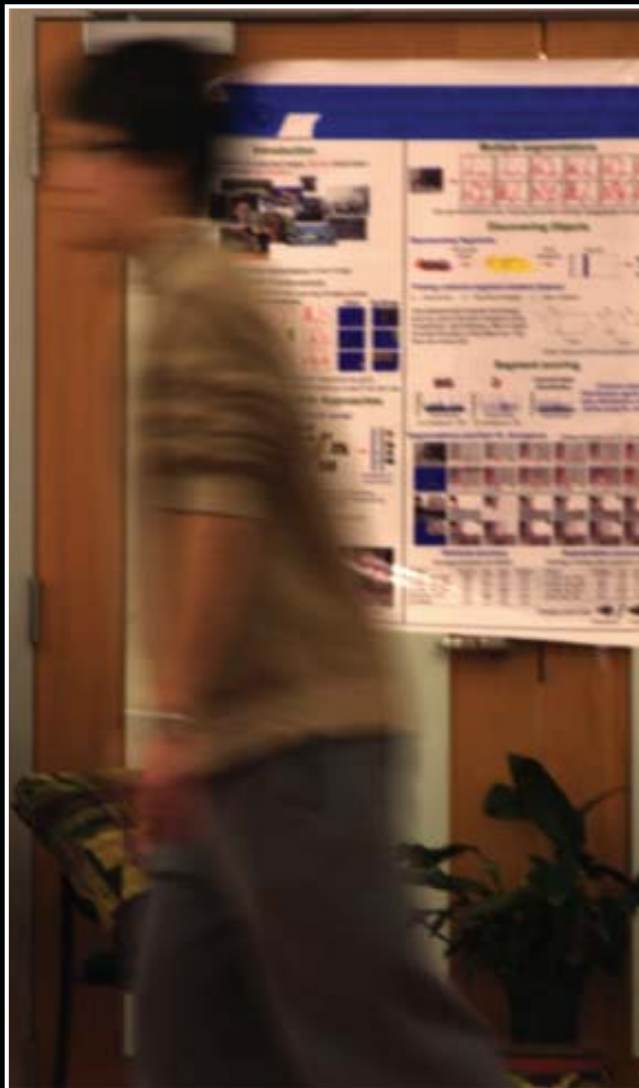


Tracking- recorded image



Parabolic- recorded image





Static camera

**Unknown and
variable blur kernels**



Our parabolic input

**Blur kernel is invariant
to velocity**



**Our output after
deblurring**

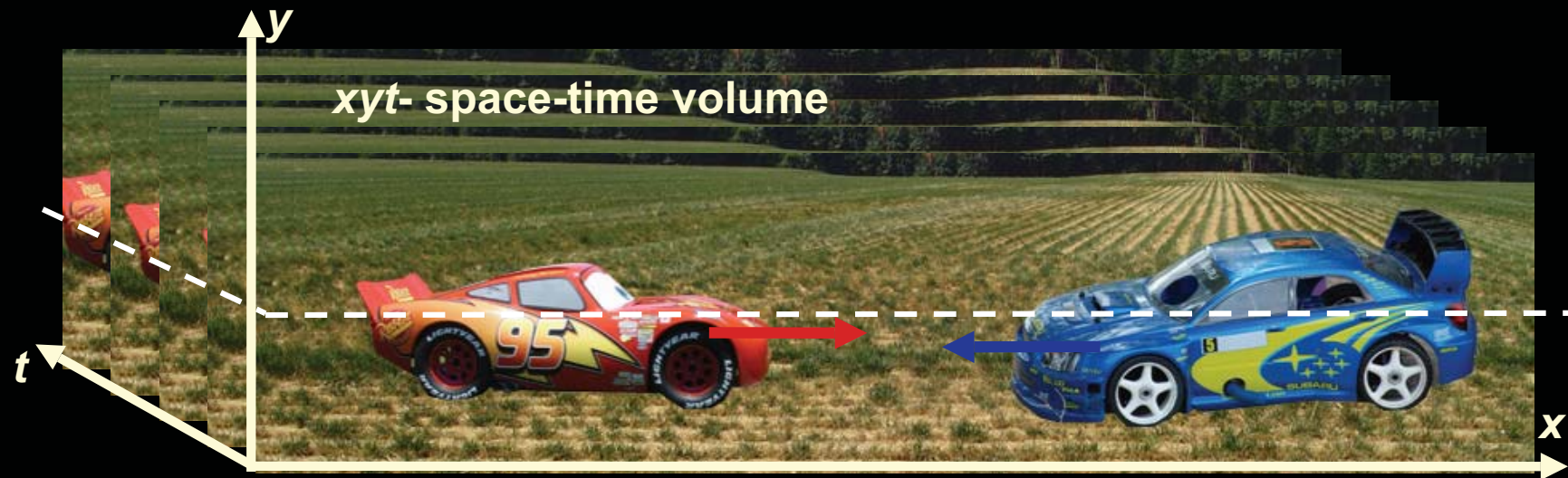
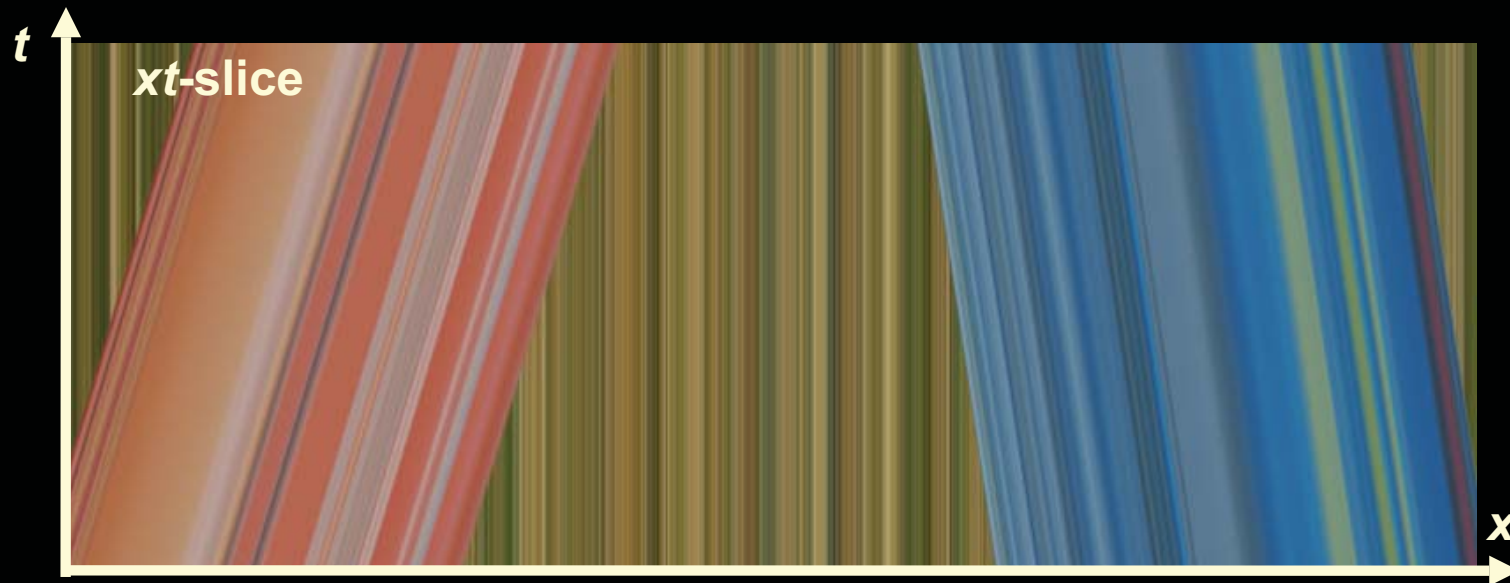
**NON-BLIND
deconvolution**

Big ideas in Comp Photo

- ◆ Multiple-exposure & multiplexing
- ◆ **Coded imaging**
- ◆ Prior information
- ◆ The raw data is high dimensional
- ◆ Active imaging

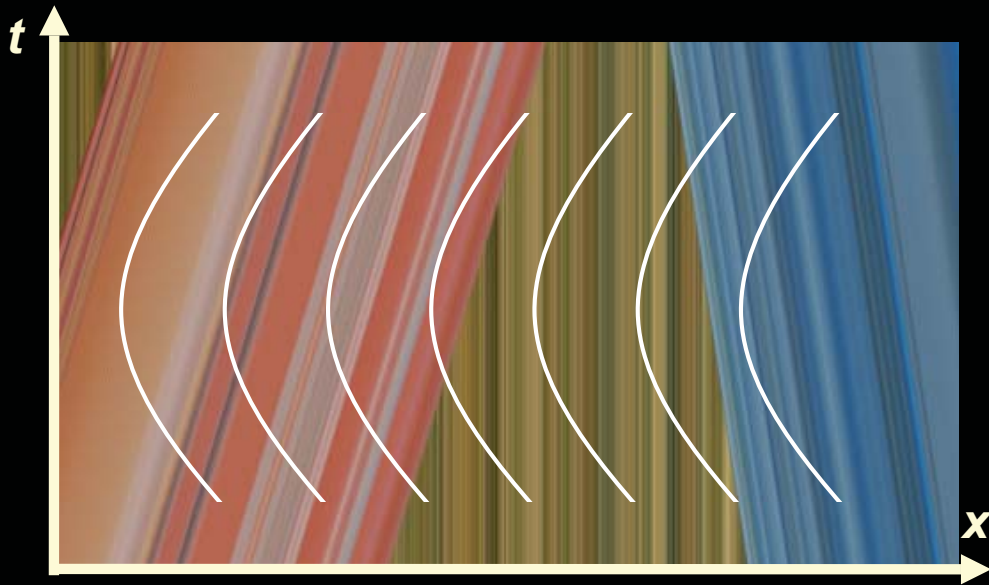


The space time volume

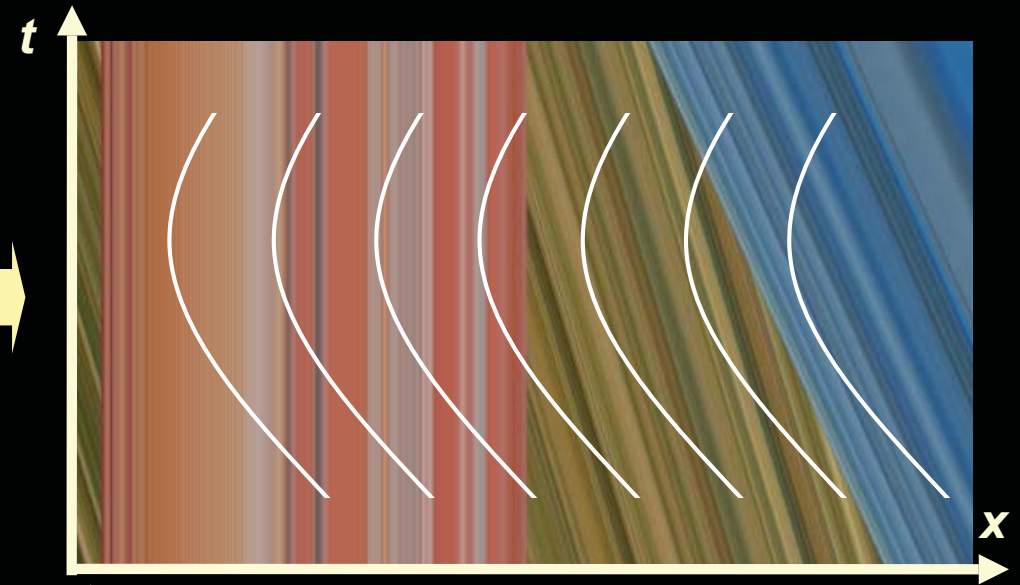


Solution: parabolic curve – shear invariant

Static object coordinates



Moving object coordinates



Shearing: $(x, t) \rightarrow (x - st, t)$

Sheared parabola

Shifted parabola

Deblurring and information loss

Assume: we could perfectly identify blur kernel

Which camera has motion blur that is easy to invert?

- Static? Flutter Shutter? Parabolic?

Prove: parabolic motion achieves near optimal information preservation



blurred input



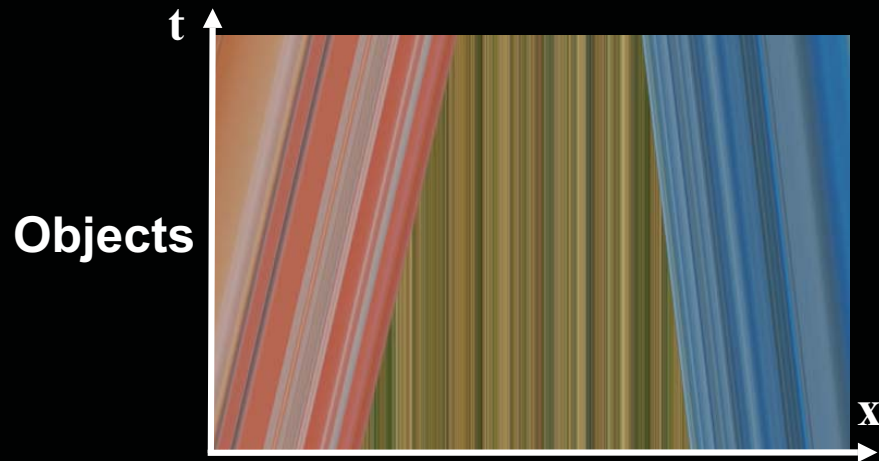
deblurred



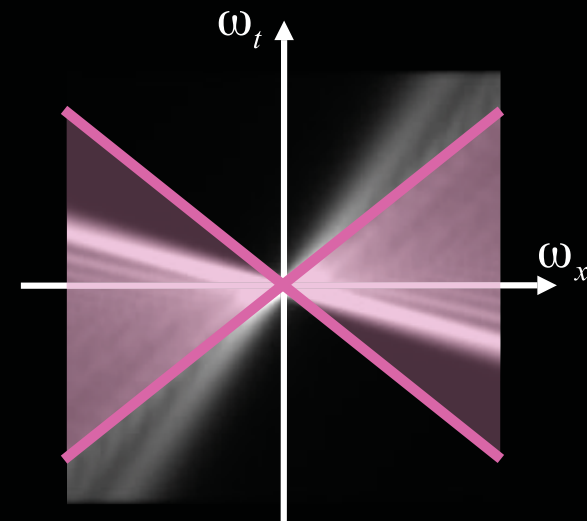
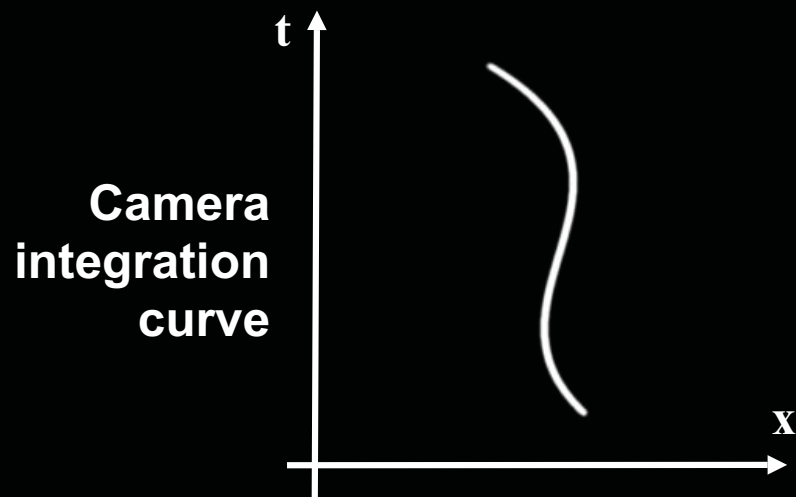
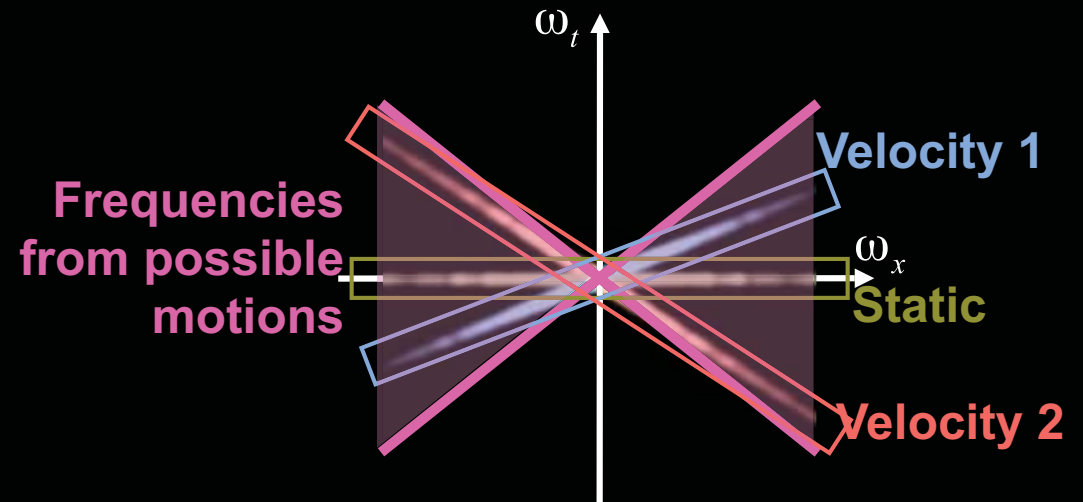
static input

Space-time Fourier domain

Primal Domain



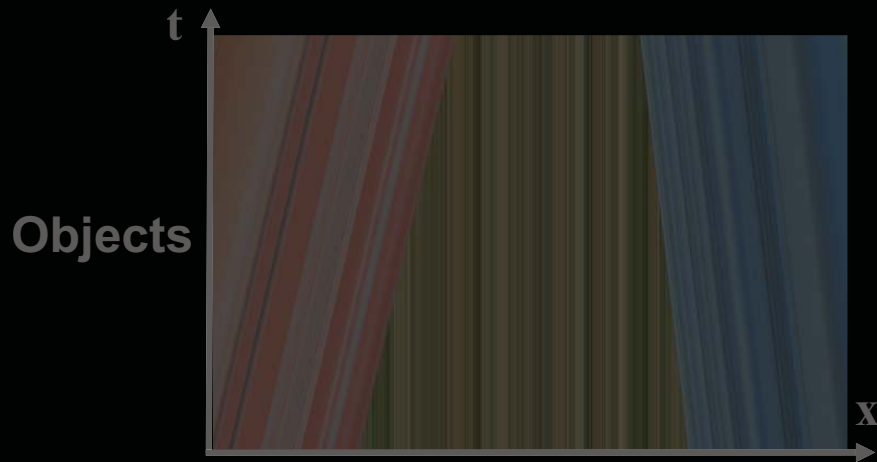
Frequency Domain



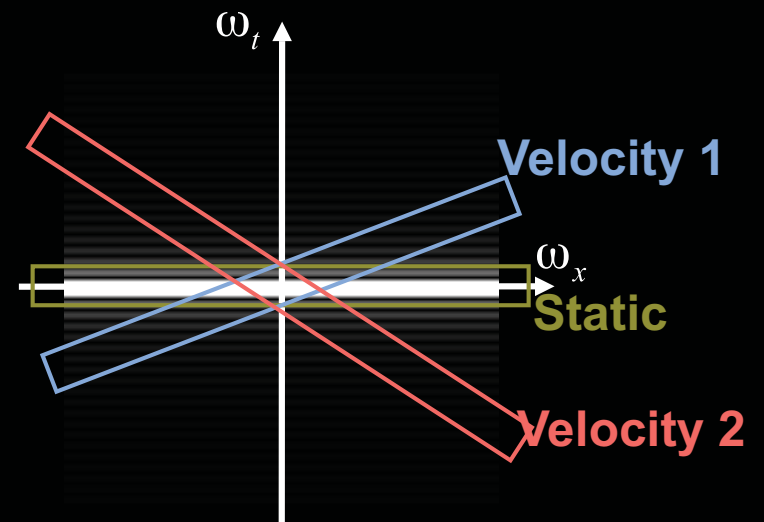
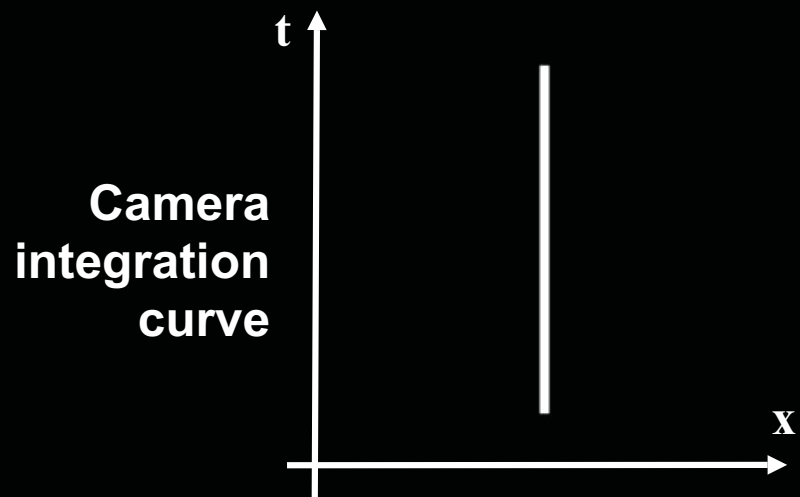
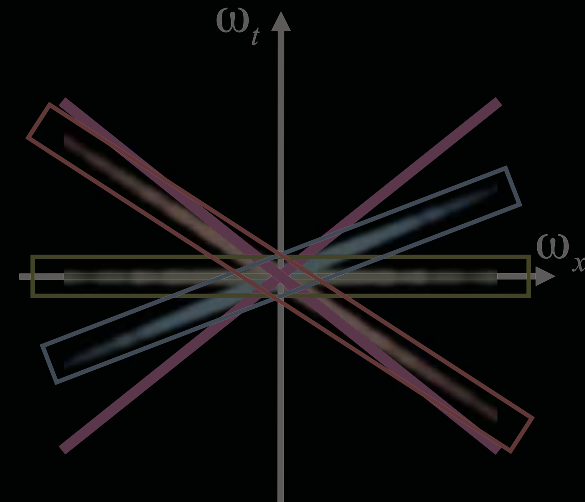
Bounded velocities range=> need to preserve a **double wedge** in the frequency domain

Static camera

Primal Domain



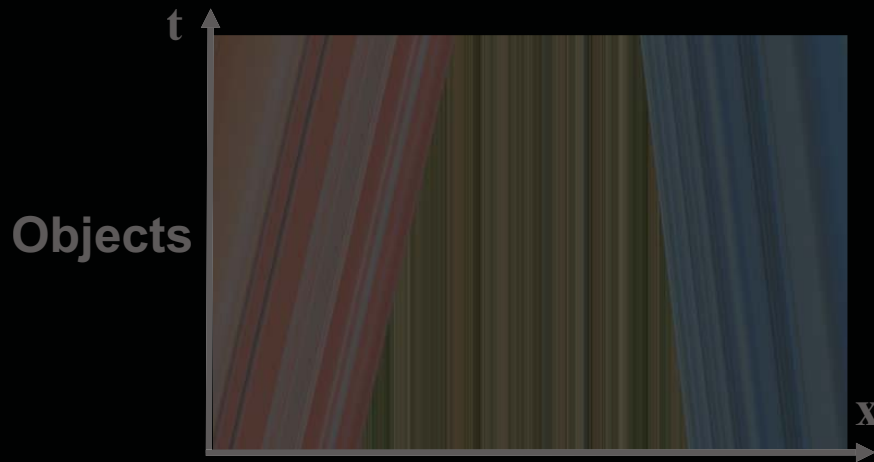
Frequency Domain



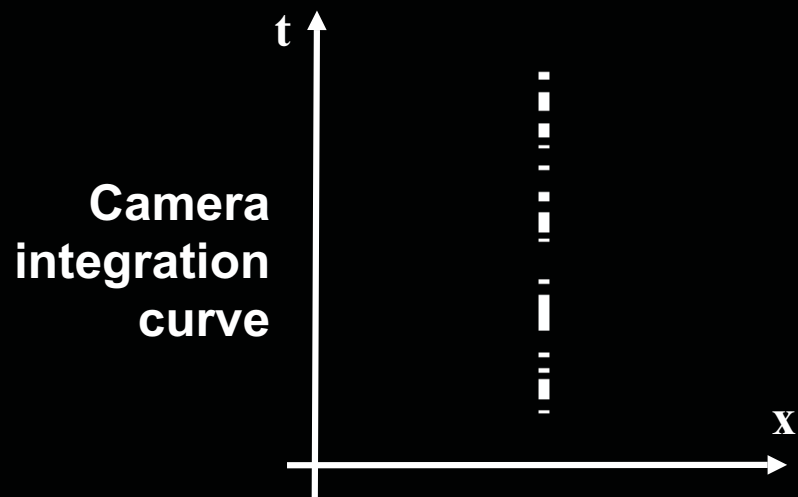
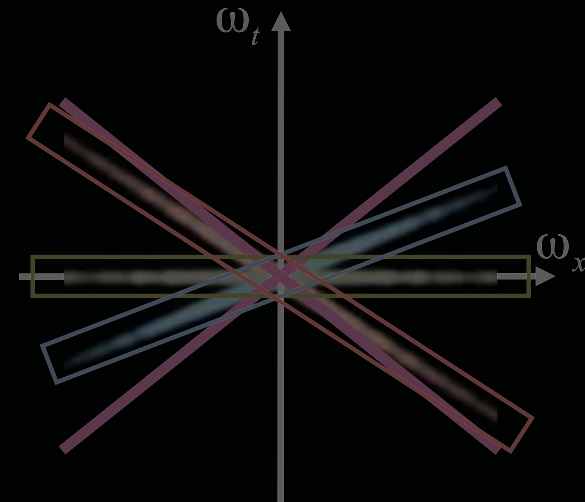
Vertical integration segment **Static object: high response**
Higher velocities: low

Flutter shutter (Raskar et al 2006)

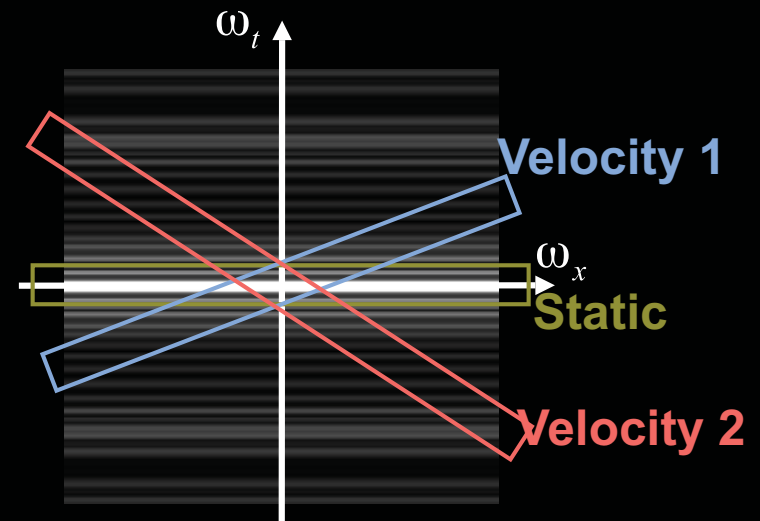
Primal Domain



Frequency Domain



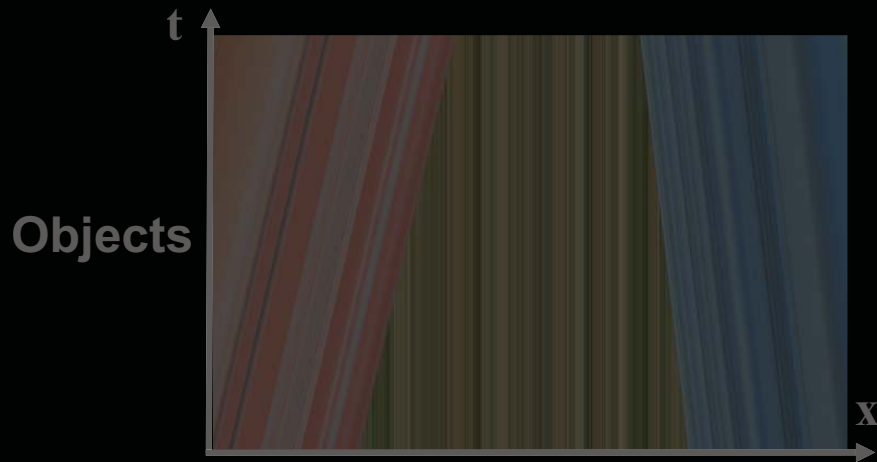
**Vertical but discontinuous
integration segment**



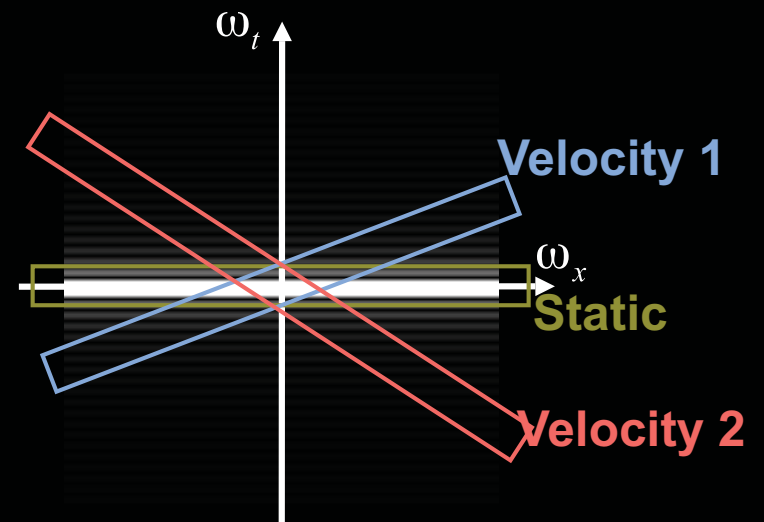
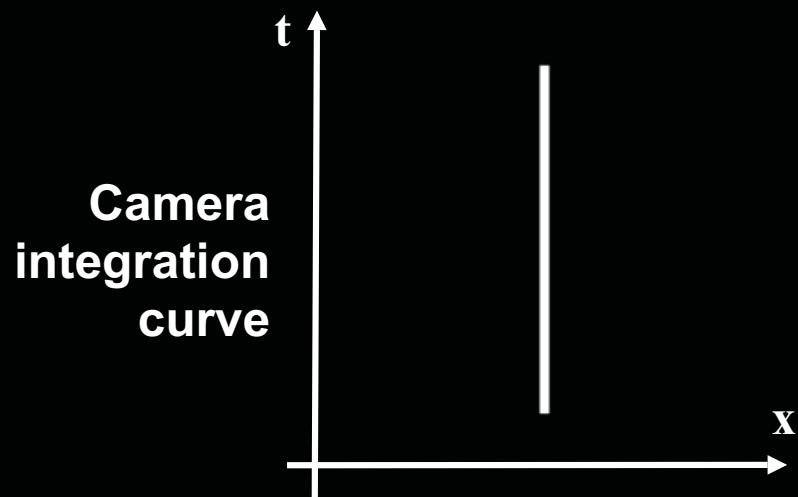
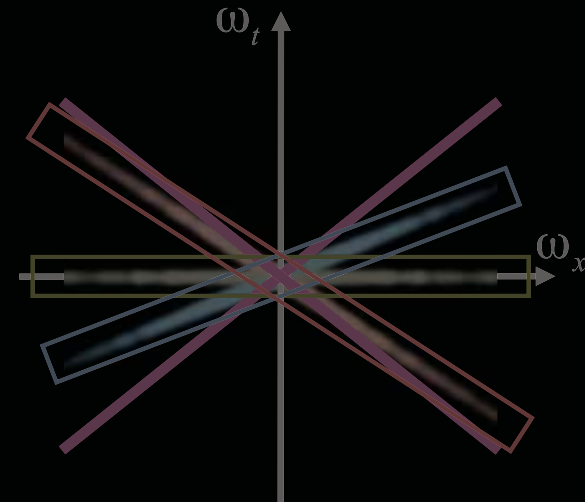
**Higher velocities:
better than static camera**

Static camera

Primal Domain



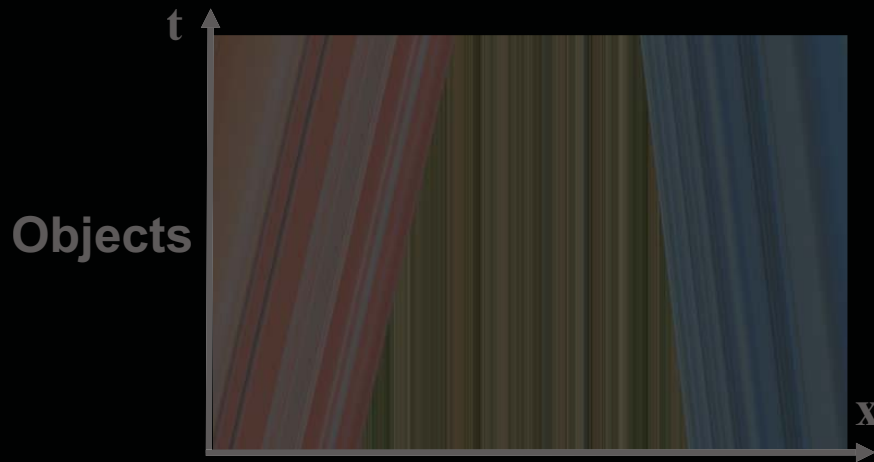
Frequency Domain



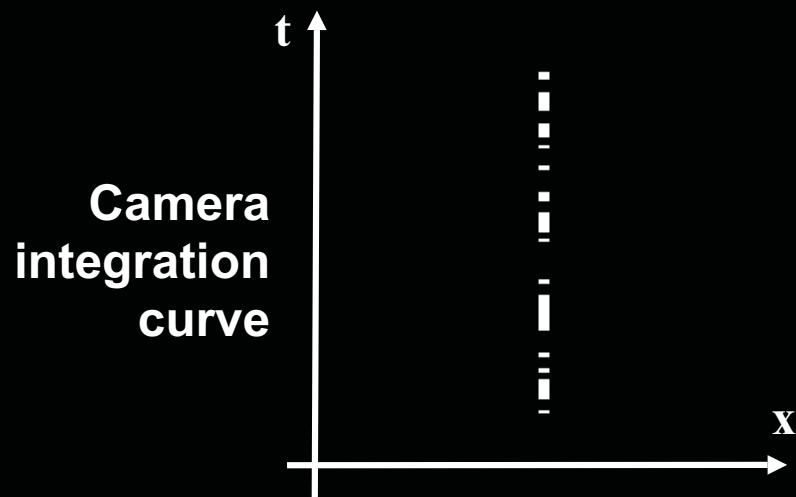
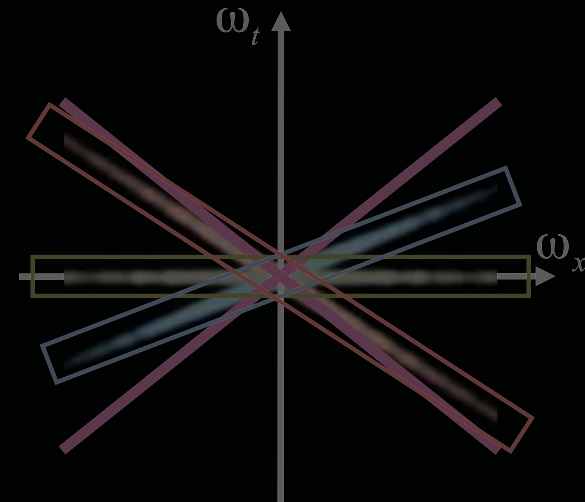
Vertical integration segment **Static object: high response**
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Flutter shutter (Raskar et al 2006)

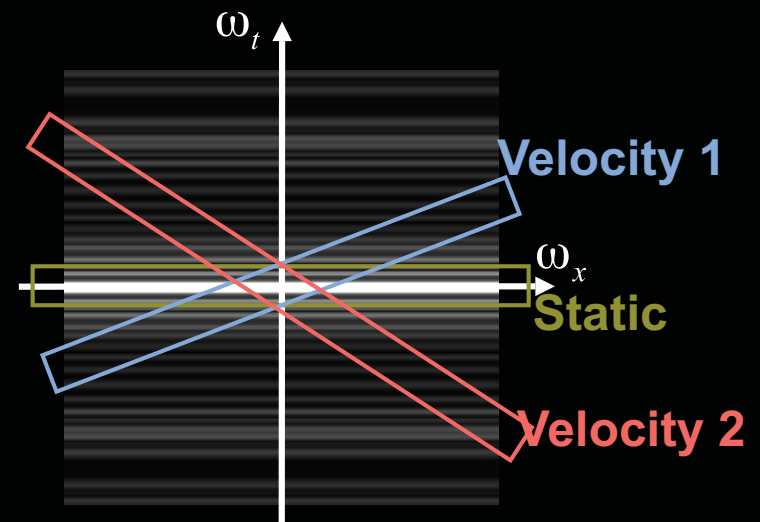
Primal Domain



Frequency Domain



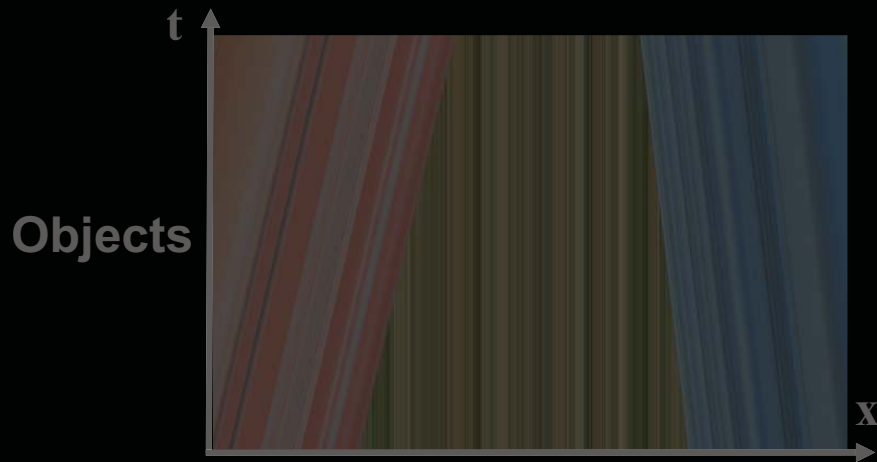
**Vertical but discontinuous
integration segment**



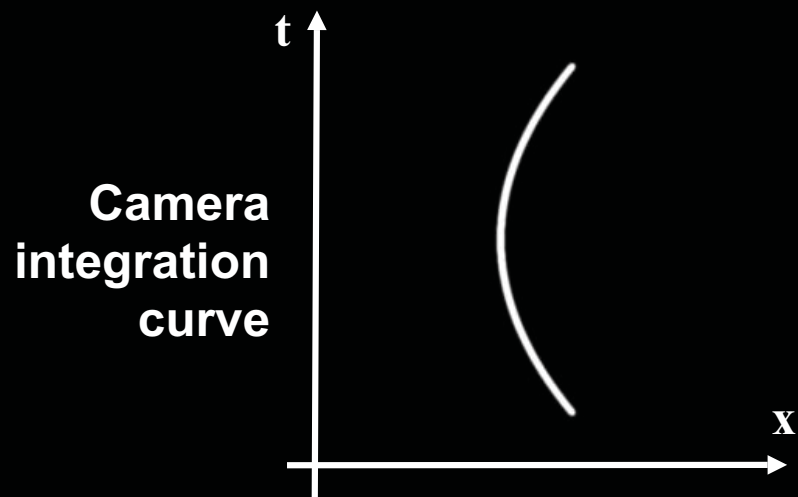
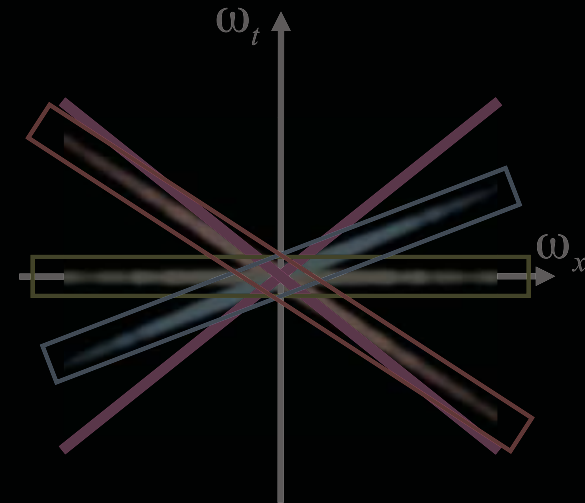
**Higher velocities:
better than static camera**

Our parabolic camera

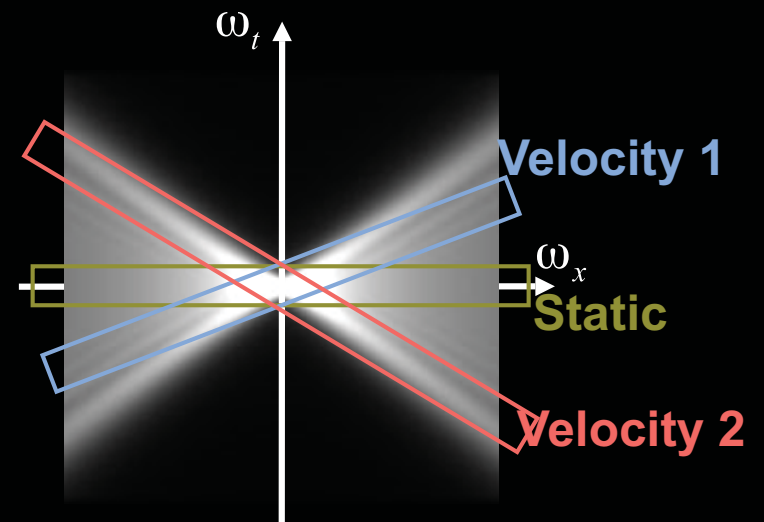
Primal Domain



Frequency Domain



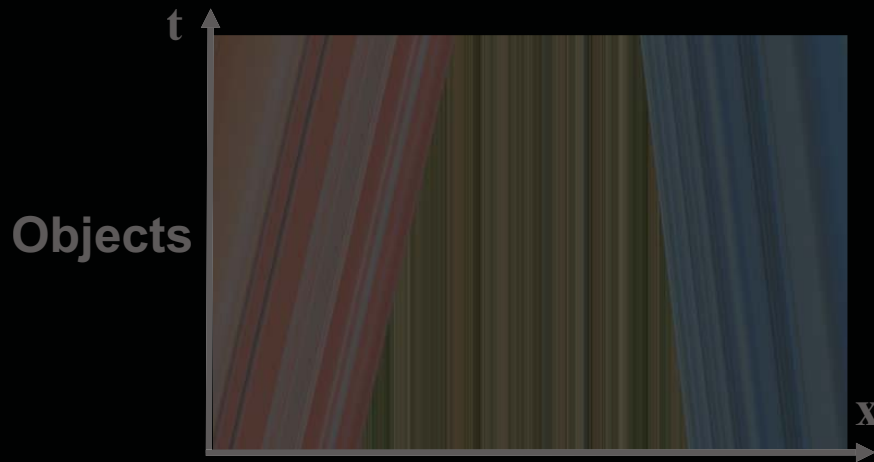
Parabola



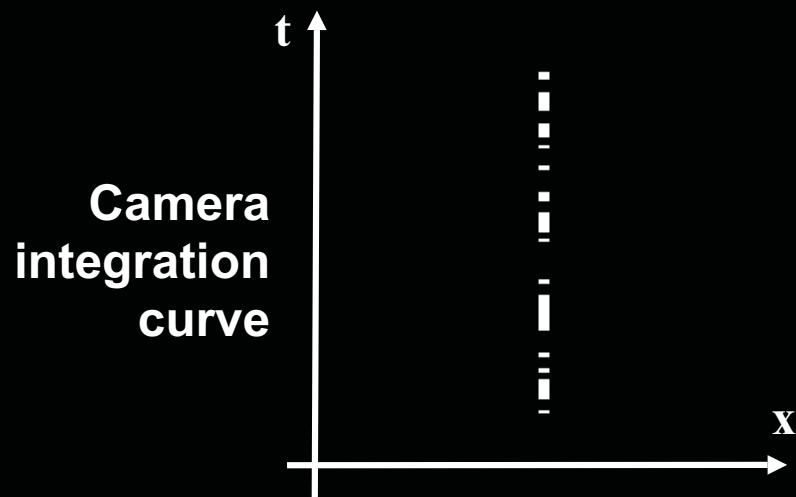
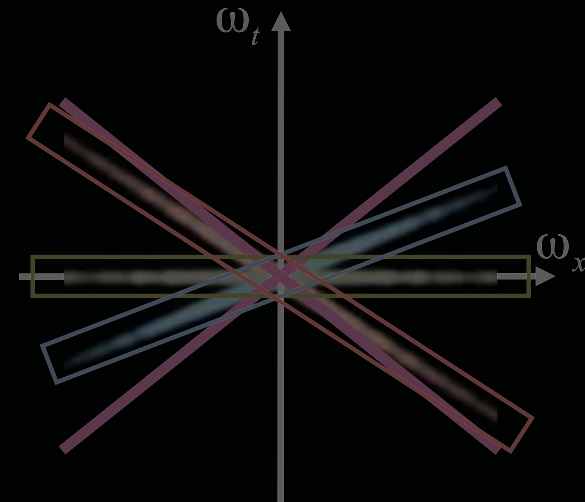
Equal high response in all range

Flutter shutter (Raskar et al 2006)

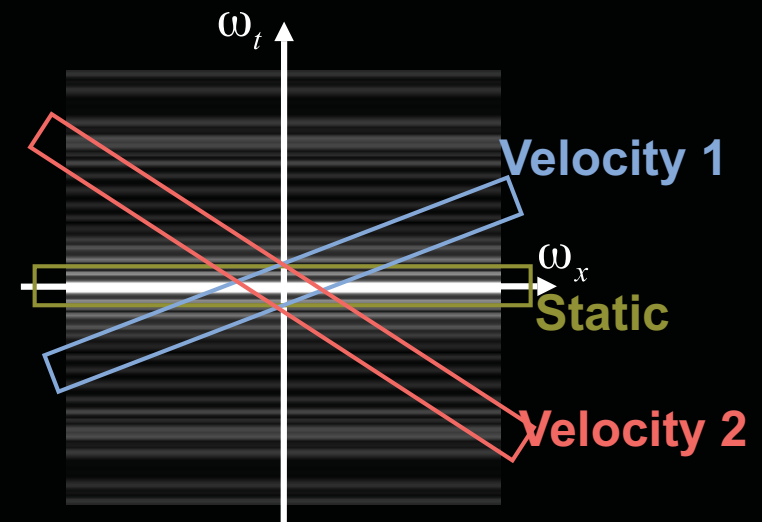
Primal Domain



Frequency Domain



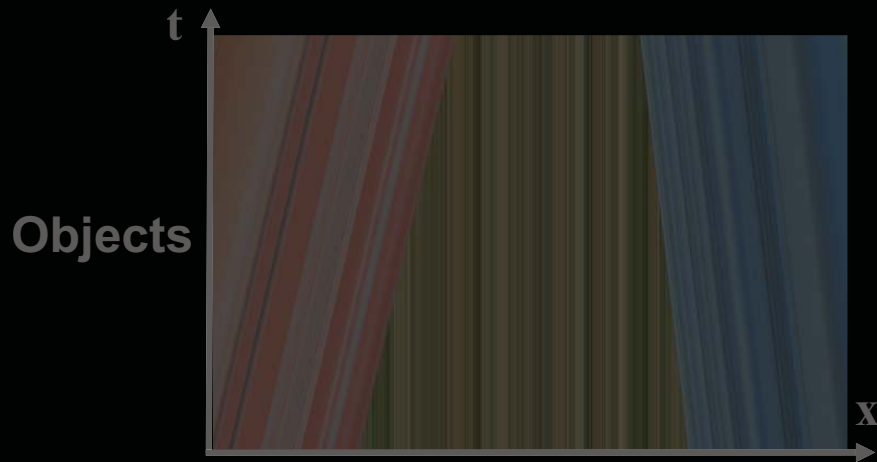
**Vertical but discontinuous
integration segment**



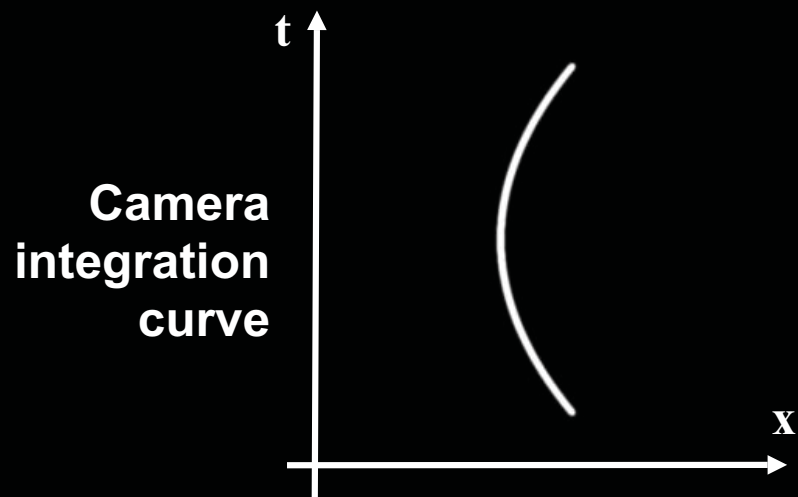
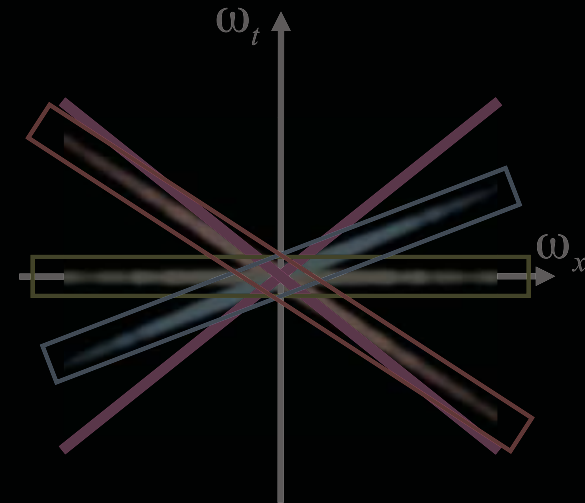
**Higher velocities:
better than static camera**

Our parabolic camera

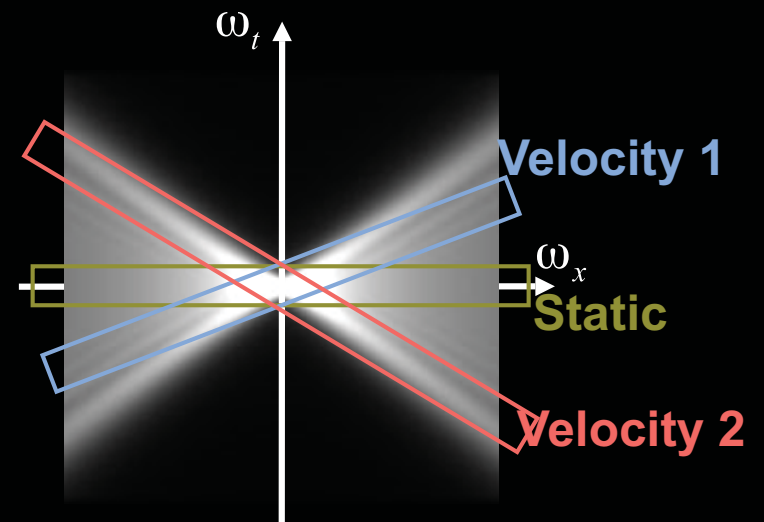
Primal Domain



Frequency Domain



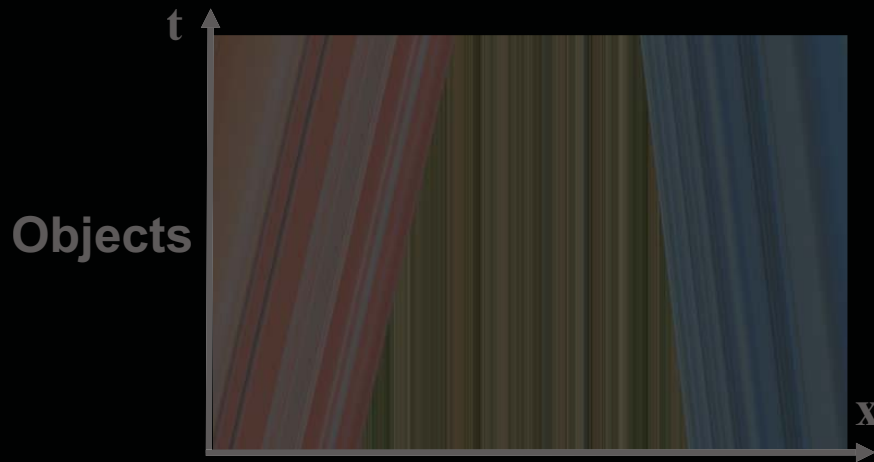
Parabola



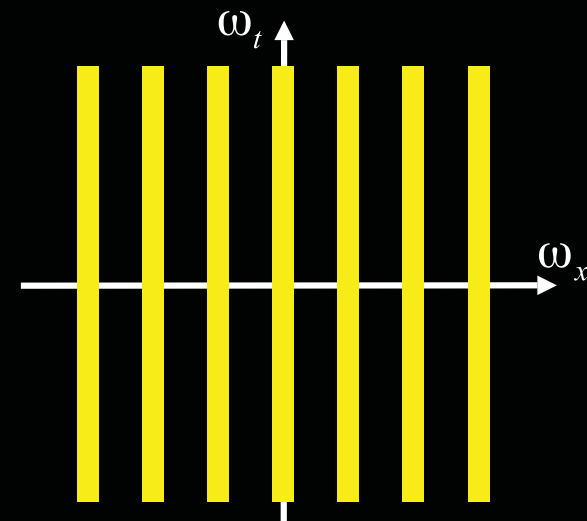
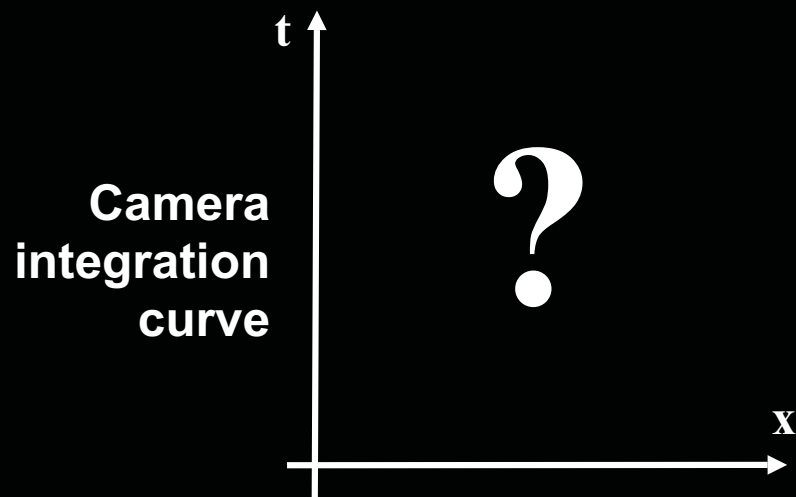
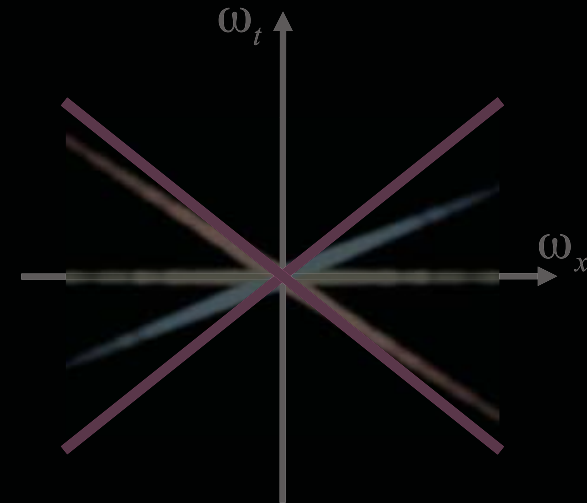
Equal high response in all range

Information budget

Primal Domain



Frequency Domain



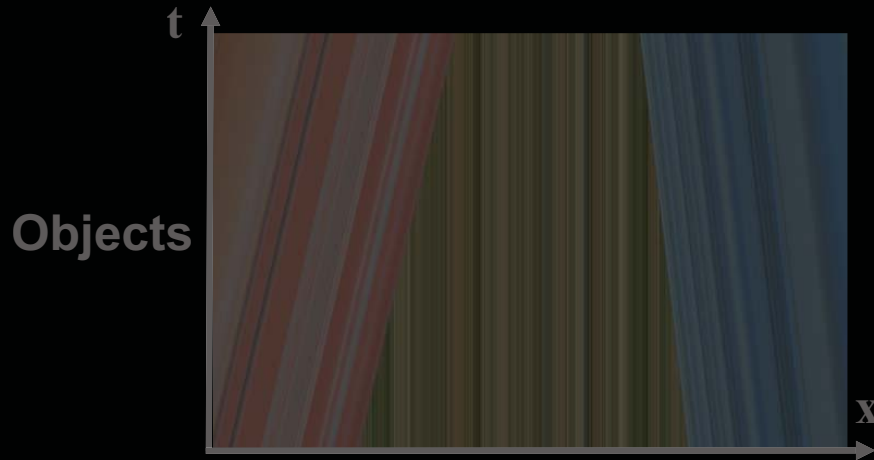
**Bounded number
of photons**



**Bounded budget per column
(norm of power spectrum)**

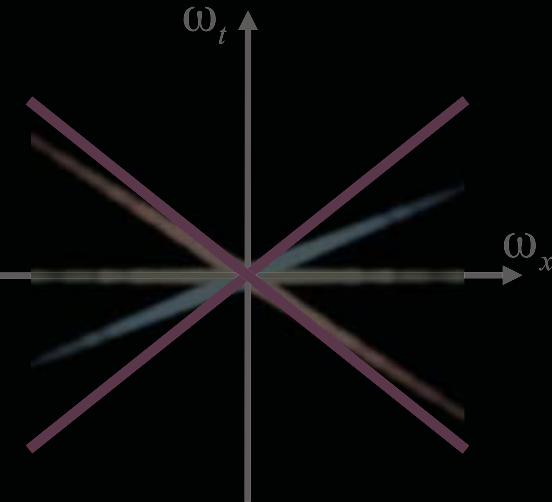
Upper bound given velocity range

Primal Domain



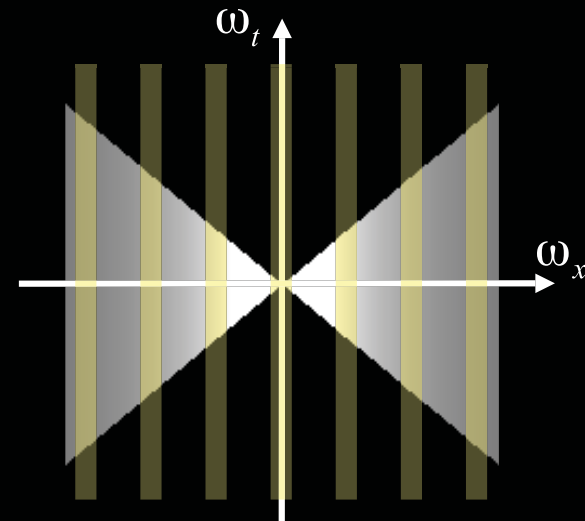
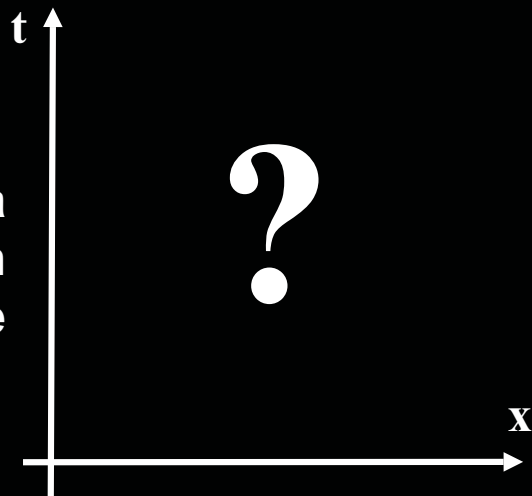
Frequency Domain

Frequencies
from possible
motions



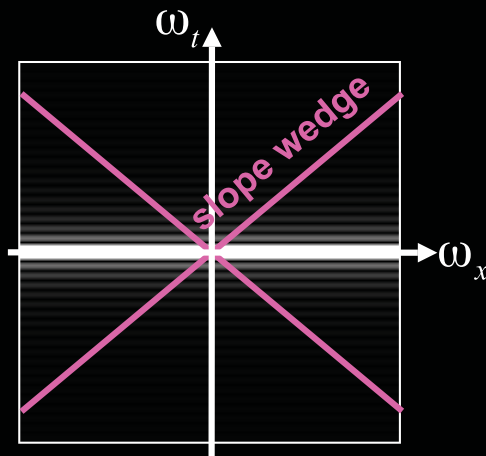
Camera
integration
curve

?

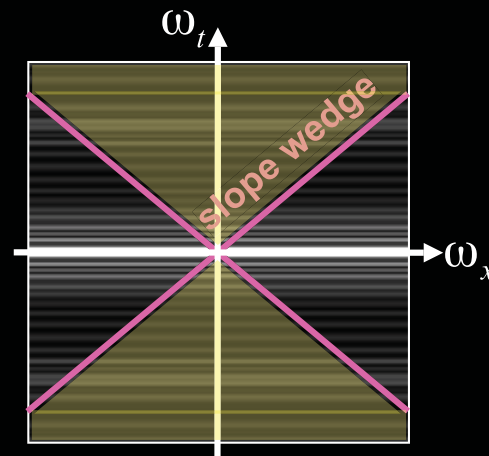


For each column, distribute budget
uniformly within wedge $|K(\omega_x, \omega_t)|^2 \leq \frac{1}{|\omega_x|}$

Cameras and information preservation



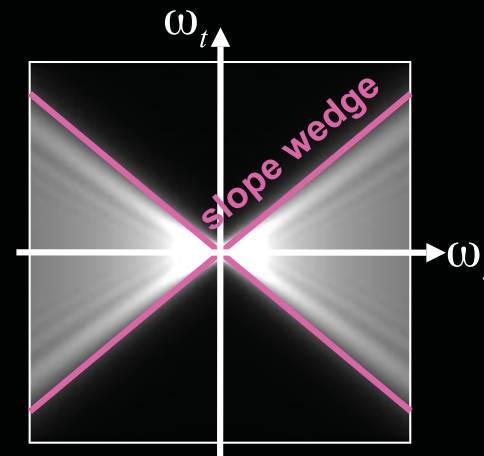
Static



Flutter shutter

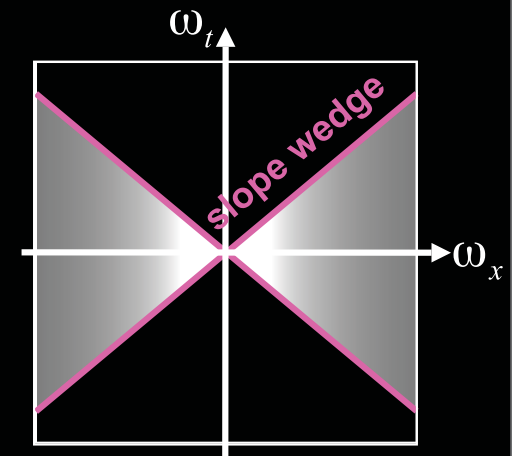
Constant horizontally
Spends frequency
“budget” outside
wedge

Handles 2D motion



Parabolic

Near optimal
“budget” usage at
all frequencies



Upper bound

Bounded
“budget” per
column ω_x

Comparing camera reconstruction

Static

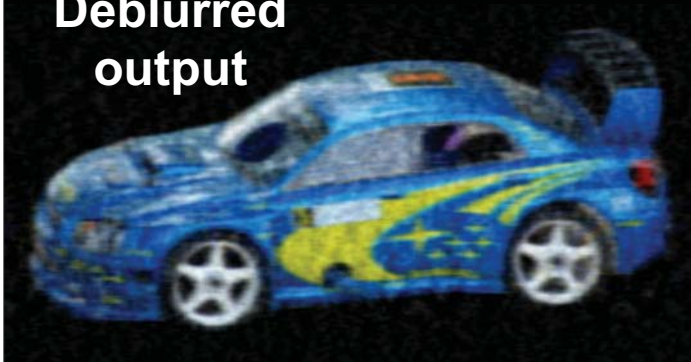
Flutter Shutter

Parabolic

**Blurred
input**



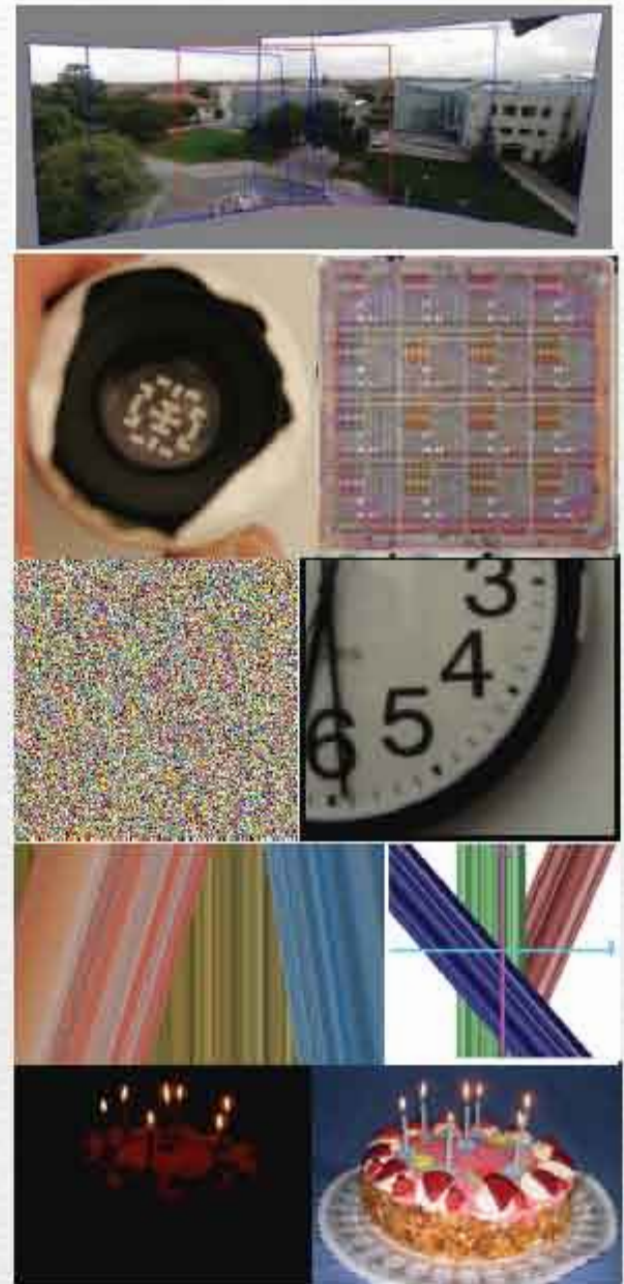
**Deblurred
output**



Note: synthetic rendering, exact PSF is known

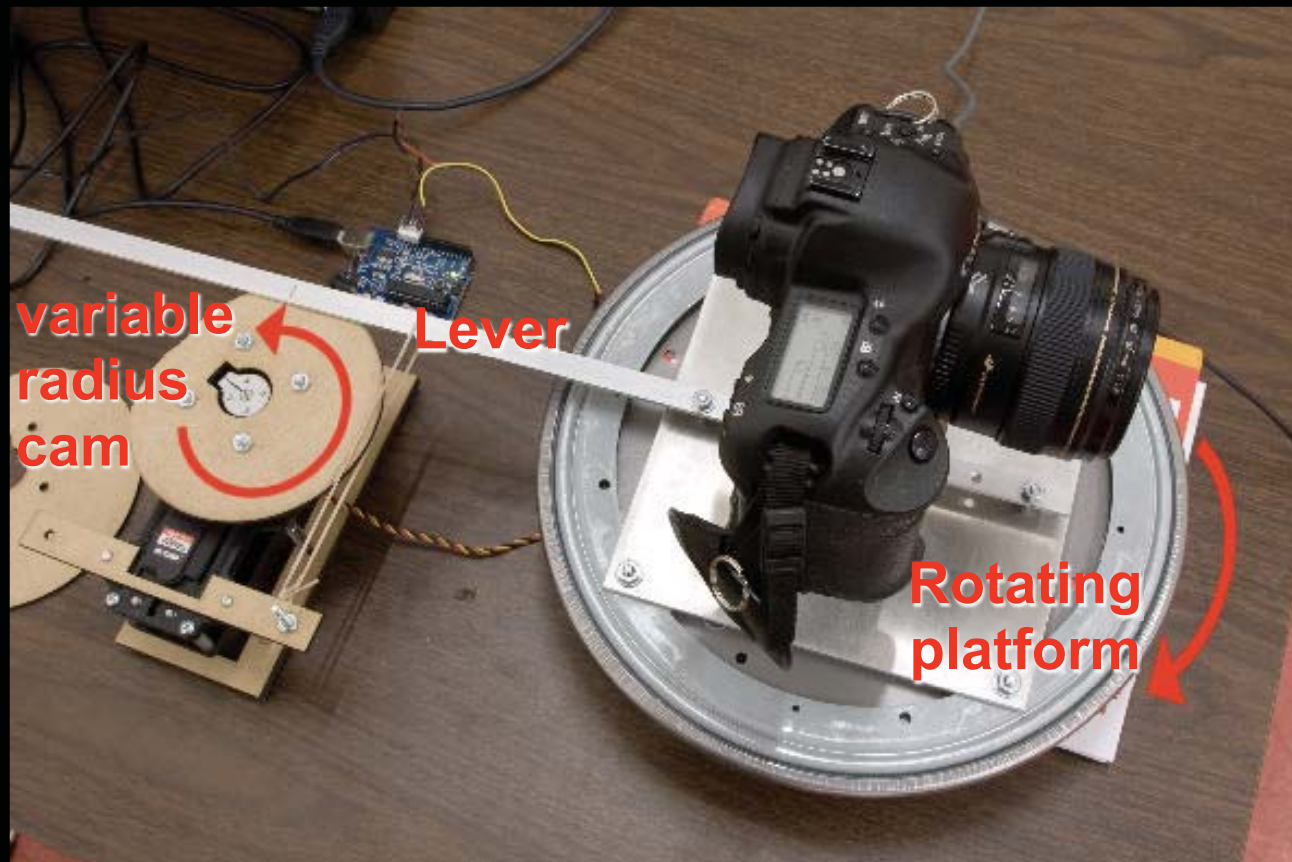
Big ideas in Comp Photo

- ◆ Multiple-exposure & multiplexing
- ◆ **Coded imaging**
- ◆ Prior information
- ◆ **The raw data is high dimensional**
- ◆ Active imaging



Hardware construction

- Ideally move sensor
(requires same hardware as existing stabilization systems)
- In prototype implementation: rotate camera



Linear rail



**Static camera input-
Unknown and variable blur**



**Our parabolic input-
is invariant to velocity**

Blur

Linear rail



Static camera input-
Unknown and variable blur



Our output after deblurring-
NON-BLIND deconvolution

Human motion– no perfect linearity



Input from a static camera



Deblurred output from our camera

Violating 1D motion assumption– forward motion

.....



Input from a static camera

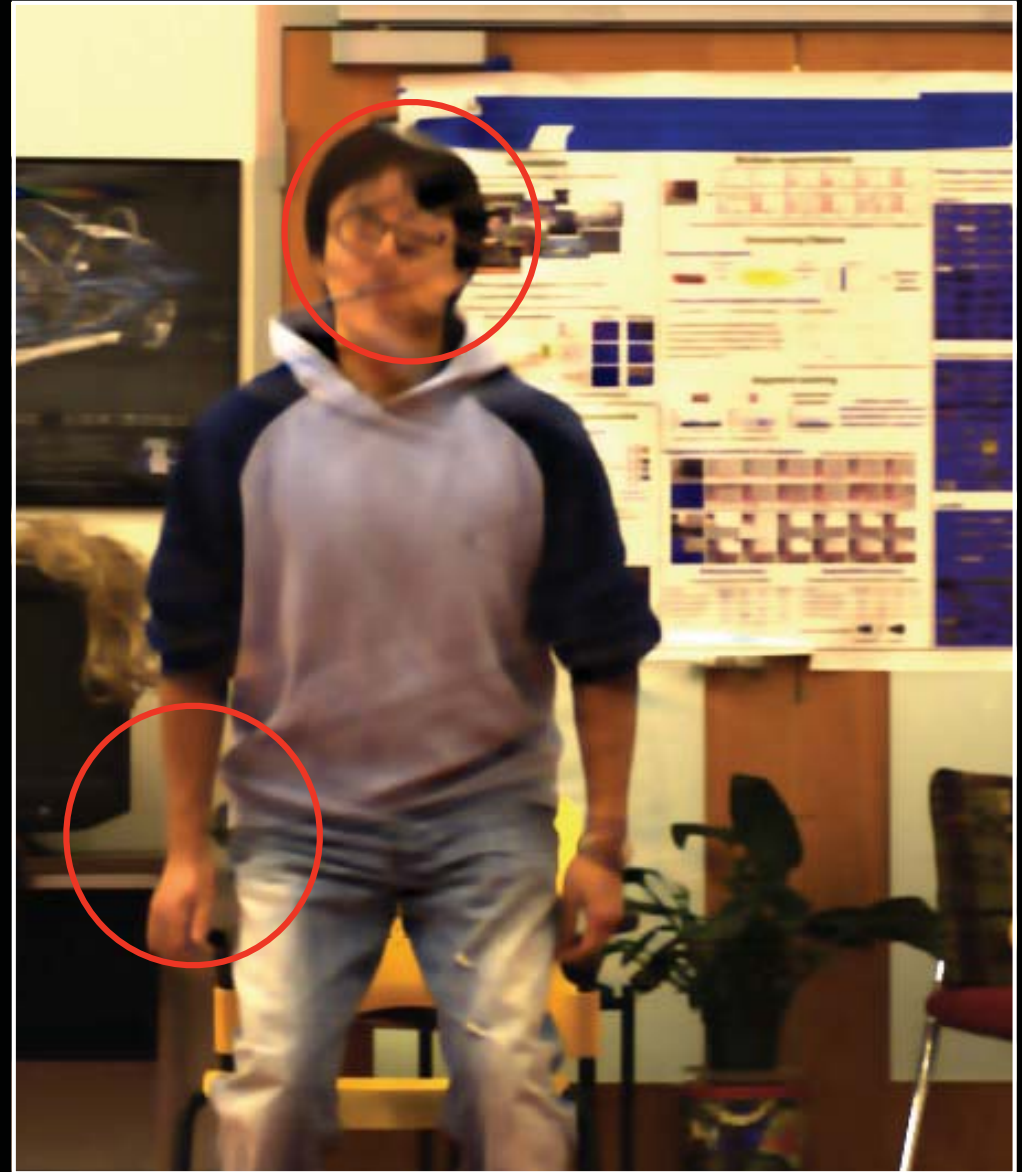


Deblurred output from our camera

Violating 1D motion assumption– stand-up motion



Input from a static camera

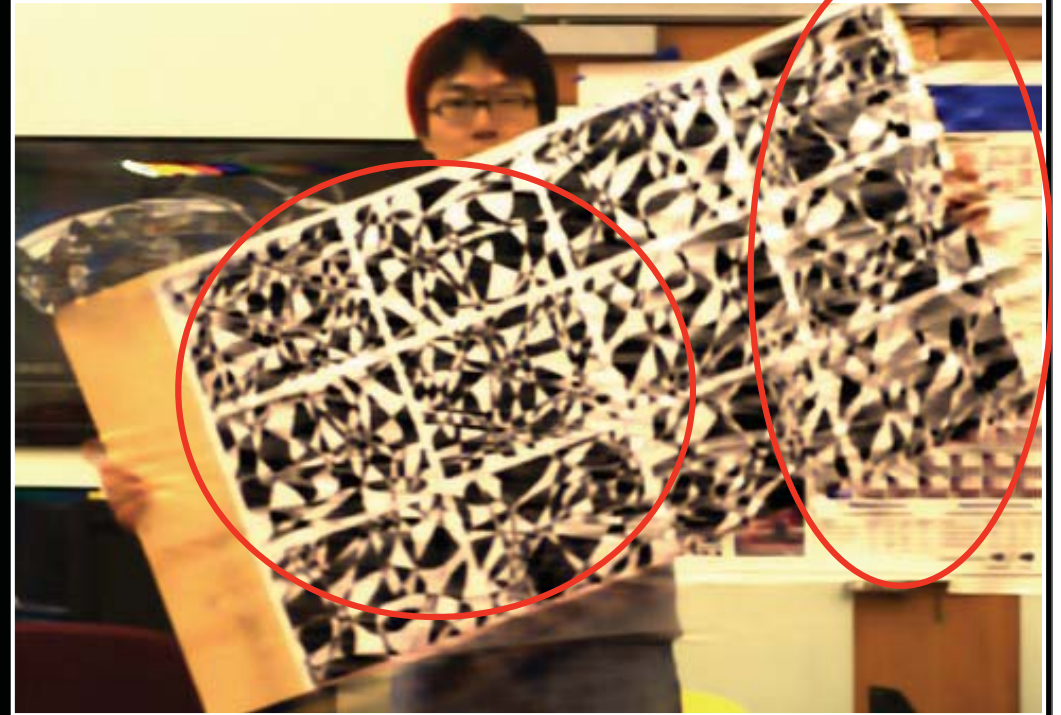


Deblurred output from our camera

Violating 1D motion assumption– rotation



Input from a static camera



Deblurred output from our camera

Parabolic curve – issues

- **Spatial shift- but does not affect visual quality in deconvolution**
- **Parabola tail clipping: not exactly the same blur**
- **Motion boundaries break the convolution model**
- **Assumes: Object motion horizontal**

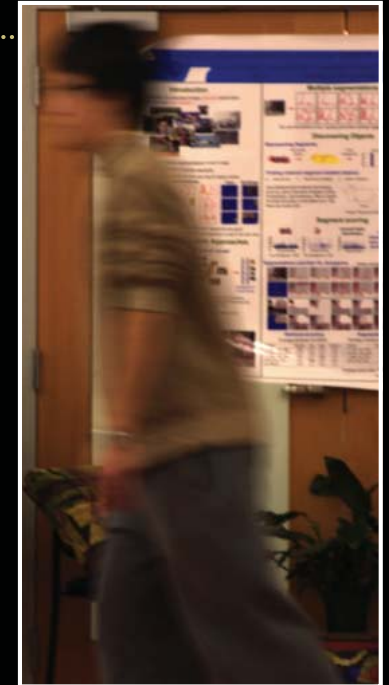
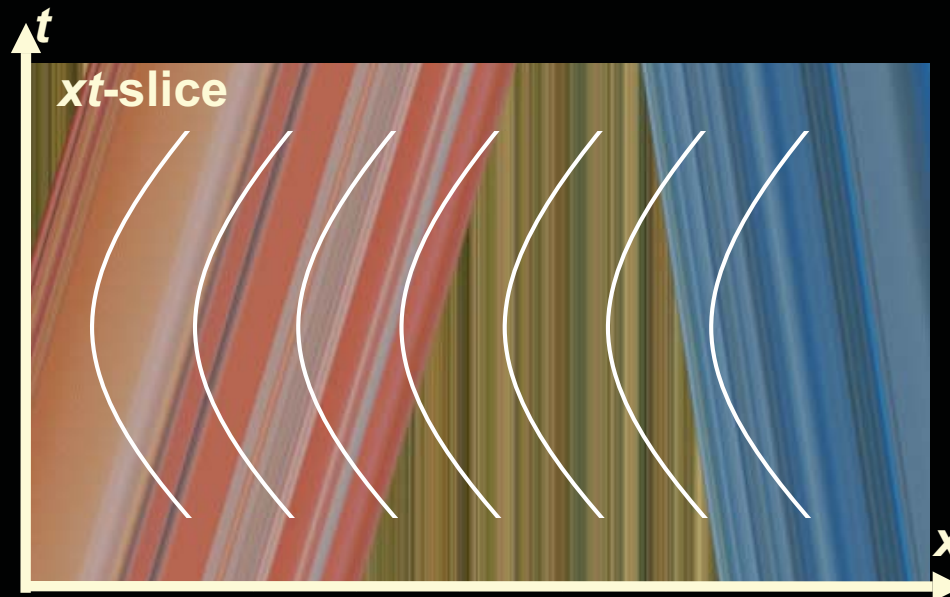
Object motion linear up to 1st order approximation

Conclusions

- Camera moved during exposure, parabolic displacement
- Blur invariant to motion:
 - Same over all image (no need to segment)
 - Known in advance (no kernel identification)
- Easy to invert (near optimal frequency response)
- For 1D motion
 - Somewhat robust to 1D motion violation
 - Future work: 2D extensions

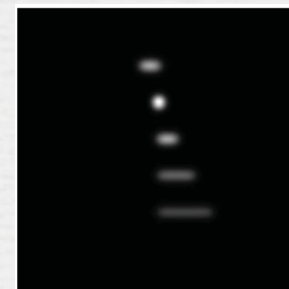
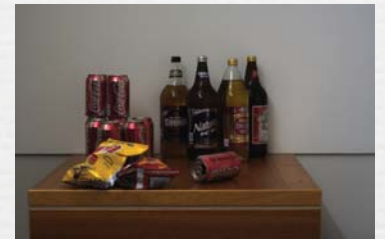
Acknowledgments:

NSF CAREER award 0447561
Royal Dutch/Shell Group NGA
NEGI-1582-04-0004
Office of Naval Research MURI
MSR New Faculty Fellowship
Sloan Fellowship

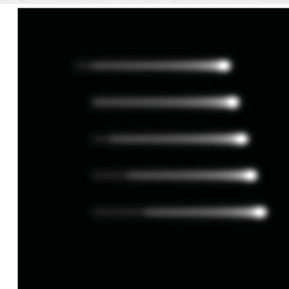


Summary

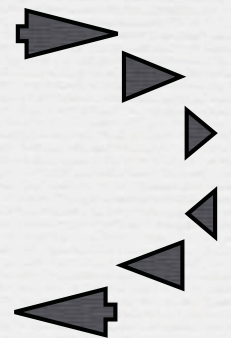
- ◆ Natural image prior
- ◆ Coded aperture : make kernel easier to identify
 - benefit:
large depth of field + depth
- ◆ Motion-invariant photography
 - For 1D motion, blur invariant to velocity



(c) Static camera



(d) Parabolic camera



Big ideas in Comp Photo

- ♦ Goals:
 - Beat physics, better image quality/quantity
 - More data (depth, etc.)
 - New visual media
 - Seeing the unseen
- ♦ Multiple-exposure imaging & multiplexing
- ♦ Coded imaging
- ♦ Prior information
- ♦ Edges matter
- ♦ The raw data is high dimensional
- ♦ Active imaging

Challenges

- ♦ Theory, frameworks, comparisons, optimality
- ♦ Diffraction, wave optics
- ♦ Putting it all together
(engineering, system, applications)
- ♦ Better priors
 - Kernel identification
 - High-quality inversion
- ♦ Video
- ♦ Real-time enhancement (microscope)
- ♦ Applied visual perception
- ♦ Intrinsic images
- ♦ Matting
- ♦ Scene and object recognition
- ♦ 3D reconstruction

Understanding camera trade-offs through a Bayesian analysis of light field projections

Anat Levin¹, Bill Freeman^{1,2}, Fredo Durand¹

Computer Science and Artificial Intelligence Lab (CSAIL),

¹Massachusetts Institute of Technology

and ²Adobe Systems

Cameras, old and new

Traditional camera: Lens forms final 2D image



Computational camera: Recorded data is not the final output.

- Visual array estimated from sensor measurements.
- Extra design degree of freedom.
Beyond 2D images--acquisition of light field or depth.
Post-exposure re-synthesis of image.



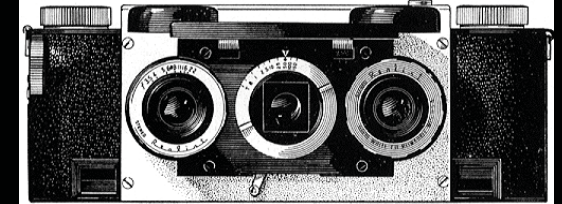
An explosion of cameras

- Best way to capture image and depth: Stereo? Plenoptic camera? Coded aperture? or...?
- What aspects of these cameras contribute to their performance?
- Can we design new cameras with improved reconstruction performance?

Conventional single-lens cameras



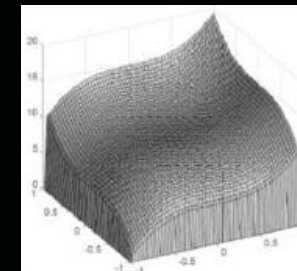
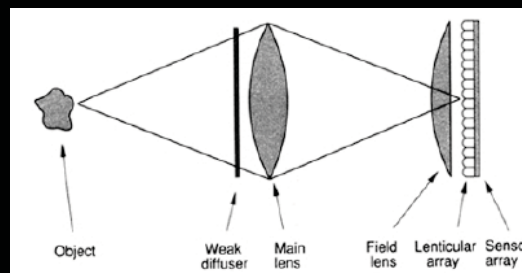
Stereo and trinocular cameras



Plenoptic cameras



Coded aperture

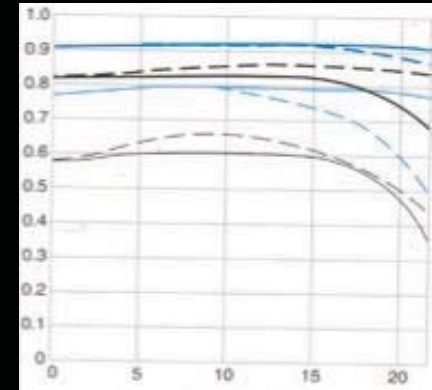


Wavefront coding

Camera evaluation, old and new

Traditional optics evaluation:

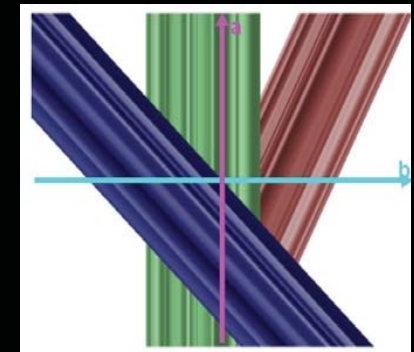
2D image sharpness (eg, Modulation Transfer Function)



contrast vs. spatial frequency

Our modern camera evaluation:

How well does the recorded data allow us to estimate the visual world - the lightfield?



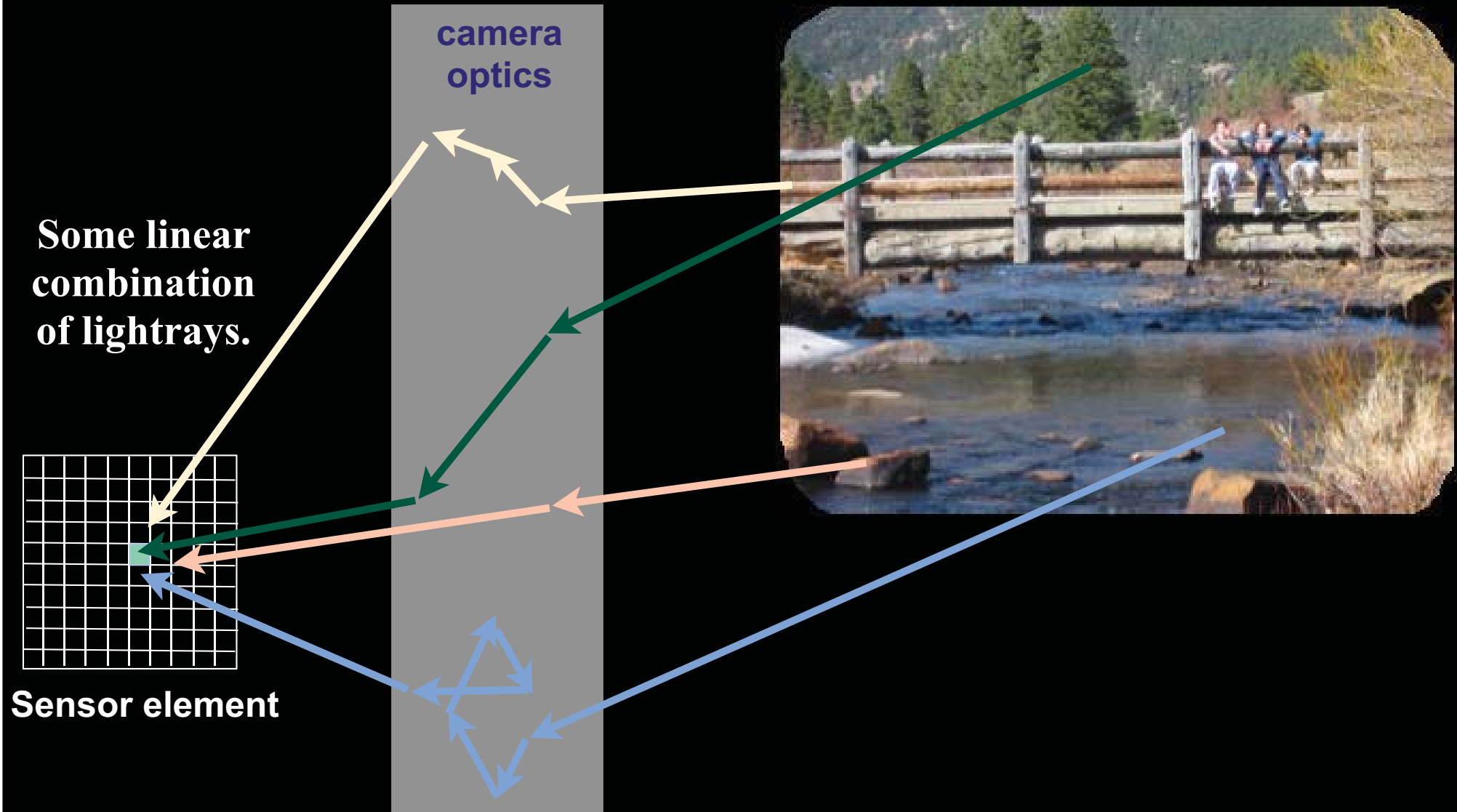
lightfield reconstruction

Computational photography camera evaluation: an estimation problem

- **Characteristics of the signal to be estimated.**
- **Projection functions of various cameras.**
- **Bayesian lightfield analysis**
 - **Reconstructing the lightfield from camera data.**
 - **Comparing performance tradeoffs of different cameras.**

so let's talk about lightfields and cameras

What does a camera sensor element record?



Sensor element data



The diagram illustrates the relationship between sensor data, camera projection, lightfield, and noise. It features a horizontal gray bar at the top and a vertical gray bar on the right. The equation $y_i = T_i x + n_i$ is centered, with y_i on the left, T_i in the middle, x on the right, and n_i on the far right. Below y_i is the word "datum". Below T_i is the text "The camera" and "4D->2D linear projection". Below x is the text "The lightfield (4D)". Below n_i is the word "noise".

$$y_i = T_i x + n_i$$

datum

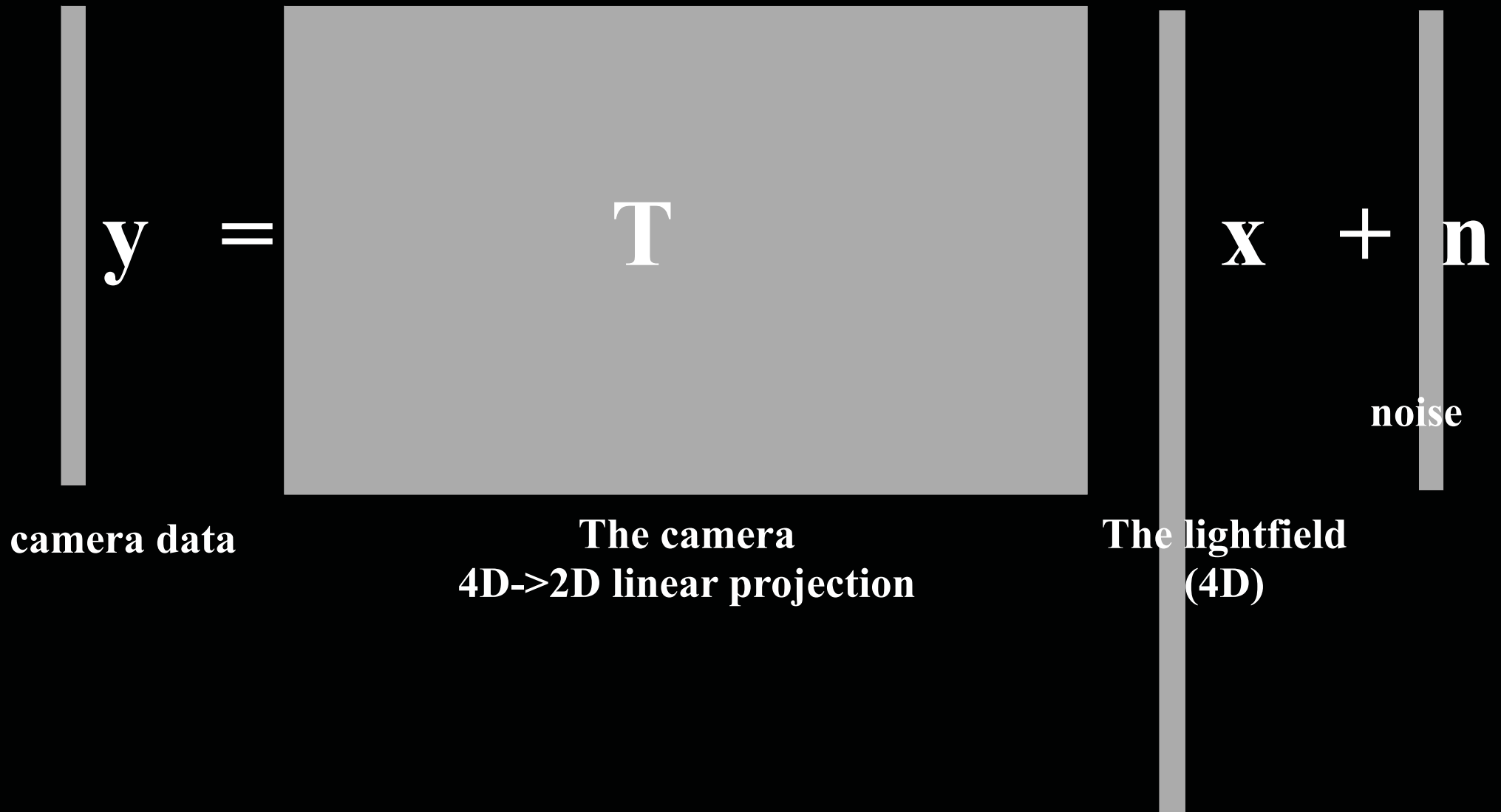
The camera
4D->2D linear projection

The lightfield
(4D)

noise

What is a camera?

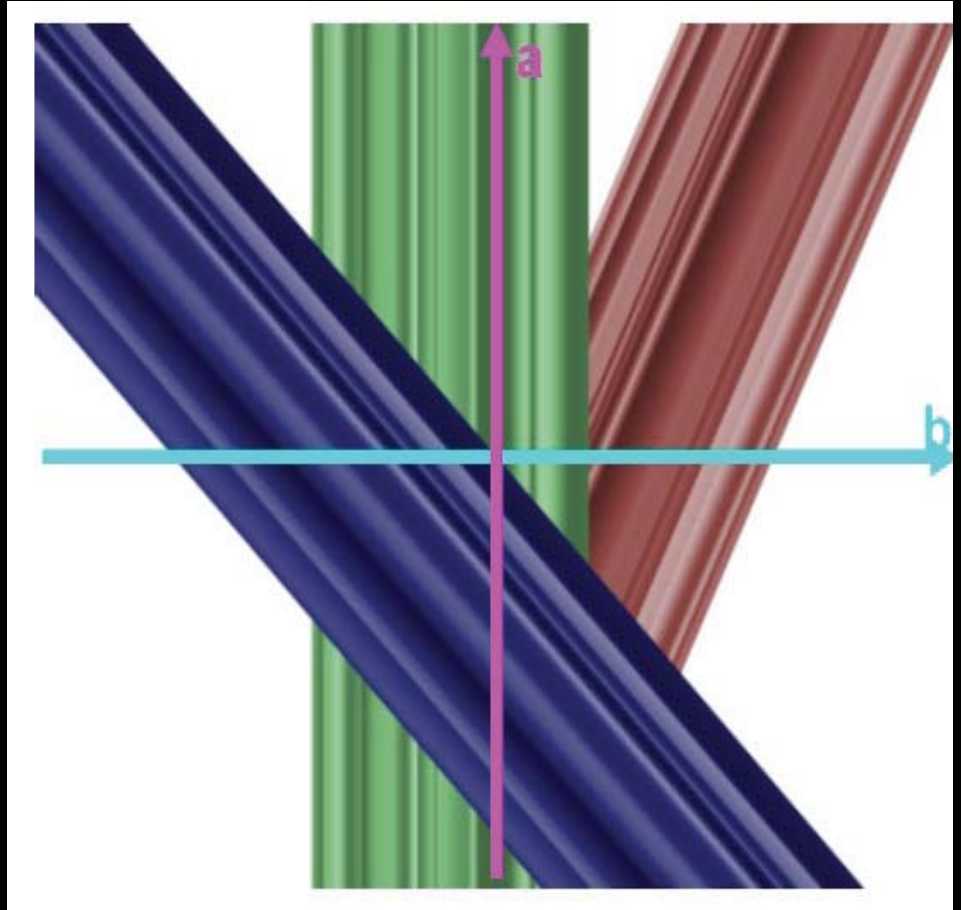
Camera: all-positive linear projection of a 4D lightfield



A more revealing parameterization of the lightfield

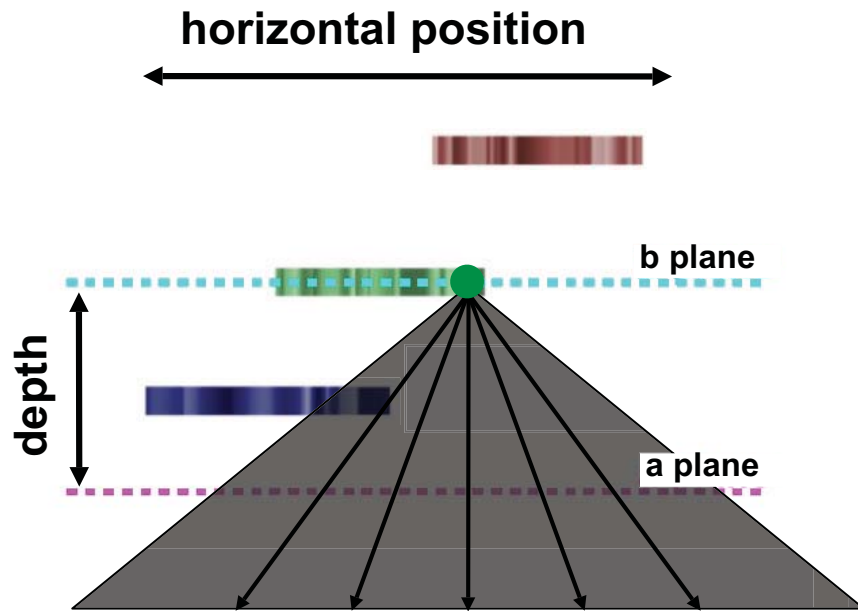
Light field: parameterization of the 4D space of light rays in the world

Provides a convenient way to model different lenses and cameras designs



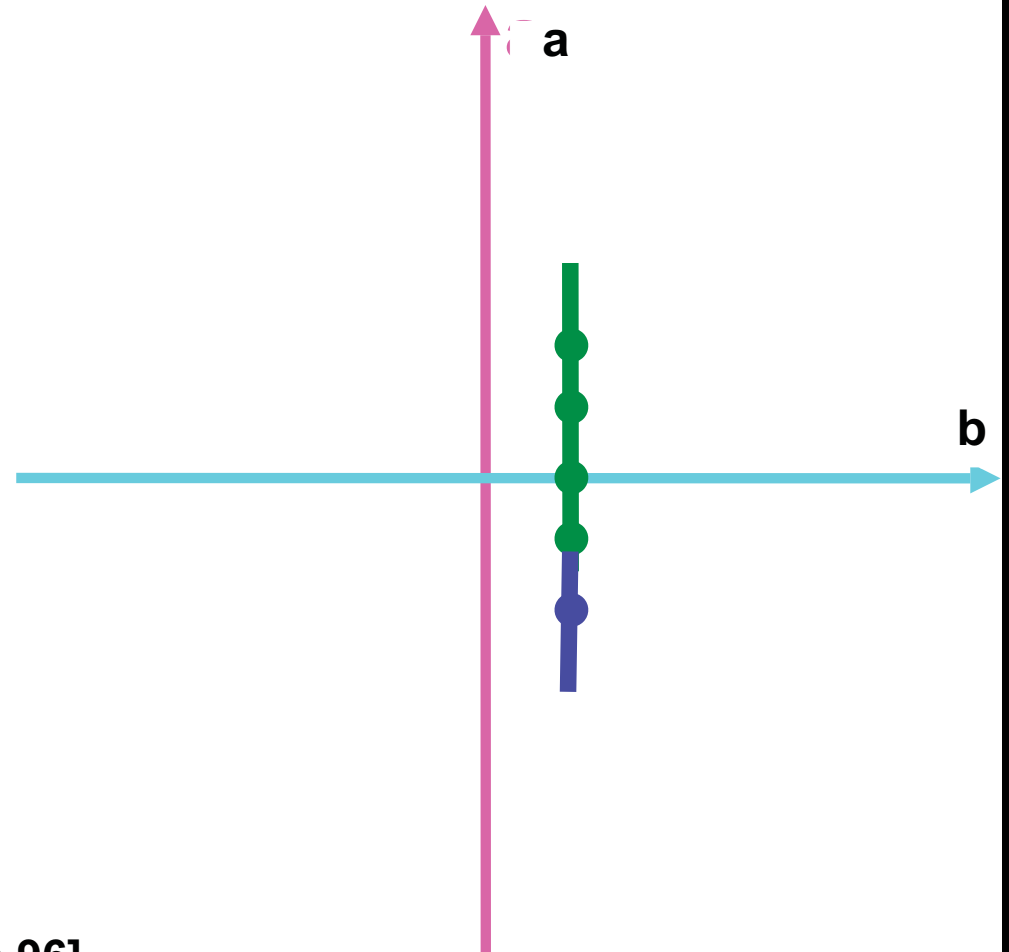
Lightfield tutorial

flatworld 1D scene



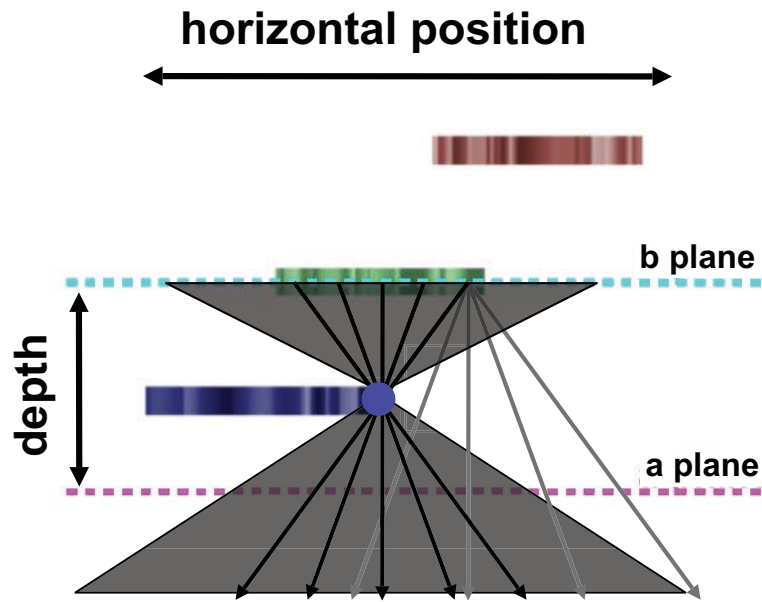
2 plane parameterization [Levoy and Hanrahan 96]

2D lightfield



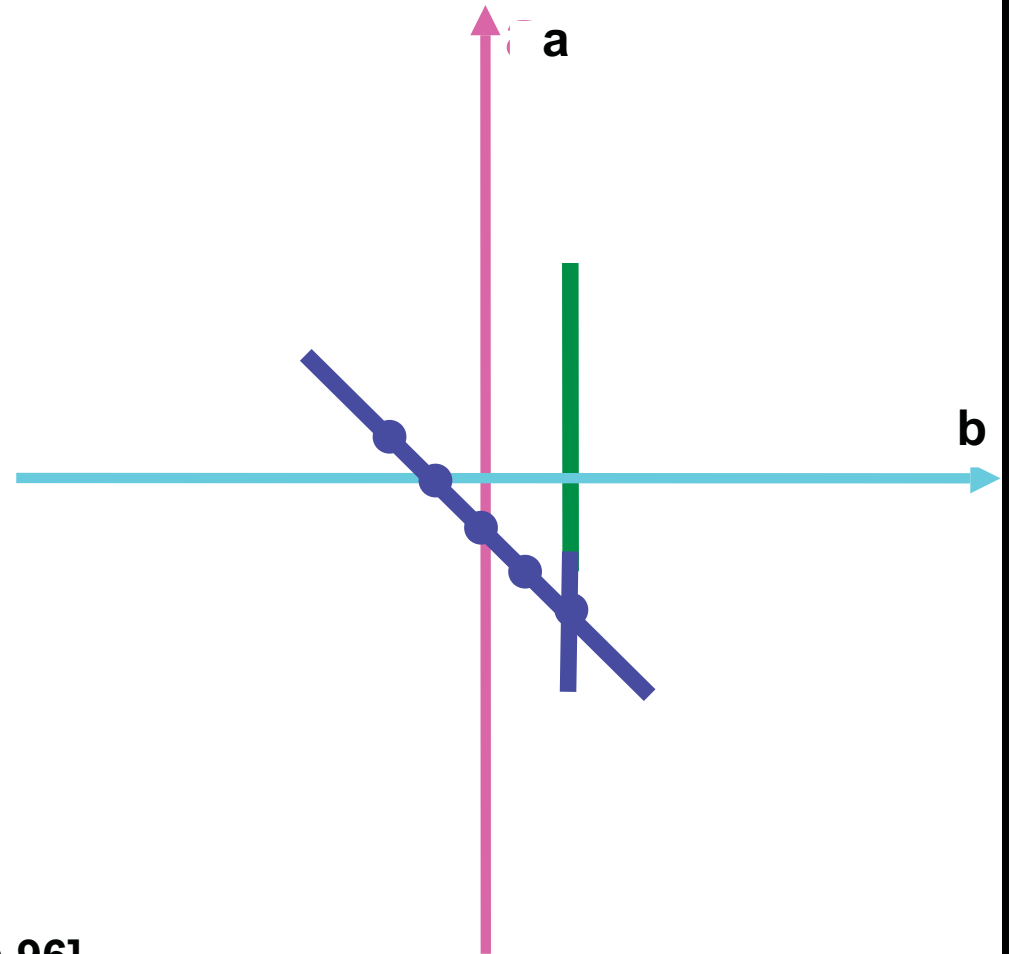
Lightfield tutorial

flatworld 1D scene



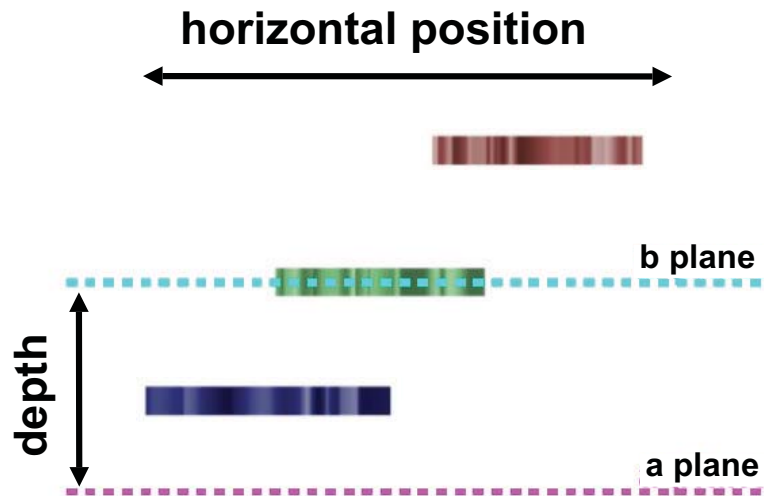
2 plane parameterization [Levoy and Hanrahan 96]

2D lightfield



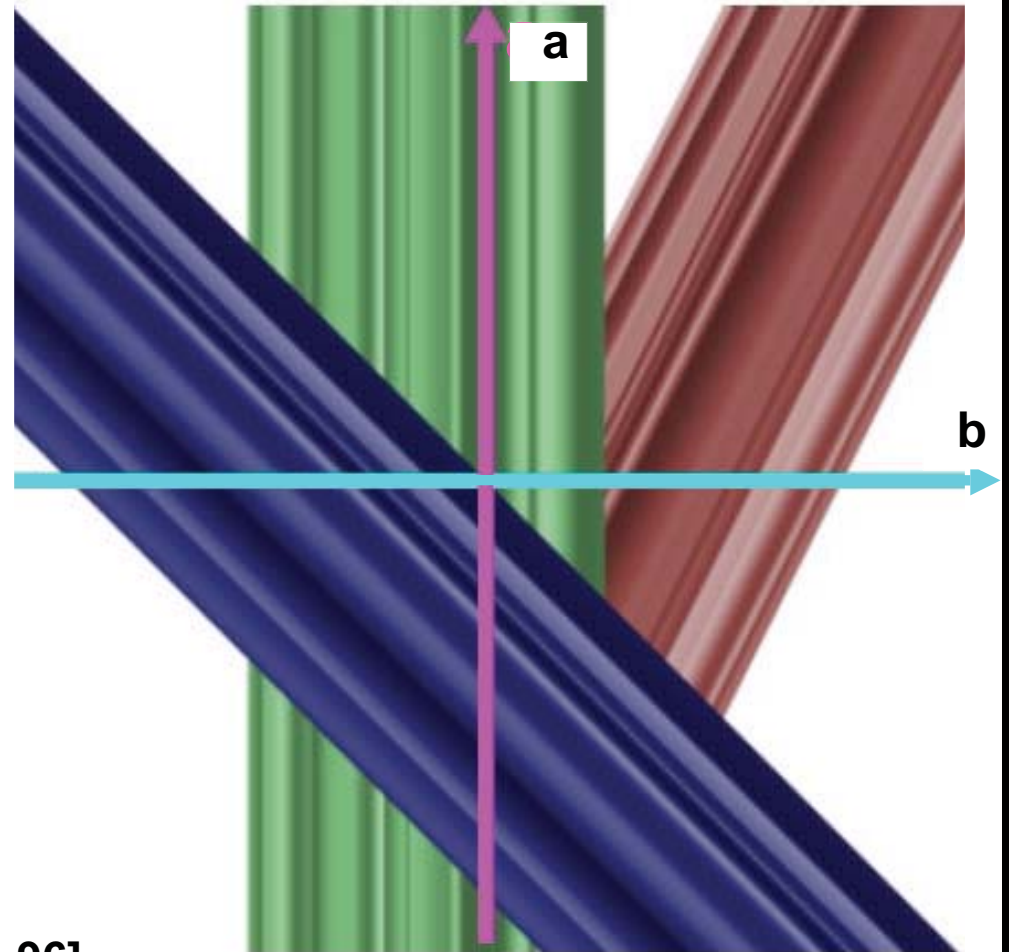
Lightfield tutorial

flatworld 1D scene



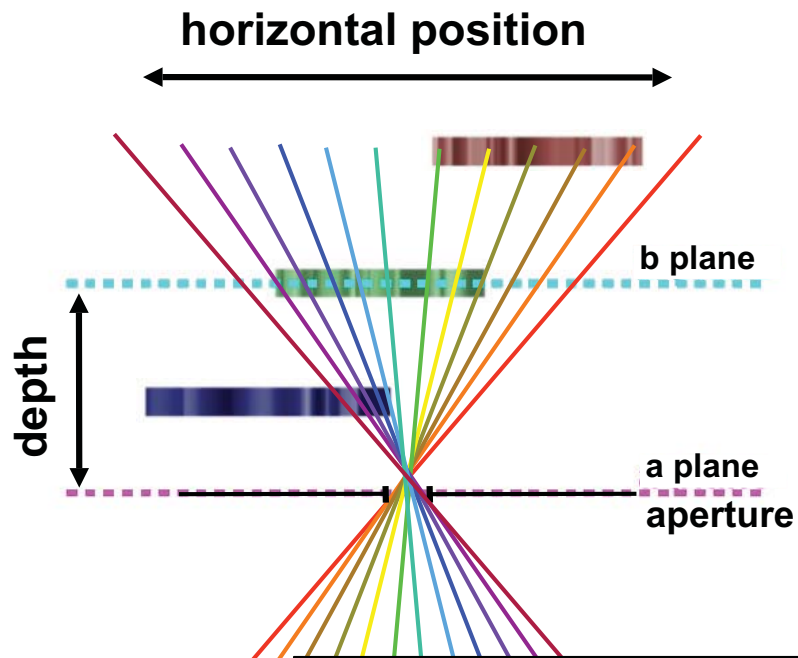
2 plane parameterization [Levoy and Hanrahan 96]

2D lightfield

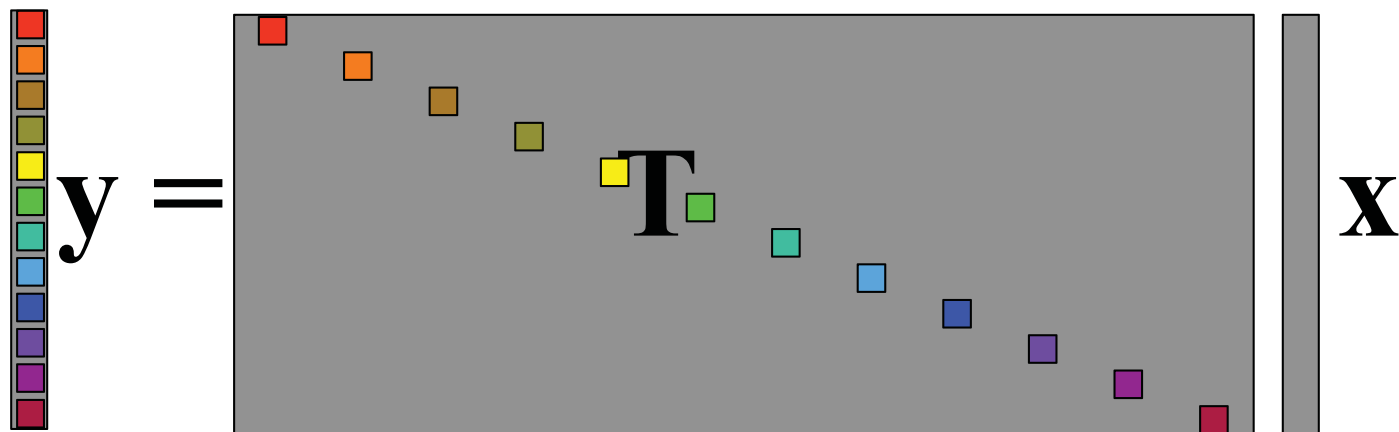
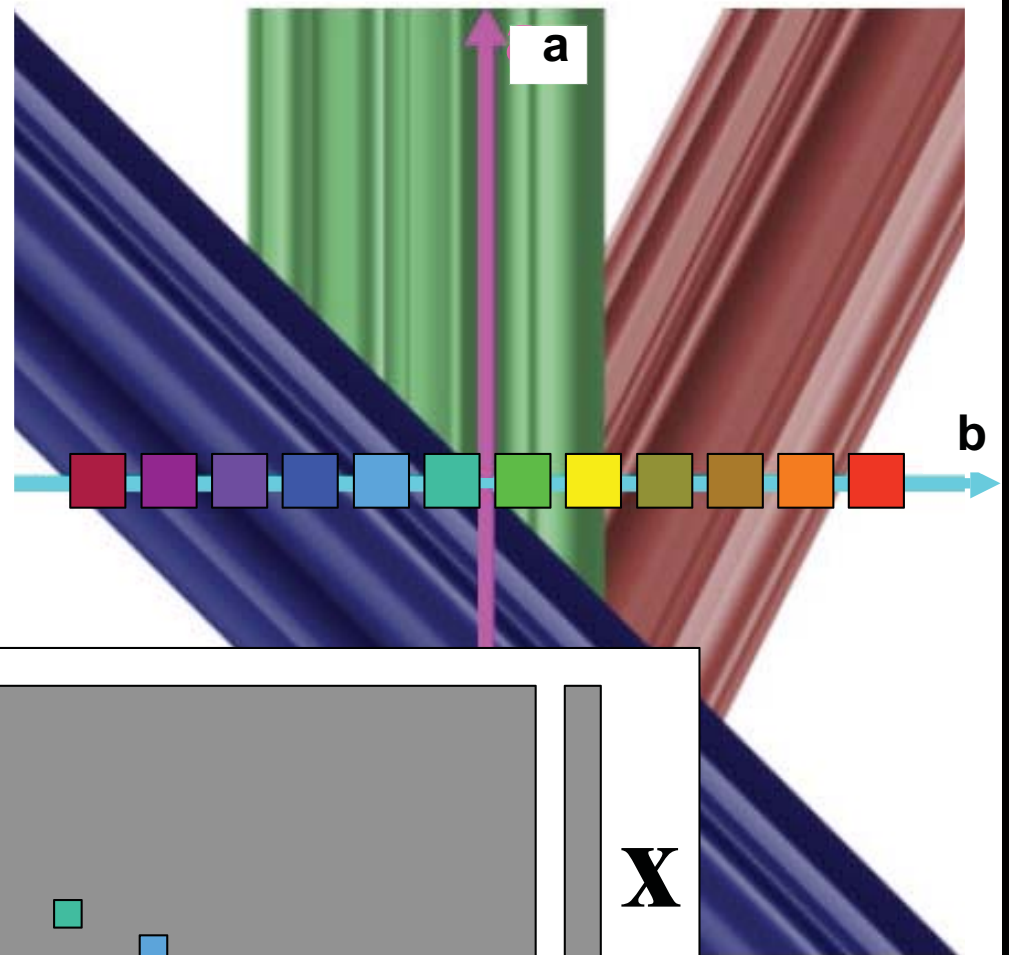


Pinhole camera

flatworld 1D scene

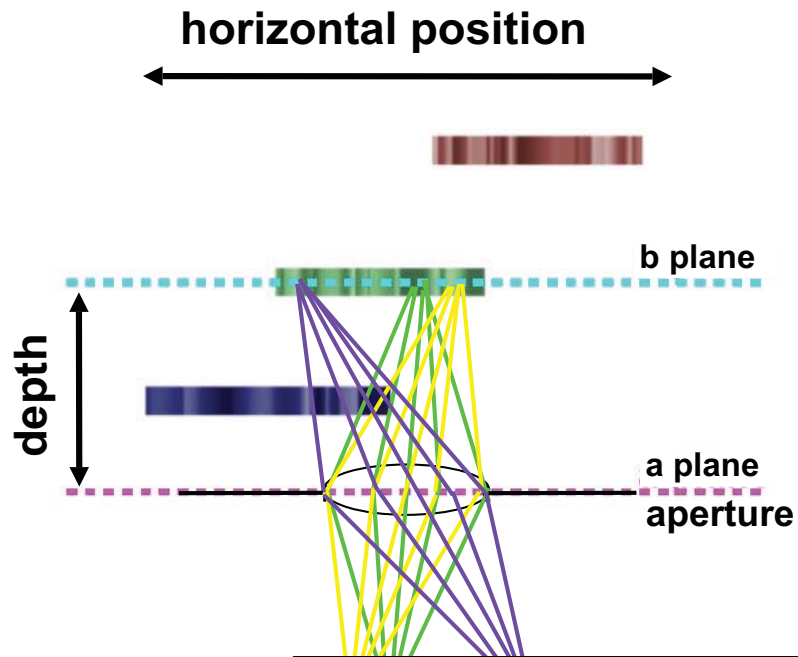


2D lightfield

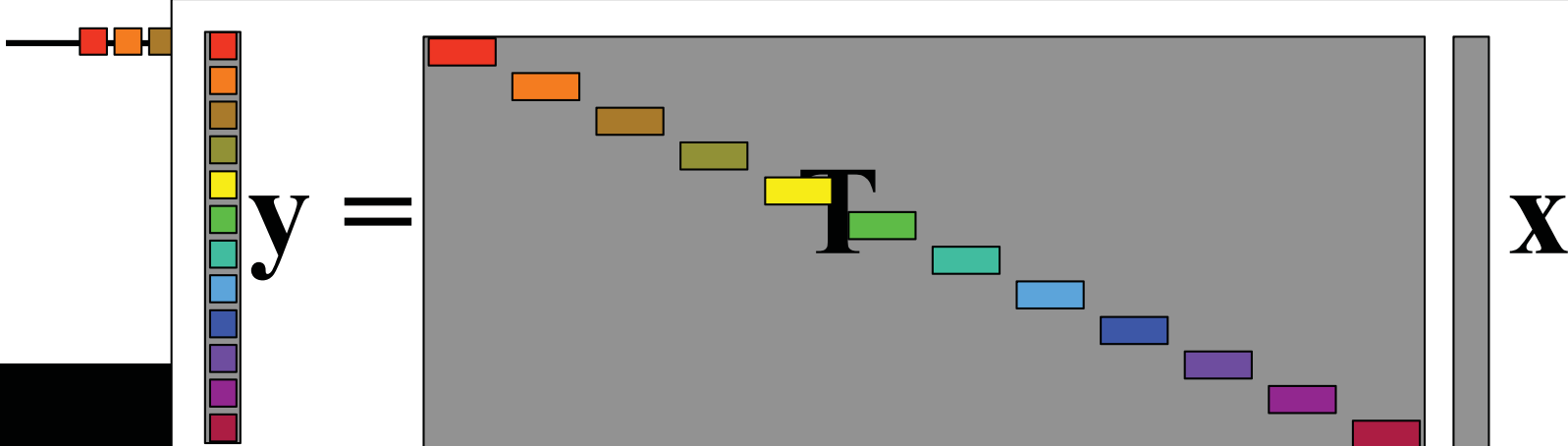
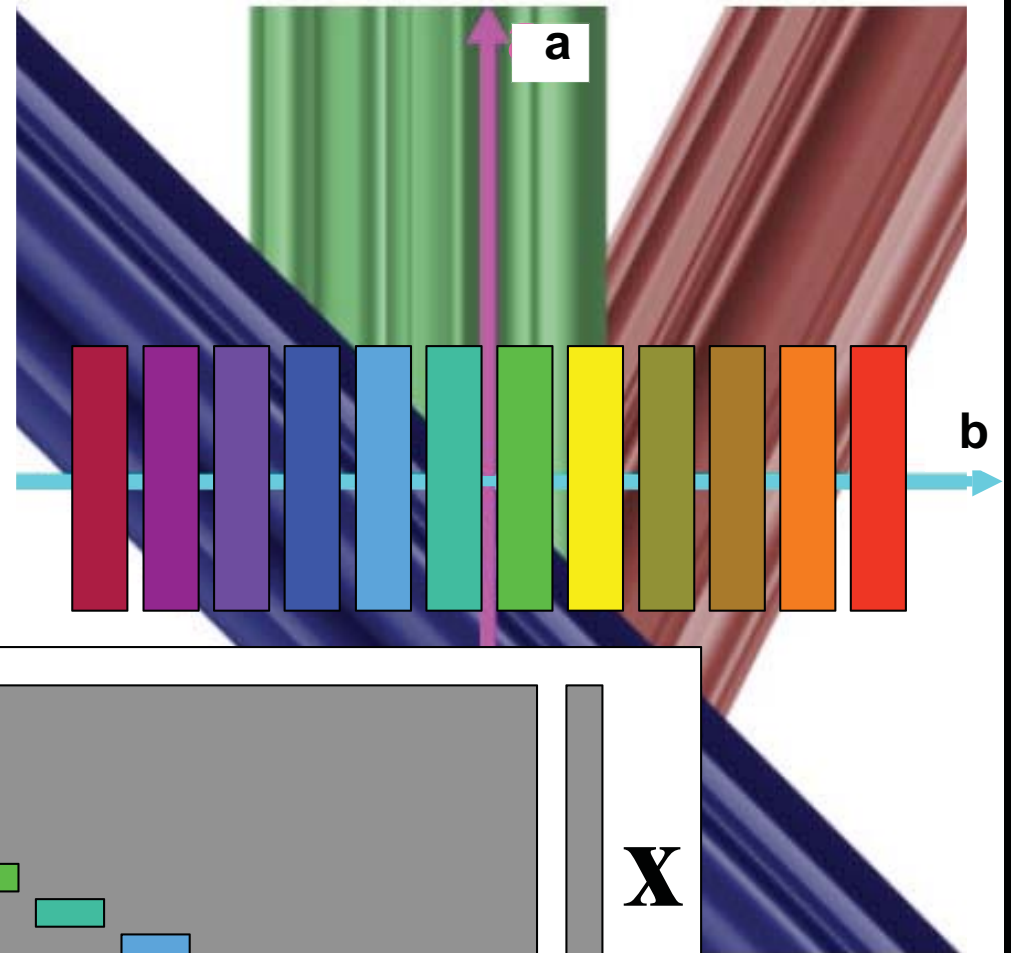


Lens, focused at green object

flatworld 1D scene

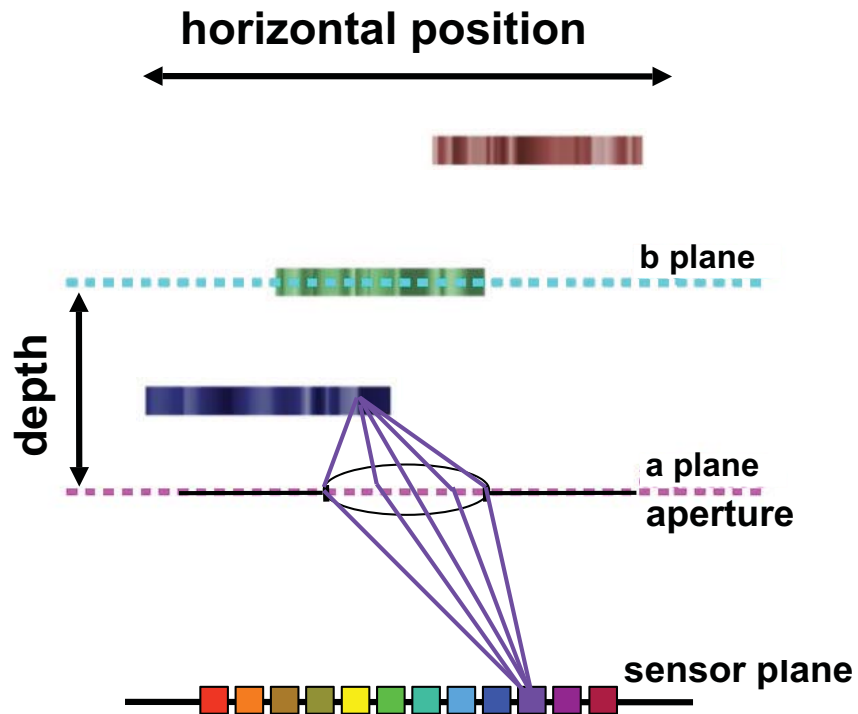


2D lightfield

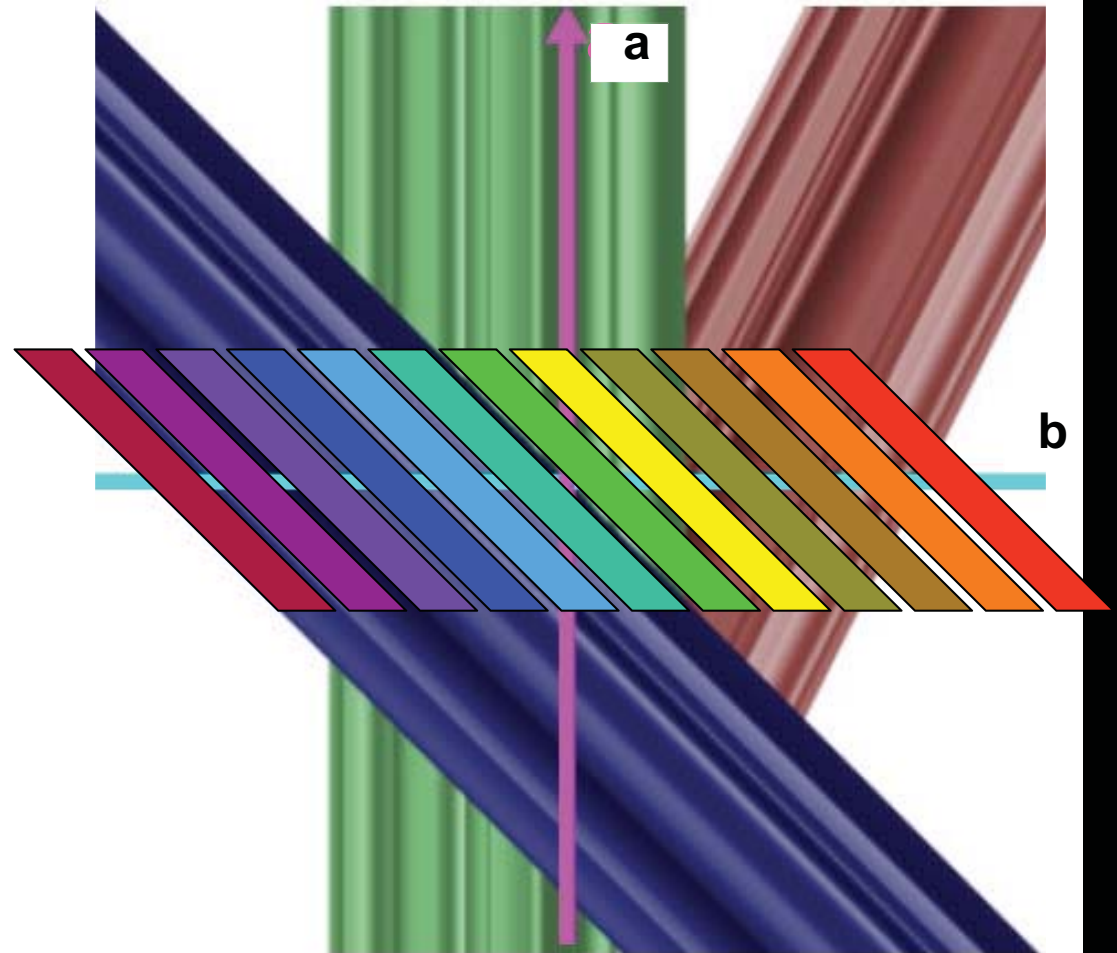


Lens, focused at blue object

flatworld 1D scene

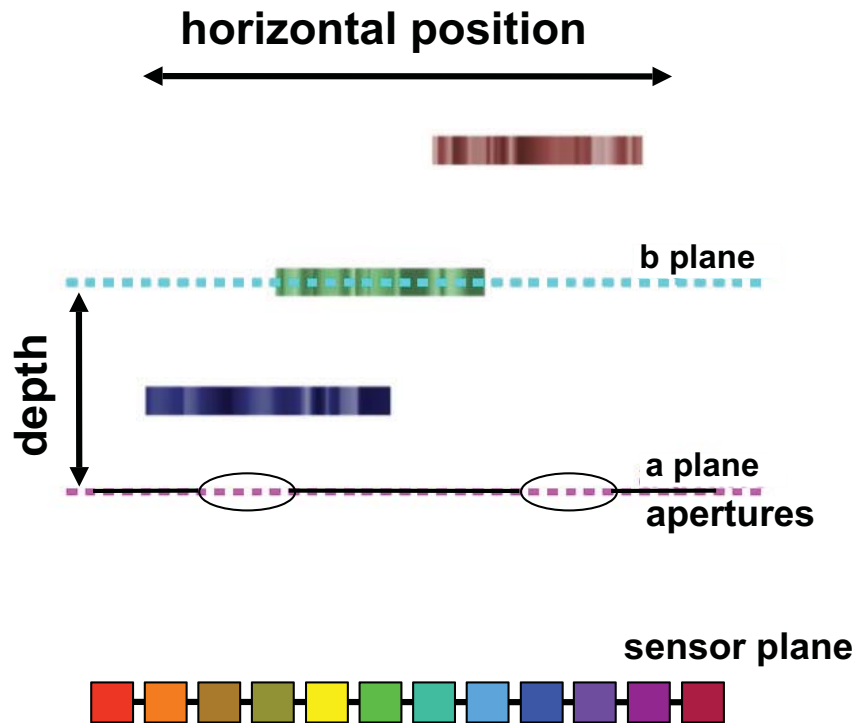


2D lightfield

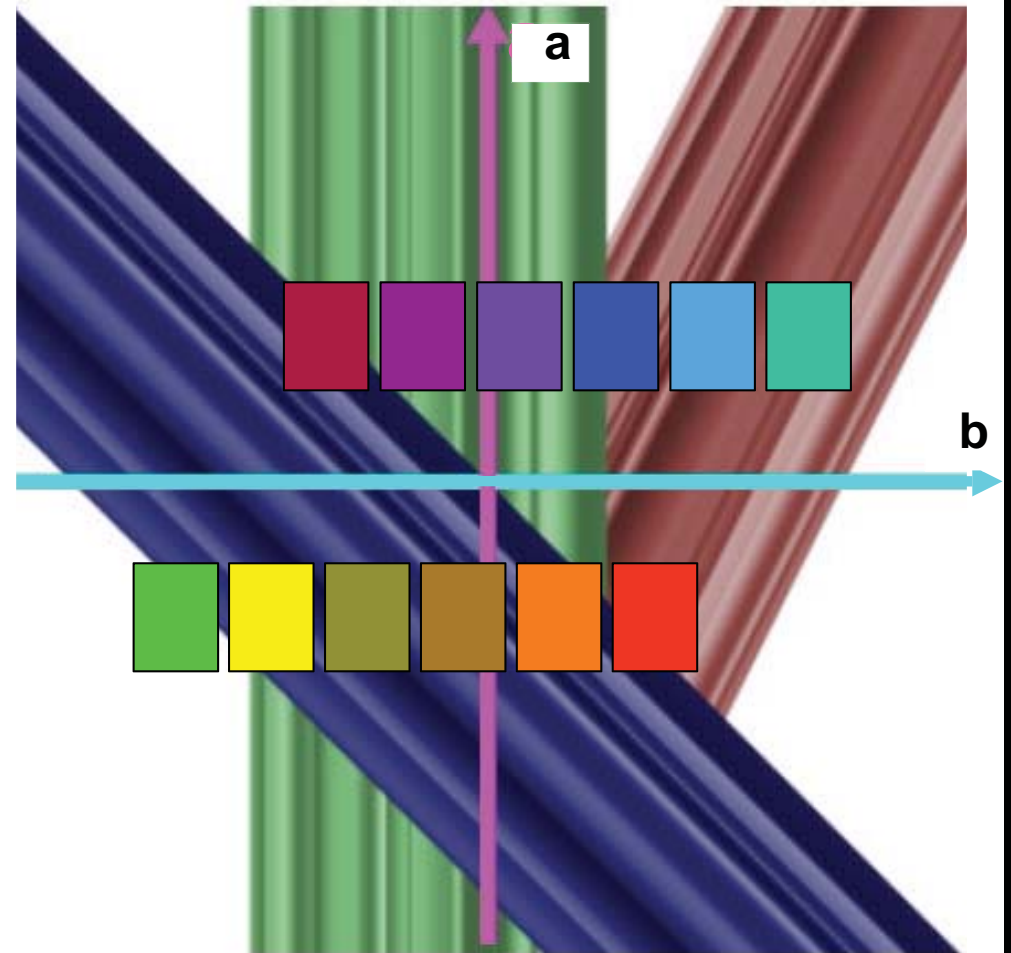


Stereo

flatworld 1D scene

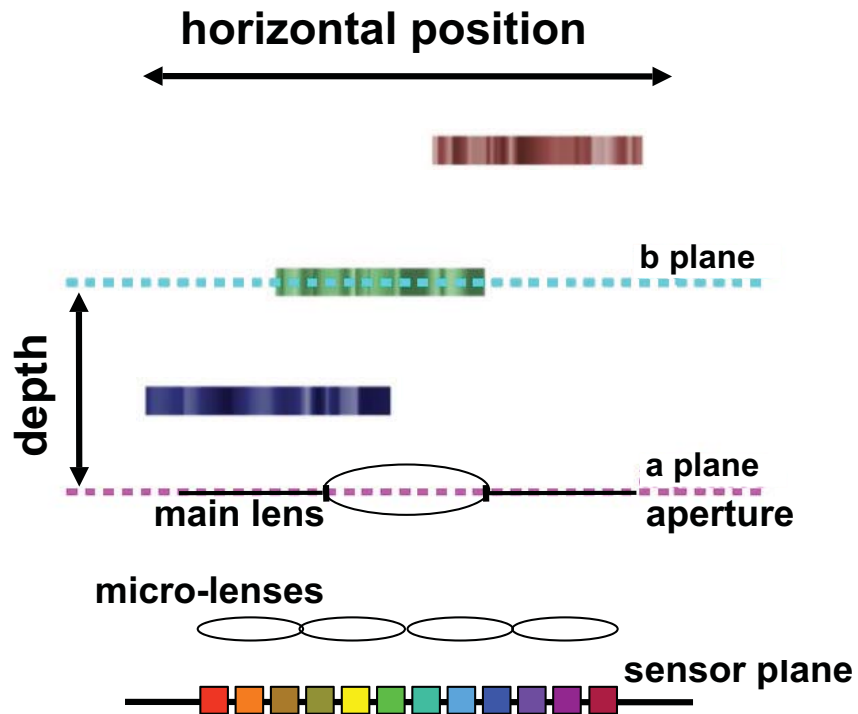


2D lightfield

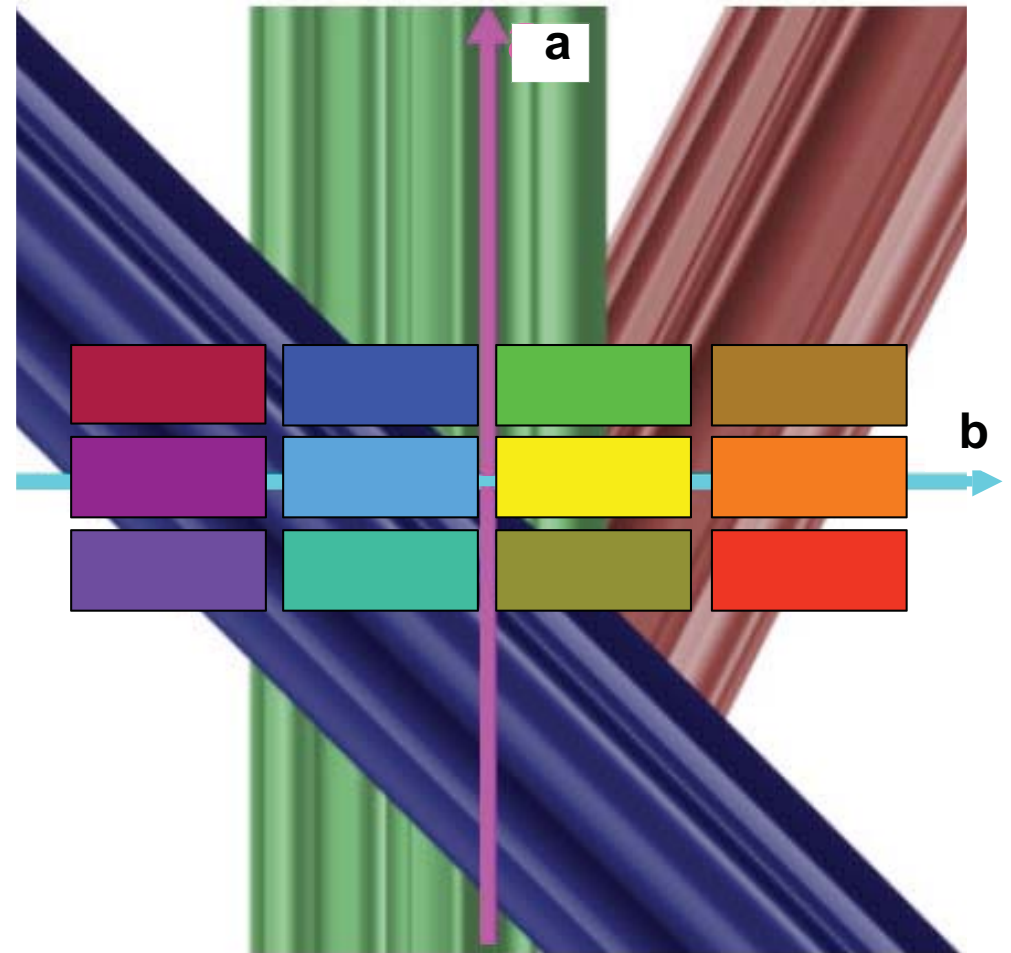


Plenoptic camera

flatworld 1D scene



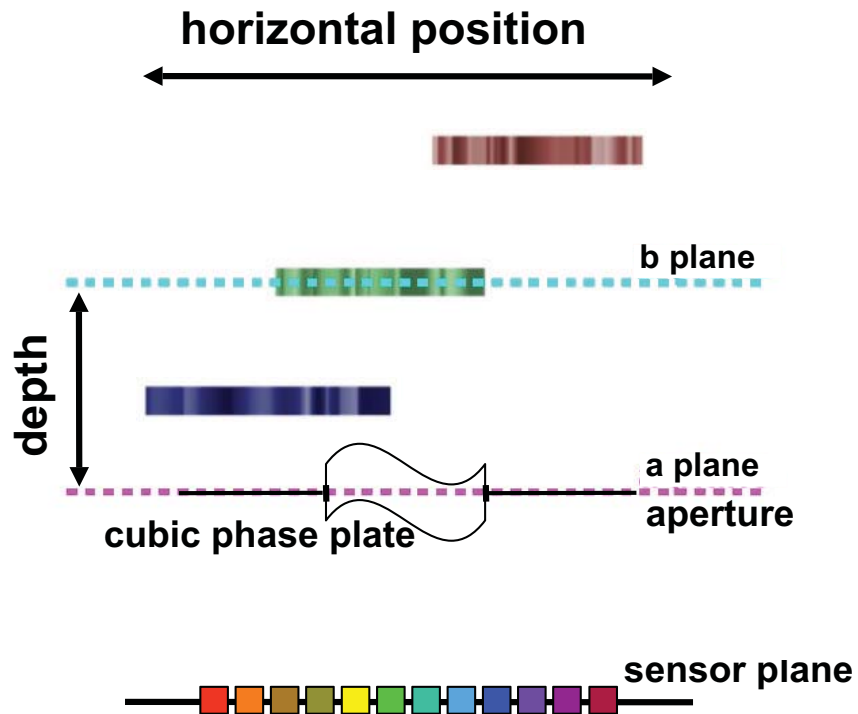
2D lightfield



Adelson and Wang 92, Ng et al 05

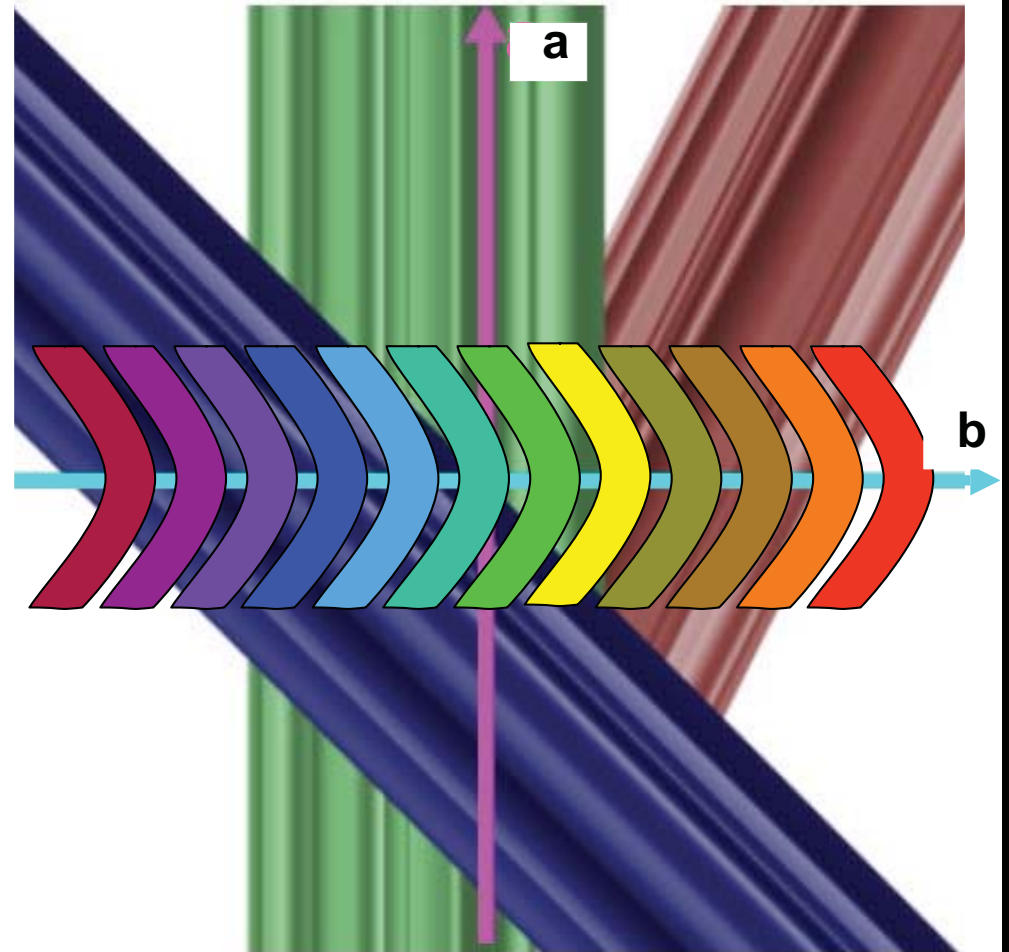
Wavefront coding

flatworld 1D scene



Dowski and Cathey,94

2D lightfield



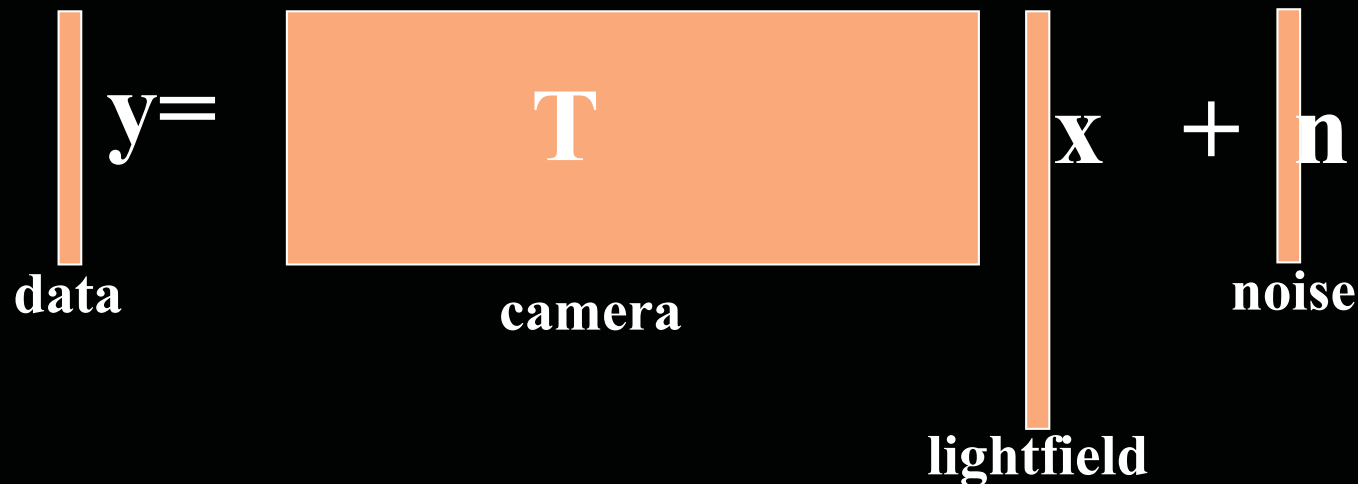
Computational imaging

Camera: Rank deficient projection of a 4D lightfield.

Decoding: ill-posed inversion, need prior on lightfield signals.

Camera evaluation: How well can recover the lightfield from projection?

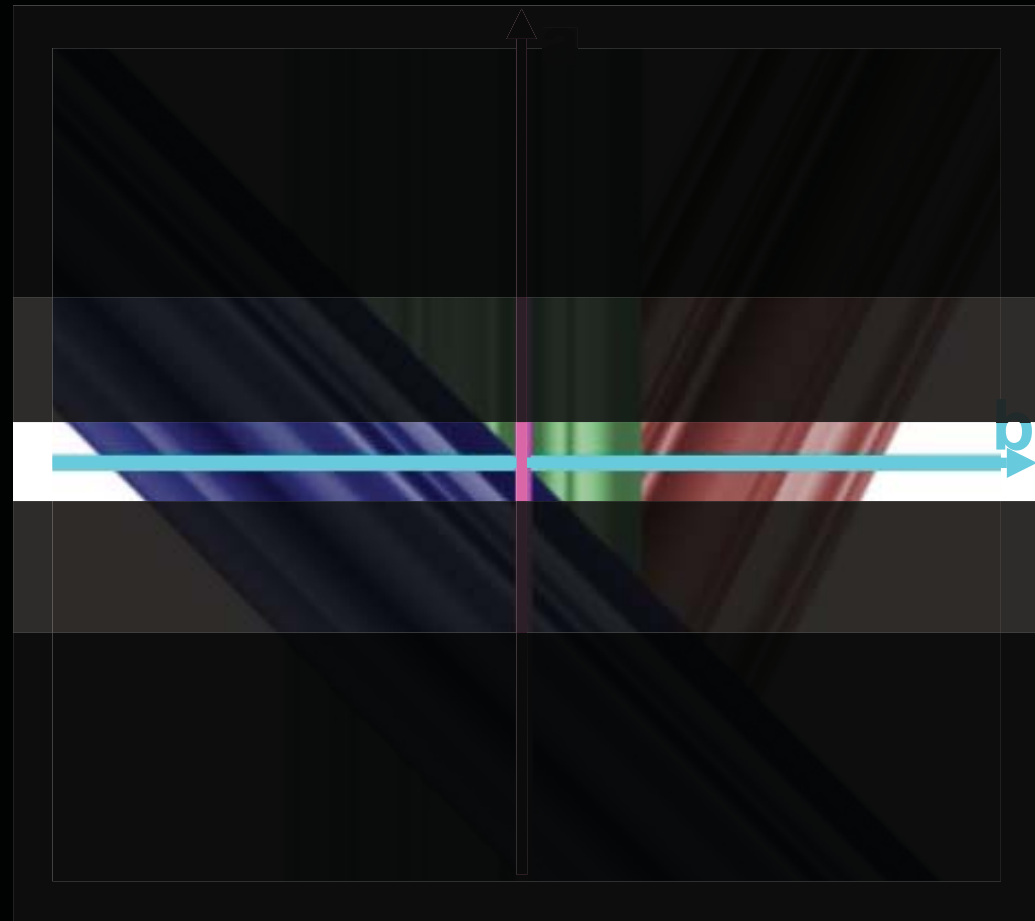
$$\mathbf{y} = \mathbf{T}\mathbf{x} + \mathbf{n}$$



Varying imaging goals by weighted lightfield reconstruction

- Full light field reconstruction (potentially image&depth)
- Reconstruct a bounded view range
- Single row light field reconstruction (pinhole all focused image)

Weight reconstruction error differently in different light field entries



Bayesian lightfield imaging – Outline

- **Specify lightfield reconstruction goals**
 - Full lightfield / Single, all-focus view /...
- **Specify lightfield prior**
- **Imaging with one computational camera**
 - Specify camera projection matrix
 - Camera decoding - Bayesian inference
- **Comparing computational cameras**
 - Specify camera projection matrices
 - Evaluate expected error in lightfield reconstruction

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Our light field prior: a mixture of signals at different slopes



Hidden variable S modeling local slope

Conditioning on slope:

small variance along slope direction

high variance along spatial direction

Light field prior is a mixture of oriented Gaussians (MOG):

$$P(x) = \int_S P(S)P(x|S)$$

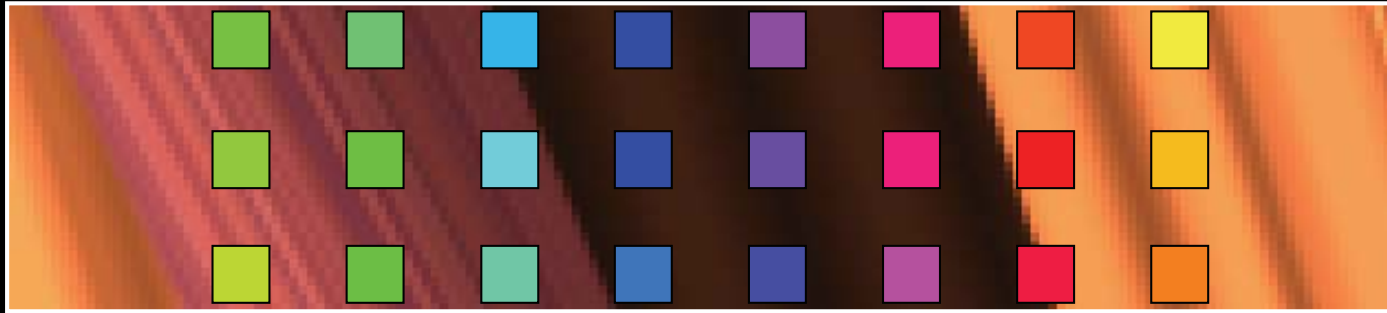
Piecewise smooth
prior on slopes

Given slope, lightfield
prior is Gaussian and
simple

Bayesian lightfield imaging – Outline

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Prior effect on reconstruction



Band-limited reconstruction to account for unknown depth



See paper for
inference details



Reconstruction using light field prior

Bayesian lightfield imaging – Outline

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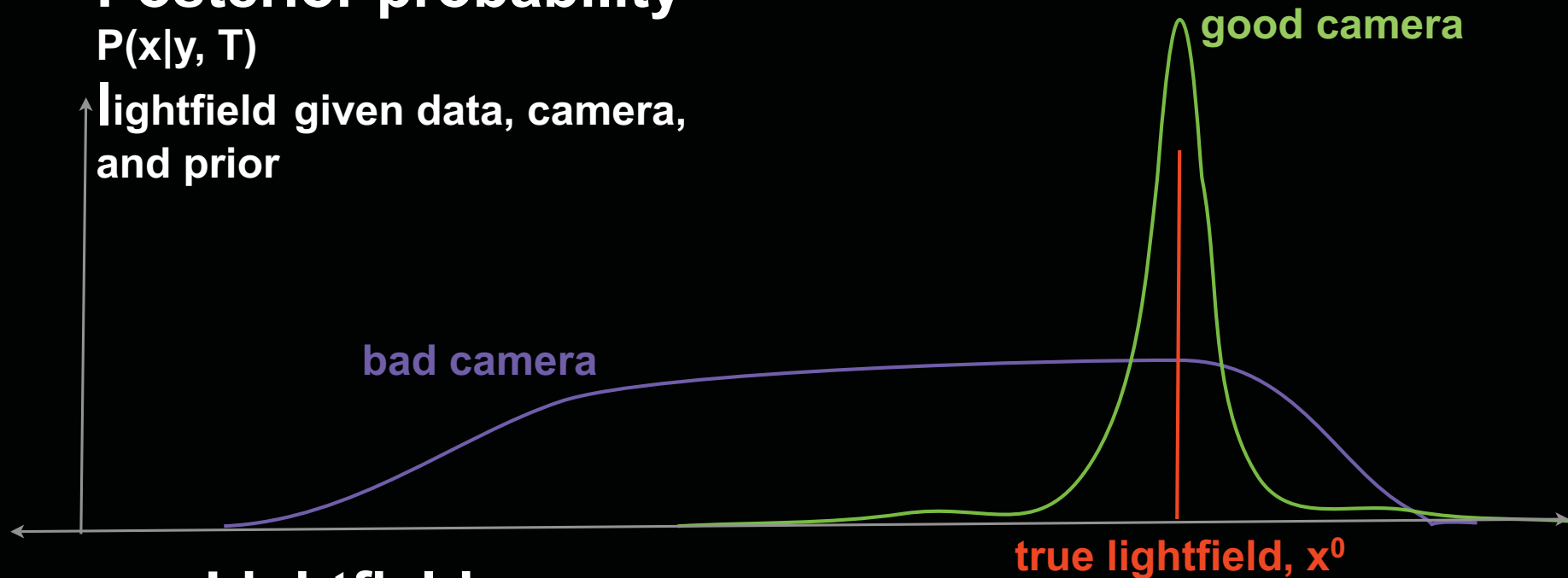
Camera evaluation

**Goal: evaluate inherent ambiguity of a camera projection,
independent of inference algorithm**

Posterior probability

$P(x|y, T)$

lightfield given data, camera,
and prior



Lightfield, x

(schematic picture of the very
high-dimensional vector)

Camera evaluation function: expected squared error

$$E_{P(x|y;T)} \left[\|x - x^0\|^2 \right] = \int_x P(x | y; T) \|x - x^0\|^2$$

With our mixture model prior, conditioned on the lightfield slopes S , everything is Gaussian and analytic. So let's write the posterior as:

$$P(x | y; T) = \int_S P(S | y; T) P(x | y, S; T)$$

Then our expected squared error becomes an integral over all slope fields:

$$E_{P(x|y;T)} \left[\|x - x^0\|^2 \right] = \int_S P(S | y; T) E_{P(x|y,S;T)} \left[\|x - x^0\|^2 \right]$$

Approximate by Monte Carlo sampling near the true slope field:

$$E_{P(x|y;T)} \left[\|x - x^0\|^2 \right] \approx \sum_{S_i} P(S_i | y; T) E_{P(x|y,S_i;T)} \left[\|x - x^0\|^2 \right]$$

Bayesian camera evaluation tool

Input parameters:

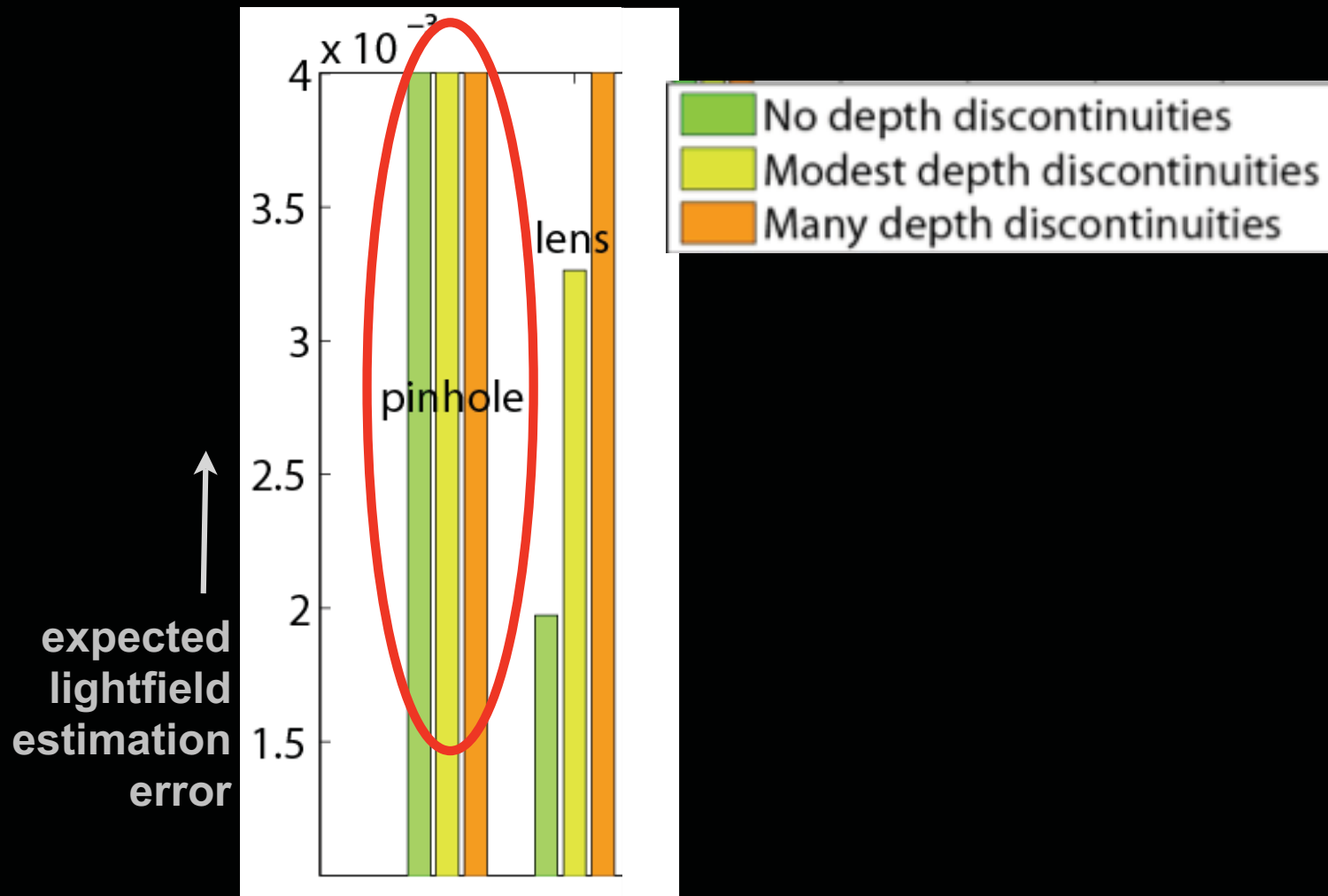
- Reconstruction goals (weight on light field entries)
- Camera matrix
- Noise level
- Spatial and depth resolution

Output: expected reconstruction error

Matlab software online:

people.csail.mit.edu/alevin/papers/lightfields-Code-Levin-Freeman-Durand-08.zip

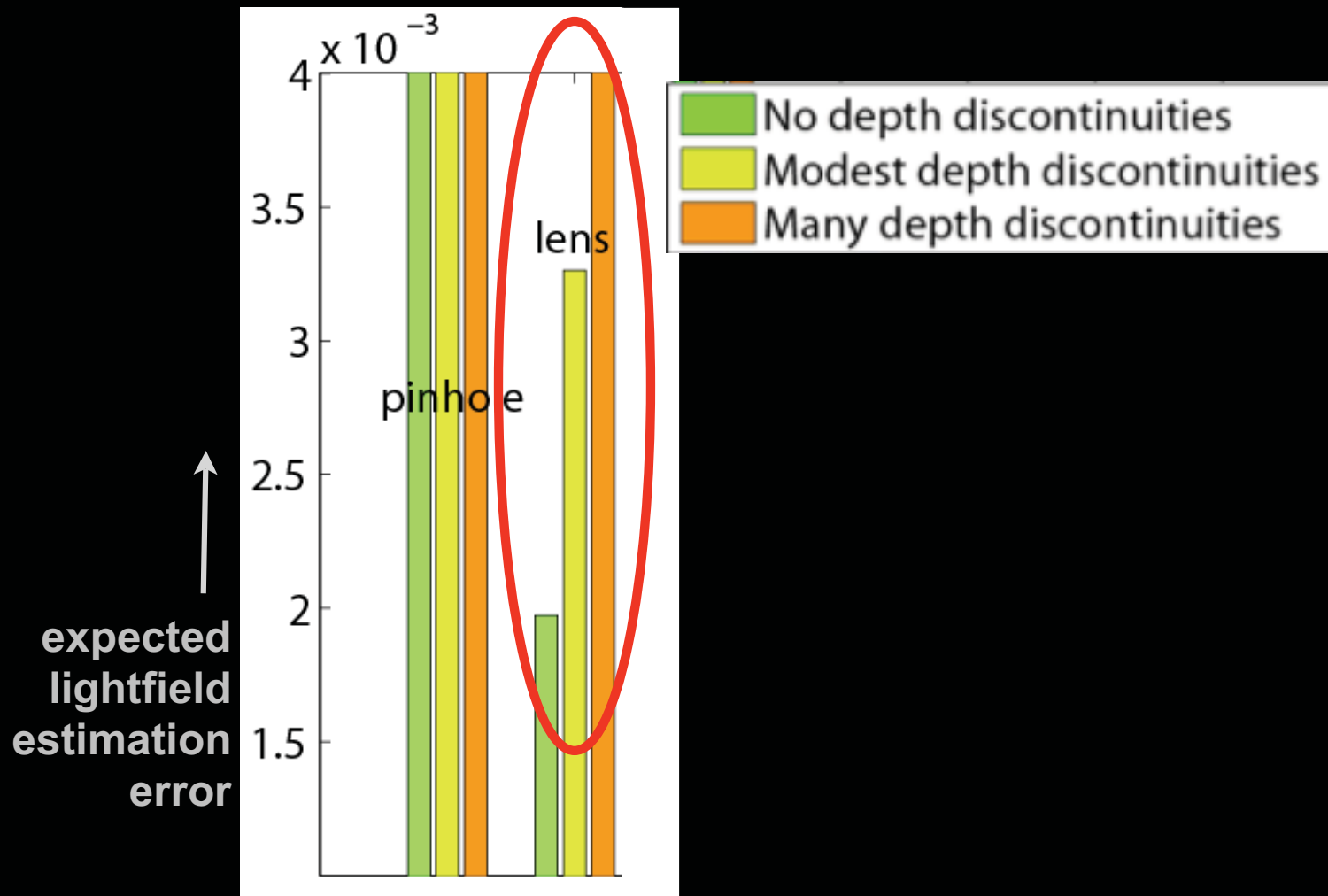
1D camera evaluation– full light field reconstruction



Observation:

As expected, a pinhole camera doesn't estimate the lightfield well

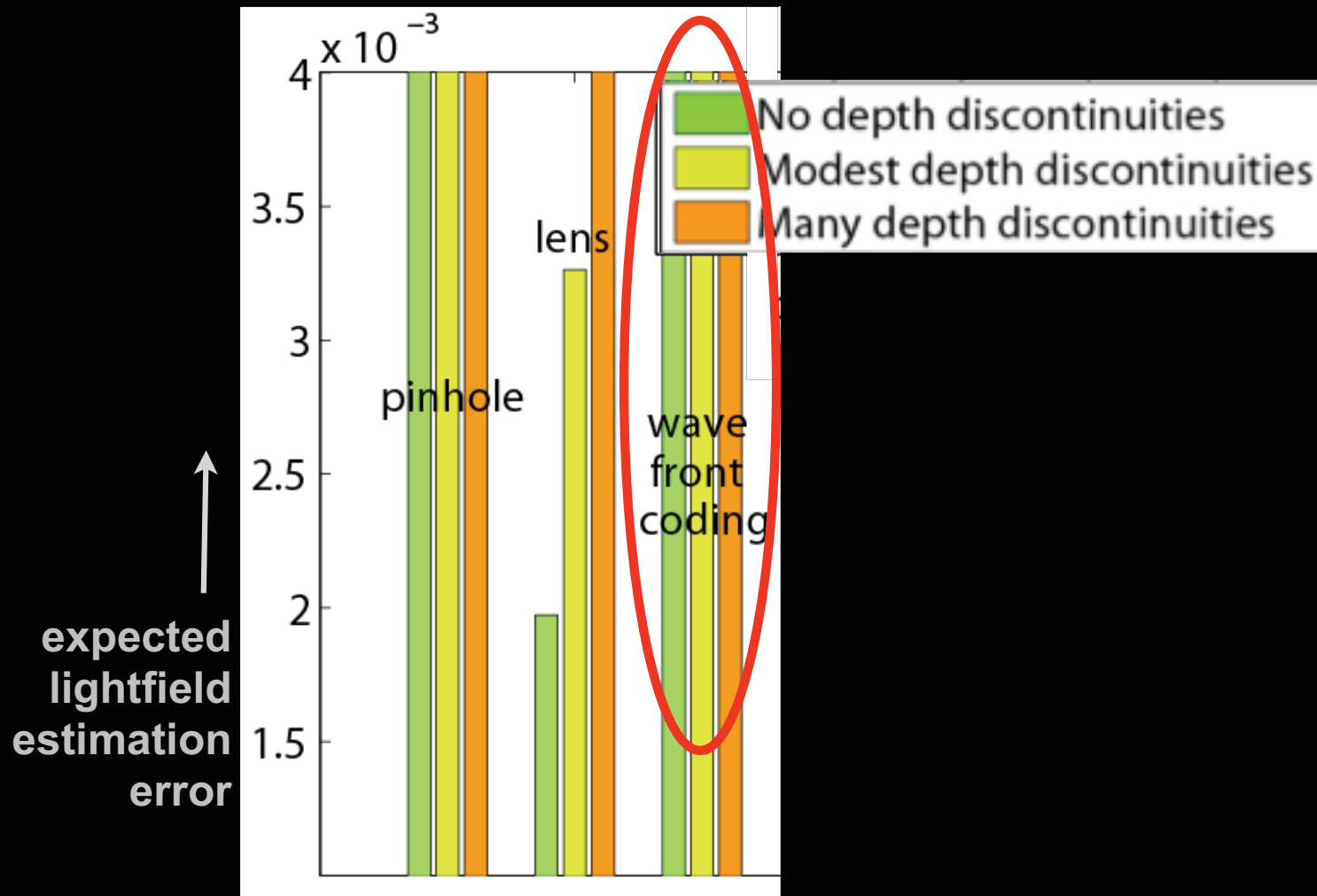
1D camera evaluation– full light field reconstruction



Observation:

When depth variation is limited, some depth from defocus exist in a single monocular view from a standard lens

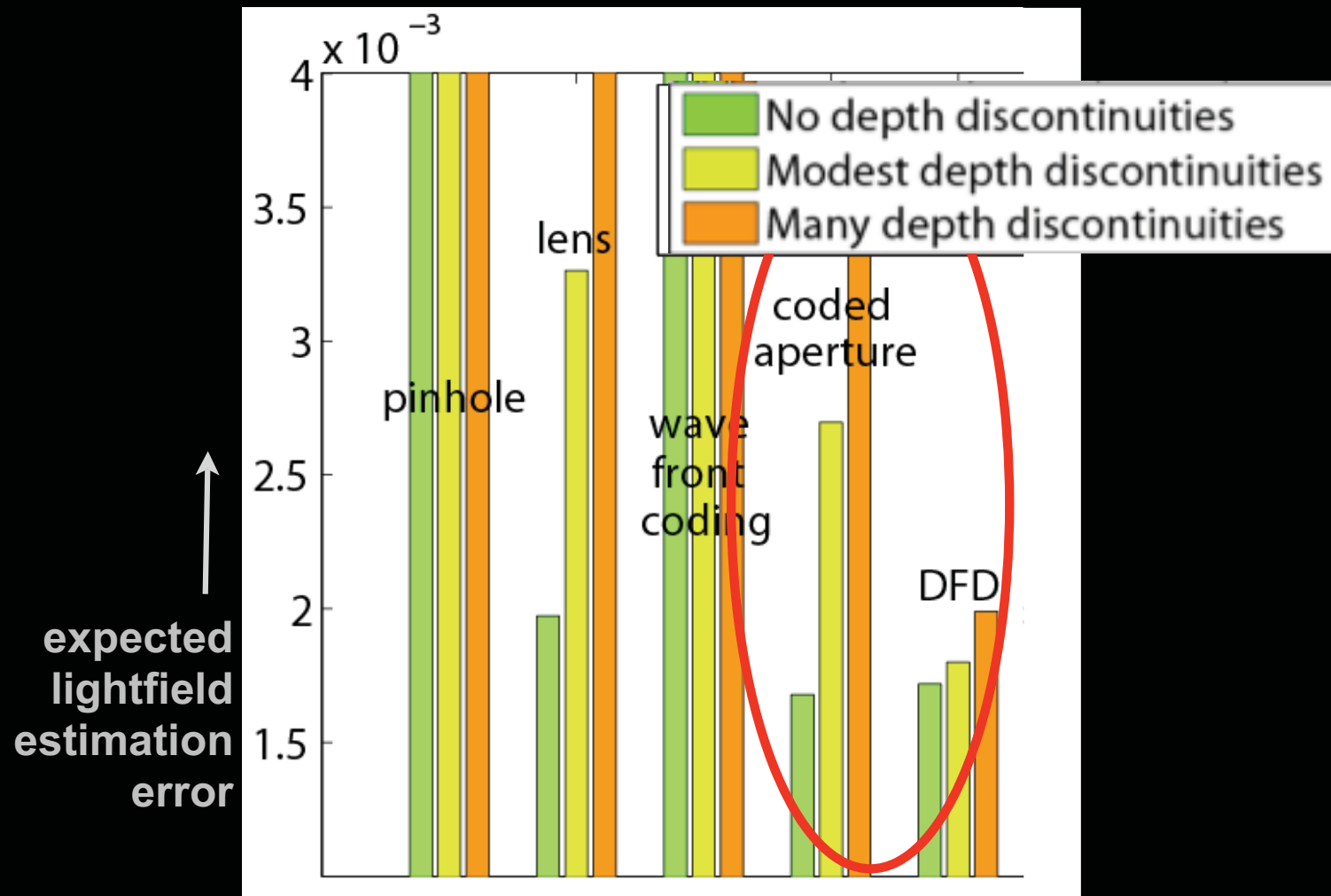
1D camera evaluation– full light field reconstruction



Observation:

Wavefront coding, not designed to estimate the lightfield, doesn't.

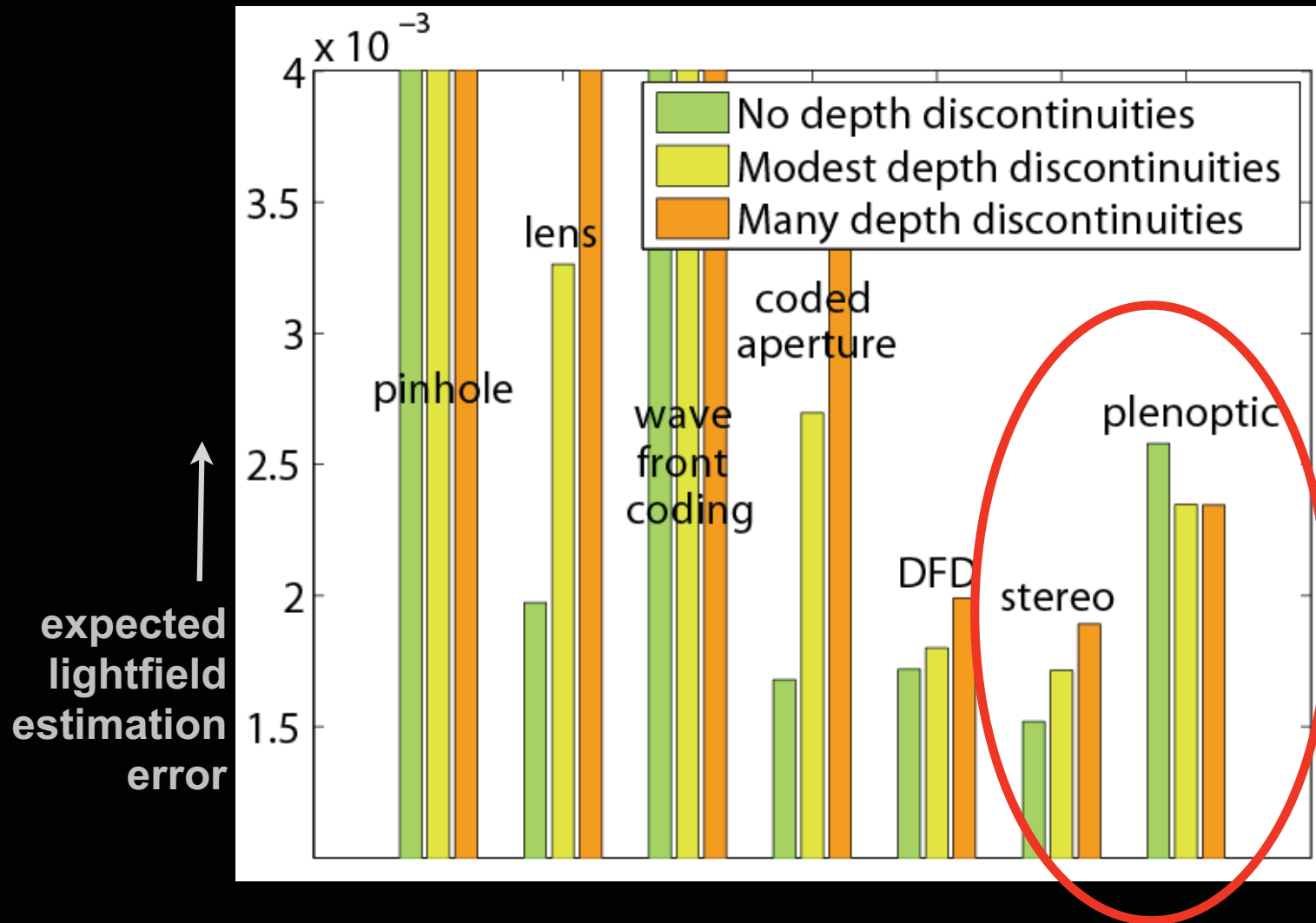
1D camera evaluation– full light field reconstruction



Observation:

Depth-from-defocus (DFD) outperforms the coded aperture at these settings

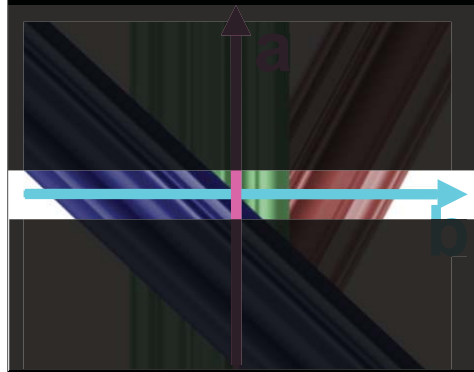
1D camera evaluation– full light field reconstruction



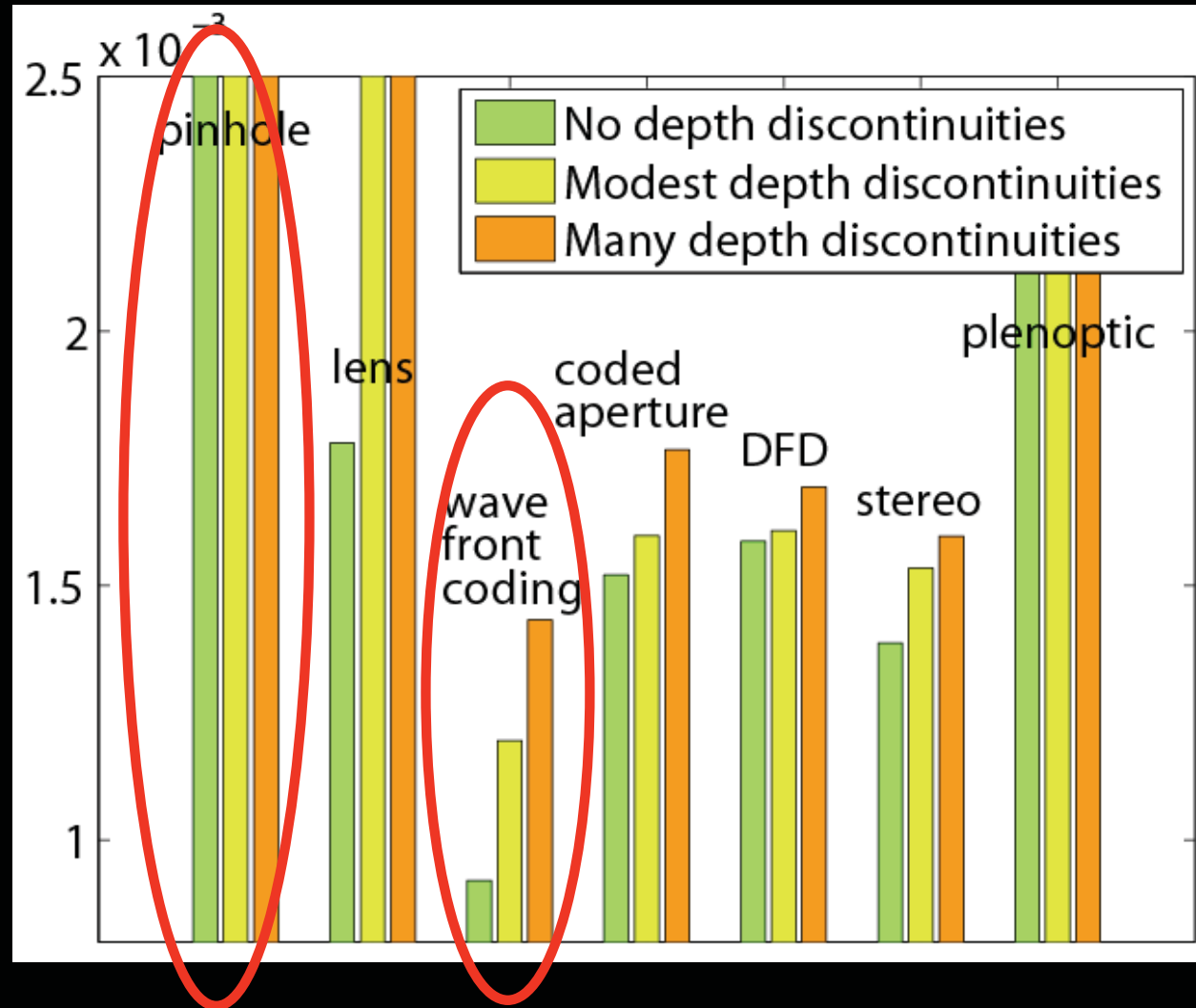
Observation: Stereo error is less than Plenoptic

Since depth variation is smaller than texture variation, no need to sacrifice so much spatial resolution to capture directional information

1D camera evaluation– single row reconstruction



↑
expected
lightfield
estimation
error



Observations:

Pinhole camera- poor estimation due to noise

Wavefront coding- no depth information, but accurate reconst for a single view 33

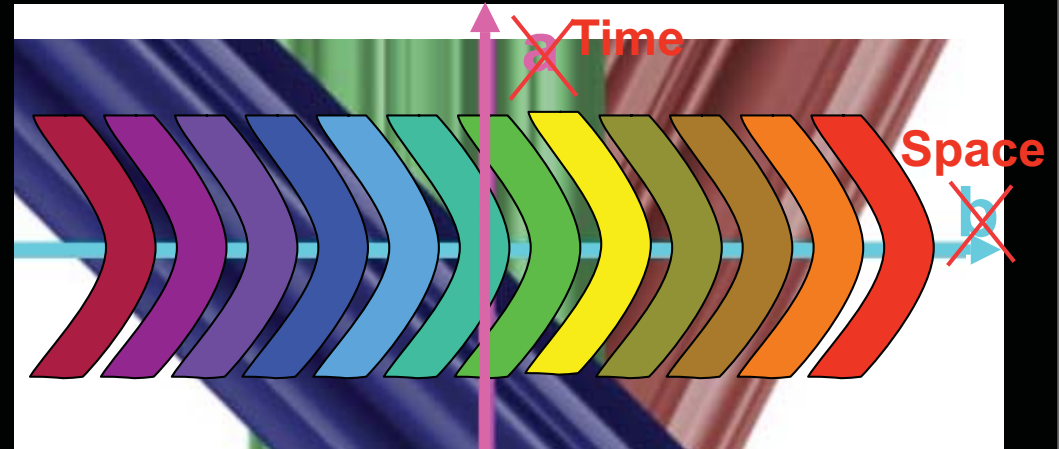
Application: motion invariant photography

Depth invariant integration



Motion invariant integration

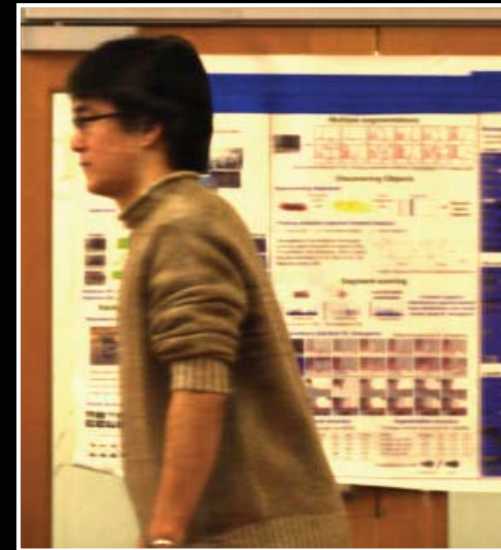
SIGGRAPH 2008, Levin et al.



Static camera



motion invariant

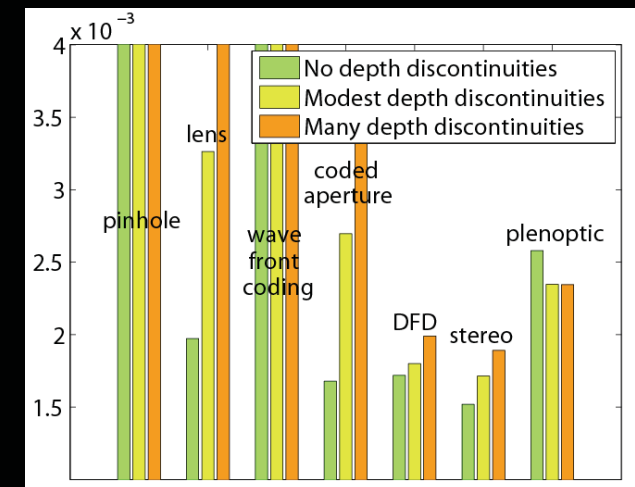
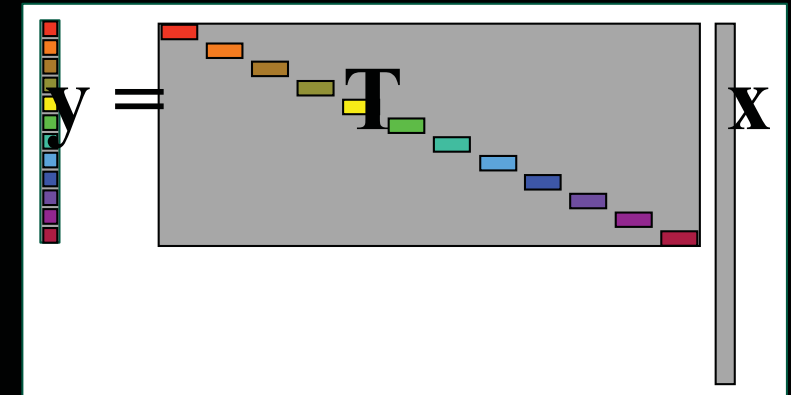


output after

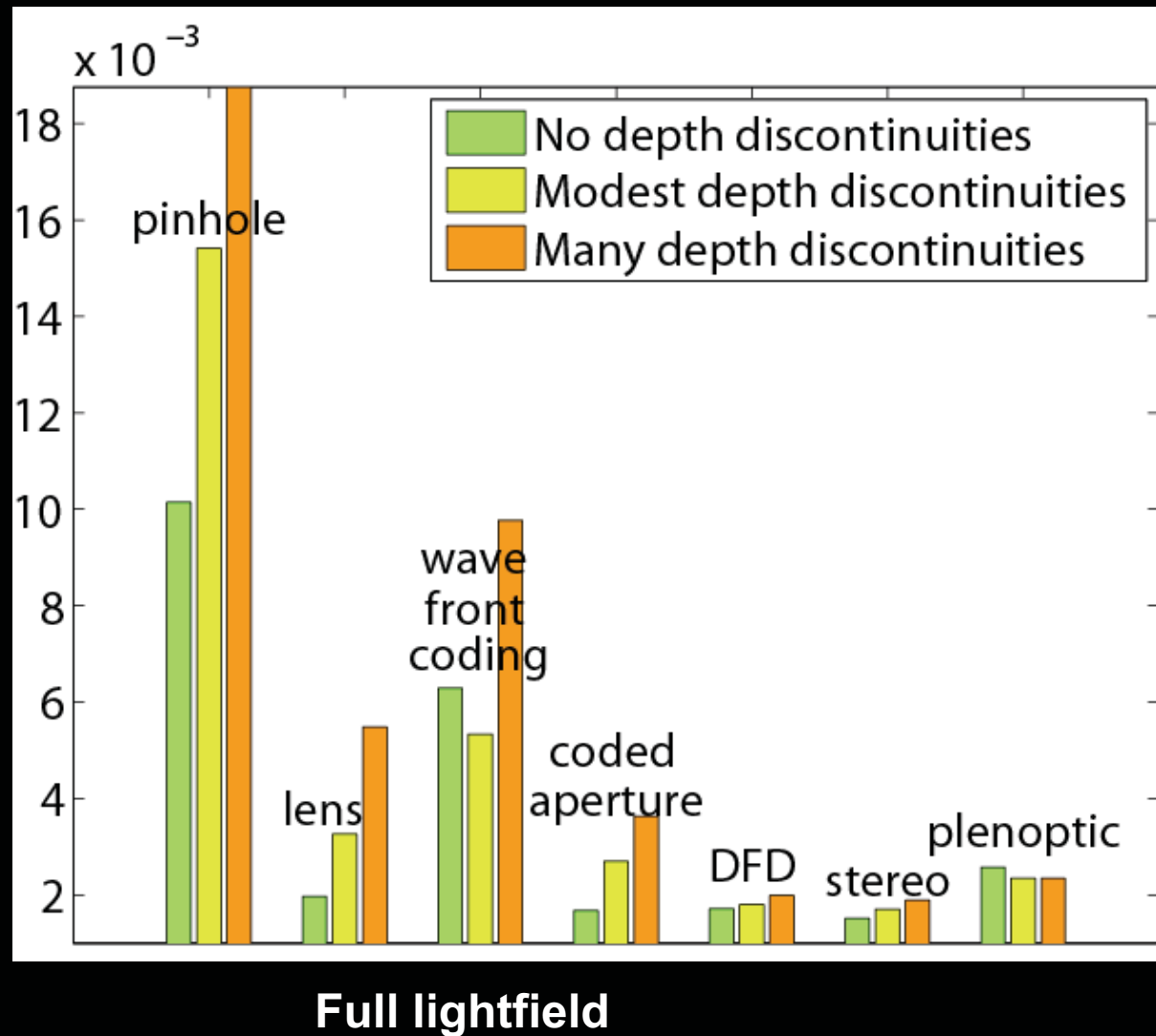
speed-invariant blur allows non-blind deconvolution

Summary: Bayesian lightfield imaging

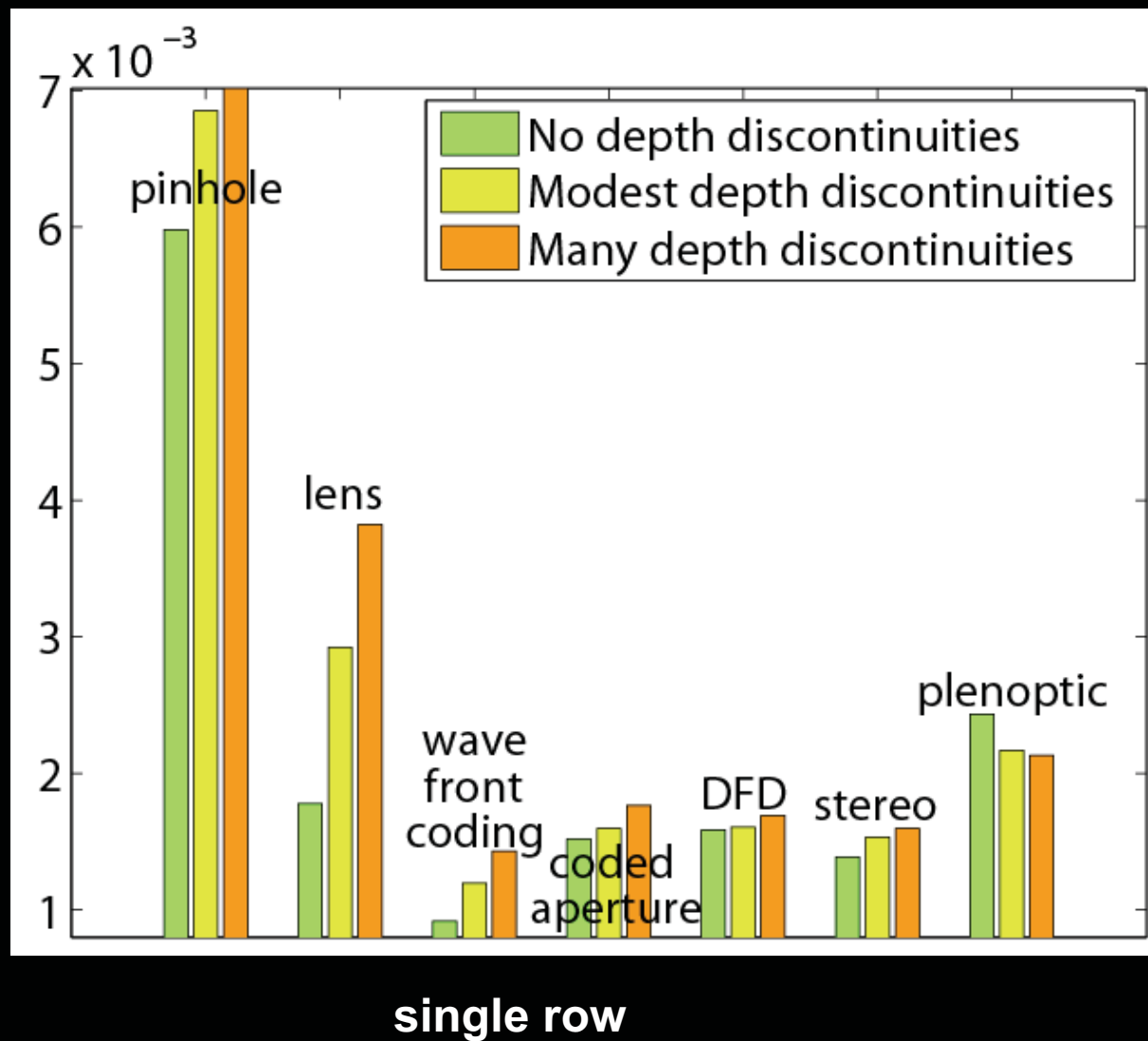
- Model imaging as linear light field projection
- New prior on light field signals
- Camera decoding expressed as a Bayesian inference problem
- Framework and software for comparison across camera configurations, by evaluating uncertainty in light field reconstruction
- Principled novel camera design



full lightfield reconstruction, unclipped plot

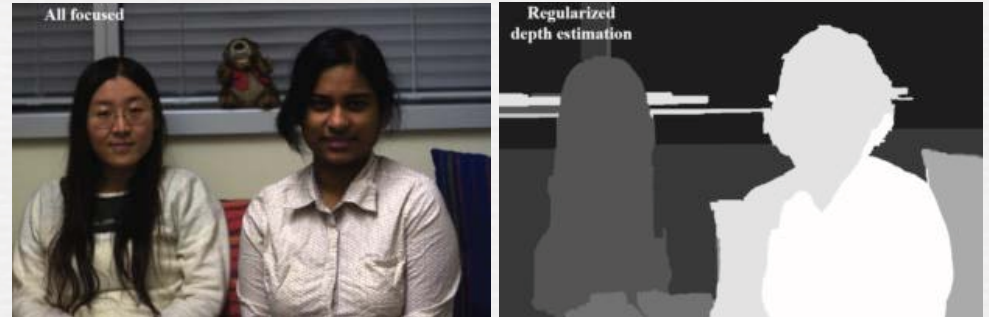


single-row reconstruction, unclipped plot

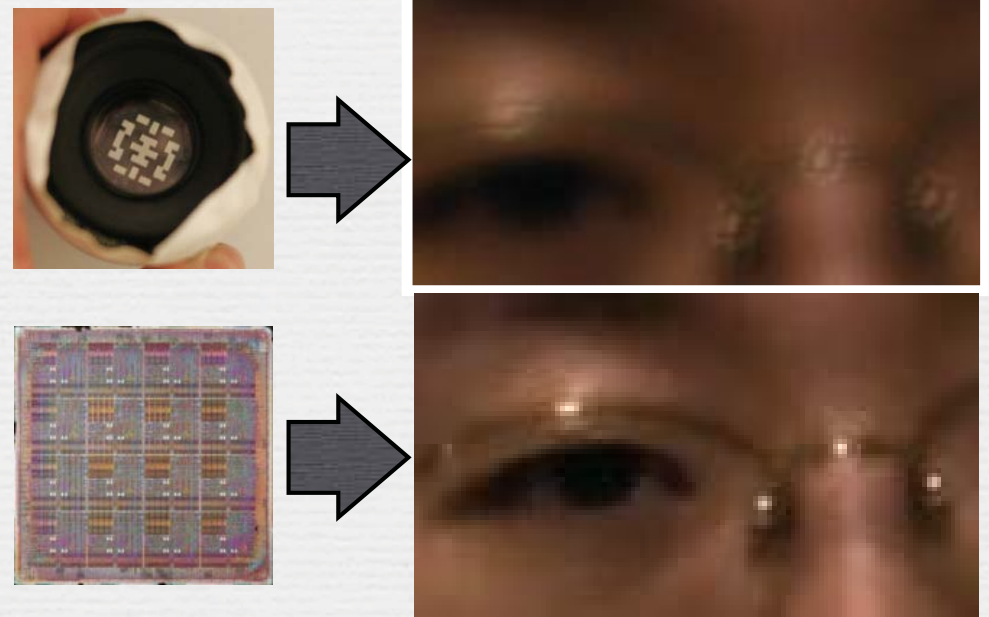


Computational photography

- ◆ Reconstruct more information (light-field / depth)



- ◆ Coding optics,
decoding algorithm



- ◆ Prior on “natural” images (sparse derivative)

$$\sum ||\nabla x||^{0.8}$$



Code search

- ◆ Design constraints:
 - Binary pattern
 - Minimum hole size
=> 1mm^2 (due to diffraction)
 - No floating parts
- ➡ Sample patterns and optimize depth inference (KL divergence)
- ➡ Formal derivation of score function in paper

